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**FINITE ELEMENT NUMERICAL ANALYSIS OF  
THE THERMO-MECHANICAL BEHAVIOUR  
OF AN ENERGY DIAPHRAGM WALL**

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# 1. Introduction

Over the last century the burning of fossil fuels like coal and oil has increased the concentration of atmospheric carbon dioxide (CO<sub>2</sub>) (<https://climate.nasa.gov/causes/>). This happens because the coal or oil burning process combines carbon with oxygen in the air to make CO<sub>2</sub>. To a lesser extent, the clearing of land for agriculture, industry, and other human activities has increased concentrations of greenhouse gases. The consequences of changing the natural atmospheric greenhouse are difficult to predict, but certain effects seem likely: on average, Earth will become warmer and some regions may welcome warmer temperatures, but others may not; warmer conditions will probably lead to more evaporation and precipitation overall, but individual regions will vary, some becoming wetter and others dryer; a stronger greenhouse effect will warm the oceans and partially melt glaciers and other ice, increasing sea level; ocean water also will expand if it warms, contributing further to sea level rise; on the other hand, some crops and other plants may respond favourably to increased atmospheric CO<sub>2</sub>, growing more vigorously and using water more efficiently. At the same time, higher temperatures and shifting climate patterns may change the areas where crops grow best and affect the makeup of natural plant communities. However, the negative aspects are

much more dangerous for our ecosystem which can be totally unbalanced and the effects are likely to become irreversible. Indeed, the industrial activities that our modern civilization depends upon, have raised atmospheric carbon dioxide levels from 280 parts per million to 400 parts per million in the last 150 years. The panel also concluded there's a better than 95 percent probability that human-produced greenhouse gases such as carbon dioxide, methane and nitrous oxide have caused much of the observed increase in Earth's temperatures over the past 50 years (<https://climate.nasa.gov/causes/>).

This phenomenon has been taken into consideration only since 1950 and some measures have begun to come true after the Kyoto Protocol (1997). As a matter of fact, in the last century, becoming aware of this risk, it was thought to push on clean energy provided by earth and employ it for human purpose under the prospective of sustainability. According to the United Nations (the UN's Brundtland Commission popularized the term in 1987), sustainability is defined as "meeting the needs of the present without compromising the ability of future generations to meet their own needs." True sustainability is when everyone, everywhere can meet their basic needs forever. Sustainable energy is energy that we will never use up or deplete, because it is inexhaustible. In particular, it is possible to classify different type of energy on the base of the natural element they take advantage of: water, sun, wind, earth's soil and organic matter are some considerable examples. Knowing the possible form of energy presented on Earth, allows us to create structures capable to use it and make it available to humans. As engineers we have skills and tools to solve or, at least, to reduce this huge problem; as human we have a moral obligation to stop it.

This thesis has the goal to study the behaviour of one of these particular structures: the energy diaphragm walls (EDW), based on the shallow geothermal.

The energy diaphragm walls are able to match two different tasks: the structural one, i.e. retain the soil, and thermal one, i.e. exchange heat with the surrounding soil. The latter skill is ensured by the shallow geothermal energy. Indeed, geothermal energy is thermal energy generated and stored in the Earth's crust. It can be found from shallow ground to several miles below the surface, and even farther down to the extremely hot molten rock, i.e. magma. Indeed, it is possible to classify the geothermal energy resource on the base of the enthalpy which is proportional to temperature distinguishing between high-enthalpy and low-enthalpy systems. The first one has the purpose of producing electricity through deep boreholes and steam turbines, which reach a depth more than 500 m; on the other hand, low enthalpy, exploiting the presence of a heat pump, allows to produce thermal energy from lower values of temperature, generally less than 30°C, taken in the shallow geosphere (no more than 200 m), e.g. for the air conditioning of buildings.

Our study is focused on low-enthalpy resources, i.e. shallow geothermal energy used to couple the structural role of geostructures with the energy supply. The system used is as simple as effective: polyethylene pipes are embedded into the concrete structures, and a heat-carrying fluid circulates through them and exchanges heat with the ground. The pipes are then connected to a heat pump system, which circulates the fluid in the heating-cooling plant of the building. This system allows the heat to be extracted from the ground during winter to satisfy the heating needs of the buildings and injected into the ground during summer, to meet air conditioning

requirements. The advantage of this technology is that it incorporates the geothermal equipment inside geostructures that are already in place for the stability of the construction, reducing the initial costs of installation with respect to other geothermal systems.

However, from the design point of view, it is necessary to take into account the effects that heat exchange have on the reinforced concrete in terms of stress and strain. It is well known that a gradient of temperature causes thermal strains or induced stresses in the material, that need to be added to the operational state of stress in a design stage, but there is still limited evidence on the impact of the thermal cycles on the serviceability and safety performance of the geostructures. Moreover, to justify higher initial costs of the installation, it is necessary to make a preliminary assessment of the effective energy advantages in the operational phase, in terms of energy efficiency of the structure.

A lot of studies have already been made. Starting from Brandl (1998 and 2006), experimental and numerical assessment have been carried out (Gao et al., 2008), to disclose for example the influences on the thermal efficiency of energy piles (Cecinato and Loveridge, 2015), and the geotechnical behaviour of energy piles for different design solutions (Knellwolf et al., 2011, Batini et al., 2015). In the tunnelling field, application of energy equipment in the lining have been tested (Markiewicz and Adam (2006), Franzius and Pralle (2011), Barla et al. (2016), Zhang et al. (2013)), as well as the influence of underground conditions on the heat exchange capacity of energy tunnels (Di Donna and Barla, 2015). Little work has been carried out for energy walls. Concerning retaining walls, thermal and mechanical aspects of their response as shallow geothermal heat exchanger has been investigated by Bourne-Webb et al. (2015 and 2016), as well as the energy

performance of diaphragm walls and their influences by Di Donna et al. (2016), Barla et al. (2017).

### *Aim and objectives*

The core of this thesis is the thermo-mechanical analysis of a real diaphragm wall, part of the car park Ventimiglia (Torino, Italy), under the prospective of installing pipes for geothermal use. For this purpose, the following objectives have been set:

- Develop a model for a thermo-mechanical problem.
- Quantify the stresses along an energy diaphragm wall.
- Identify the displacements due to thermal exchanges.

### *Structure of the dissertation*

The path followed by the thesis is divided into 5 chapters thus defined:

*Chapter 2* starts with an introduction on renewable energy to end up with geothermal energy, especially focusing on low enthalpy geothermal and the geothermal heat pump.

*Chapter 3* is focused on energy geostructures. The functionality of these particular structures is explained, in particular three types of geostructures are analyzed, tunnels, piles and walls, through papers of real cases.

*Chapter 4* develops the coupled thermos-hydro-mechanical analysis, describing the equations that govern the problem. Furthermore, the software LAGAMINE is introduced and the preliminary analyses carried out for an oedometric test are described for three different simulations: mechanical, hydro-mechanical, and thermo-hydro-mechanical.

*Chapter 5* is the core of this work thus a general framework in terms of location, geotechnical condition and geometry of the case study is made. Afterward the model realized in LAGAMINE, the geometry and the boundary conditions are described as material properties and thermos-mechanical analysis. The model is run and comparison with thesis of the colleague A.Santi (Barla et al., 2018).

*Chapter 6* is the last chapter where all the necessary observations and the final results of the thesis are underlined with critical opinion. Moreover, some tips for future analysis are suggested.

## **2. From renewable energy to low enthalpy geothermal systems**

### **2.1 Renewable energy**

Achieving solutions to environmental problems that we face today requires long-term potential actions for sustainable development. In this regard, renewable energy resources appear to be the one of the most efficient and effective solutions. That is why there is an intimate connection between renewable energy and sustainable development.

About 90% of global energy consumption is supplied by non-renewable sources. This is extremely problematic because these resources will soon be exhausted, and most of them are also major greenhouse gas emitters. On the other hand, renewable energy sources (including biomass, biofuels, hydropower, geothermal, solar, and wind) accounted for only 11% of the global energy consumption in 2010, and are projected to account for only 15% by 2040 (from U.S. Energy Information Administration, International Energy Outlook 2013). Of these, solar, wind, geothermal, and hydropower

are the cleanest energy sources as they do not require combustion and therefore have no direct greenhouse gas or air pollutant emissions.

Sure, the sources of energy most commonly used may meet our current needs, but at the rate we are using our current sources, like coal and natural gas, we will burn through them, leaving none behind for future generations, who will then be forced to do what we could already be doing: finding new ways to generate energy.

Just because something works does not automatically mean it cannot be improved. Why should energy be any different? Why should we stand around and wait until a change is the only option? We can make changes today that make lives better for our current generation, creating new jobs while providing clean energy, and also improving the lives of future generations.

Sustainable energy sources are the best sources of energy for our homes and businesses, because they are not only renewable but are also frequently developed closer to the end-user than are traditional power plants.

Here are some examples of clean energy, which are already developed in some countries more than others; however, they are spreading for their efficiency and long term economic benefit.

#### *Solar power*

Photovoltaic (PV) Solar power is harnessing the sun's energy to produce electricity. One of the fastest growing energy sources, new technologies are developing at a rapid pace. Solar cells are becoming more efficient, transportable and even flexible, allowing for easy installation. PV has mainly been used to power small and medium-sized applications, from the

calculator powered by a single solar cell to off-grid homes powered by a photovoltaic array. The 1973 oil crisis stimulated a rapid rise in the production of PV during the 1970s and early 1980s. Steadily falling oil prices during the early 1980s, however, led to a reduction in funding for photovoltaic research and development (R&D) and a discontinuation of the tax credits associated with the Energy Tax Act of 1978. These factors moderated growth to approximately 15% per year from 1984 through 1996 ([www.listverse.com](http://www.listverse.com)). Solar installations in recent years have also largely begun to expand into residential areas, with governments offering incentive programs to make “green” energy a more economically viable option.

#### *Wind power*

Wind power is the conversion of wind energy by wind turbines into a useful form, such as electricity or mechanical energy. Large-scale wind farms are typically connected to the local power transmission network with small turbines used to provide electricity to isolated areas. Residential units are entering production and are capable of powering large appliances to entire houses depending on the size. Wind farms installed on agricultural land or grazing areas, have one of the lowest environmental impacts of all energy sources. Although wind produces only about 1.5% of worldwide electricity use, it is growing rapidly, having doubled in the three years between 2005 and 2008. In several countries it has achieved relatively high levels of penetration, accounting for approximately 19% of electricity production in Denmark, 11% in Spain and Portugal, and 7% in Germany and the Republic of Ireland in 2008 ([www.listverse.com](http://www.listverse.com)). Wind energy has historically been used directly to propel sailing ships or converted into mechanical energy for pumping water or grinding grain, but the principal application of wind power today is the generation of electricity.

### *Hydroelectricity*

Hydroelectricity is electricity generated by hydropower, i.e. the production of power through use of the gravitational force of falling or flowing water. It is the most widely used form of renewable energy. Once a hydroelectric complex is constructed, the project produces no direct waste. Small scale hydro or micro-hydro power has been an increasingly popular alternative energy source, especially in remote areas where other power sources are not viable. Small scale hydro power systems can be installed in small rivers or streams with little or no discernible environmental effect or disruption to fish migration. Most small scale hydro power systems make no use of a dam or major water diversion, but rather use water wheels to generate energy. This was approximately 19% of the world's electricity (up from 16% in 2003), and accounted for over 63% of electricity from renewable sources. While many hydroelectric projects supply public electricity networks, some are created to serve specific industrial enterprises.

### *Tidal power*

Tidal energy can be generated in two ways, tidal stream generators or by barrage generation. The power created through tidal generators is generally more environmentally friendly and causes less impact on established ecosystems. Similar to a wind turbine, many tidal stream generators rotate underwater and are driven by the swiftly moving dense water. Although not yet widely used, tidal power has potential for future electricity generation. Tides are more predictable than wind energy and solar power. Historically, tide mills have been used, both in Europe and on the Atlantic coast of the USA. The earliest occurrences date from the Middle Ages, or even from Roman times. Tidal power is the only form of energy which

derives directly from the relative motions of the Earth–Moon system, and to a lesser extent from the Earth–Sun system. Indeed, the tidal forces produced by the Moon and Sun, in combination with Earth’s rotation.

### *Radiant energy*

This natural energy can perform the same wonders as ordinary electricity at less than 1% of the cost. It does not behave exactly like electricity, however, which has contributed to the scientific community’s misunderstanding of it. The Methernitha Community in Switzerland currently has 5 or 6 working models of fuel less, self-running devices that tap this energy. Nikola Tesla’s magnifying transmitter, T. Henry Moray’s radiant energy device, Edwin Gray’s EMA motor, and Paul Baumann’s Testatika machine all run on radiant energy. This natural energy form can be gathered directly from the environment or extracted from ordinary electricity by the method called fractionation.

### *Biomass*

Biomass, as a renewable energy source, refers to living and recently dead biological material that can be used as fuel or for industrial production. In this context, biomass refers to plant matter grown to generate electricity or produce for example trash such as dead trees and branches, yard clippings and wood chips biofuel, and it also includes plant or animal matter used for production of fibres, chemicals or heat. Biomass may also include biodegradable wastes that can be burnt as fuel. Industrial biomass can be grown from numerous types of plants, including miscanthus, switch grass, hemp, corn, poplar, willow, sorghum, sugarcane, and a variety of tree species, ranging from eucalyptus to palm oil. The particular plant used is usually not important to the end products, but it does affect the processing

of the raw material. Production of biomass is a growing industry as interest in sustainable fuel sources is growing.

### *Wave power*

Wave power is the transport of energy by ocean surface waves, and the capture of that energy to do useful work, for example for electricity generation, water desalination, or the pumping of water (into reservoirs). Wave energy can be difficult to harness due to the unpredictability of the ocean and wave direction. Wave farms have been created and are in use in Europe, using floating Pelamis Wave Energy converters. Most wave power systems include the use of a floating buoyed device and generate energy through a snaking motion, or by mechanical movement from the wave's peaks and troughs. The rising and falling of the waves moves the buoy-like structure creating mechanical energy which is converted into electricity and transmitted to shore over a submerged transmission line.

### *Geothermal energy*

Geothermal energy is a very powerful and efficient way to extract a renewable energy from earth through natural processes. This can be performed on a small scale to provide heat for a residential unit (a geothermal heat pump), or on a very large scale for energy production through a geothermal power plant. It has been used for space heating and bathing since ancient roman times, but is now better known for generating electricity. Geothermal power is cost effective, reliable, and environmentally friendly, but has previously been geographically limited to areas near tectonic plate boundaries, if we consider only the high enthalpy method. Recent technological advances have dramatically expanded the range and size of viable resources, especially for direct applications such as

home heating. The largest group of geothermal power plants in the world is located at The Geysers, a geothermal field in California, United States. As of 2004, five countries (El Salvador, Kenya, the Philippines, Iceland, and Costa Rica) generate more than 15% of their electricity from geothermal sources. Geothermal power requires no fuel, and is therefore immune to fluctuations in fuel cost, but capital costs tend to be high. Drilling accounts for most of the costs of electrical plants, and exploration of deep resources entails very high financial risks. Geothermal power offers a degree of scalability: a large geothermal plant can power entire cities while smaller power plants can supply rural villages or heat individual homes. Geothermal electricity is generated in 24 countries around the world and a number of potential sites are being developed or evaluated.

The latter is more complexed than the way it is just described and, because it is the core of this thesis, it will be well developed in depth in the next chapters.

## **2.2 Geothermal energy**

Geothermal Energy (from the ancient Greek "geo", earth, and "thermos", heat) is, in its broadest definition, the natural warmth of the Earth. The heat is produced mainly by the radioactive decay of potassium, thorium, and uranium in Earth's crust and mantle and also by friction generated along the margins of continental plates. The subsequent annual low-grade heat flow to the surface averages between 50 and 70 mill watts (mW) per square metre worldwide. In contrast, incoming solar radiation striking Earth's surface provides 342 watts per square metre annually. Geothermal heat energy can be recovered and exploited for human use, and it is available anywhere on Earth's surface. The estimated energy that can be recovered and utilized on the surface is  $4.5 \times 10^6$  exajoules, or about  $1.4 \times 10^6$  terawatt-

years, which equates to roughly three times the world's annual consumption of all types of energy. The amount of heat within 10,000 meters of Earth's surface contains 50,000 times more energy than all the oil and natural gas resources in the world (www.statista.com).

The areas with the highest underground temperatures are in regions with active or geologically young volcanoes. These "hot spots" occur at tectonic plate boundaries or at places where the crust is thin enough to let the heat through. How it is shown in Figure 2.1, the Pacific Rim, often called the Ring of Fire for its many volcanoes, has many hot spots, including some in Alaska, California, and Oregon. Nevada has hundreds of hot spots, covering much of the northern part of the state.

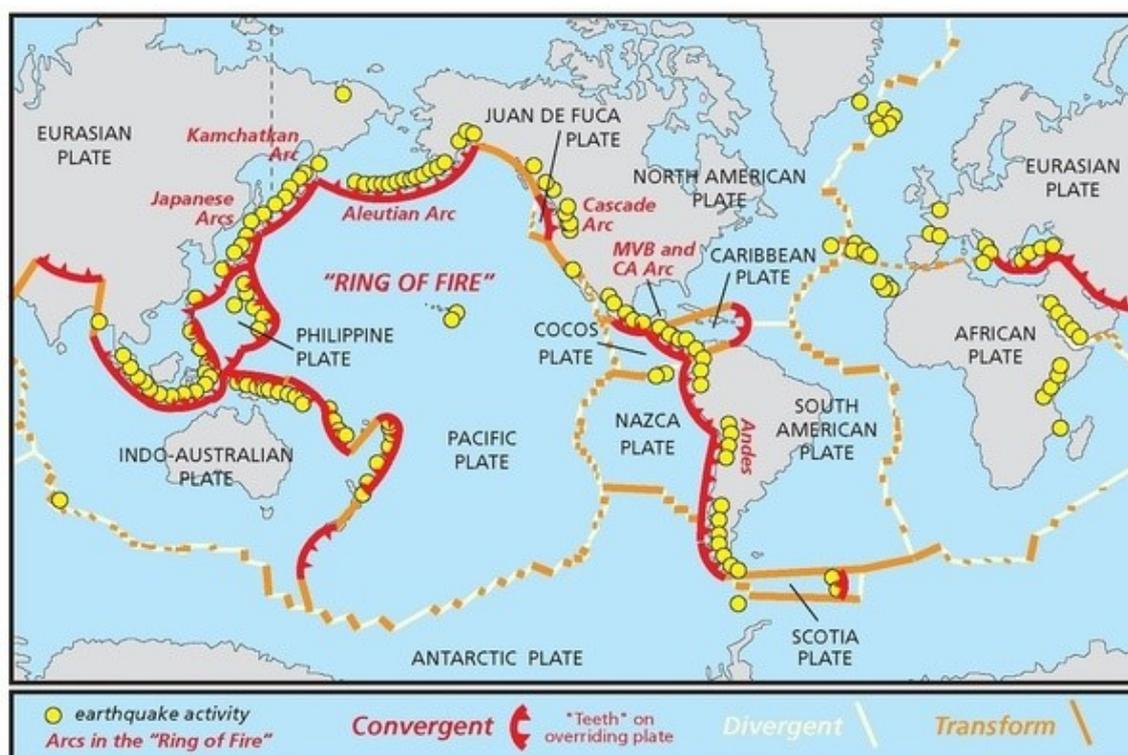


Figure 2.1 Tectonic plates boundaries (www.quora.com)

These regions are also seismically active. Earthquakes and magma movement break up the rock covering, allowing water to circulate. As the water rises to the surface, natural hot springs and geysers occur, such as Old Faithful at Yellowstone National Park. The water's temperature in these systems can be more than 200°C.

Seismically active hotspots are not the only places where geothermal energy can be found. There is a steady supply of milder heat at depths of anywhere from 10 to a few hundred feet below the surface virtually in any location on Earth. Even the ground below your own backyard or local school has enough heat to control the climate in your home or other buildings in the community. In addition, there is a vast amount of heat energy available from dry rock formations very deep below the surface (4–10 km). Using the emerging technology known as Enhanced Geothermal Systems (EGS), we may be able to capture this heat for electricity production on a much larger scale than conventional technologies currently allow. While still primarily in the development phase, the first demonstration EGS projects provided electricity to grids in the United States and Australia in 2013.

It is interesting to analyse the Figure 2.2 which highlights the geothermal energy of Europe-Asia countries. How we can see, there are a lot of potential areas where this green energy can be exploited, e.g. Toscana, Italy.



Figure 2.2 Geothermal energy in Europa-Asia ([www.askjaenergy.com](http://www.askjaenergy.com))

Hence, geothermal energy can be exploited in three different ways, below listed.

2.2.1 Direct use: Probably the most widely used set of applications involves the direct use of heated water from the ground without the need for any specialized equipment. This kind of applications makes use of low-temperature geothermal resources, which range between about 50 and 150 °C. Such low-temperature geothermal water and steam have been used to warm single buildings, as well as whole districts where numerous buildings are heated from a central supply source. In addition, many

swimming pools, balneological facilities at spas, greenhouses, and aquaculture ponds around the world have been heated with geothermal resources. For many of those activities, hot water is often used directly in the heating system, or it may be used in conjunction with a heat exchanger, which transfers heat when there are problematic minerals and gases such as hydrogen sulphide mixed in with the fluid. Geothermal energy is best found in areas with high thermal gradients. Those gradients occur in regions affected by recent volcanism, in areas located along plate boundaries (such as along the Pacific Ring of Fire), or in areas marked by thin crust (hot spots) such as Yellowstone National Park and the Hawaiian Islands.

The total worldwide installed capacity for direct use in 2015 was about 73,290 MWt utilizing about 163,273 GW-hours per year (587,786 TG per year), producing an annual utilization factor of 28% in the heating mode.

**2.2.2 Electric power generation:** Depending upon the temperature and the fluid (steam) flow, geothermal energy can be used to generate electricity. Some geothermal power plants simply collect rising steam from the ground. In such “dry steam” operations, the heated water vapor is funneled directly into a turbine that drives an electrical generator. Other power plants, built around the flash steam and binary cycle designs, use a mixture of steam and heated water (“wet steam”) extracted from the ground to start the electrical generation process.

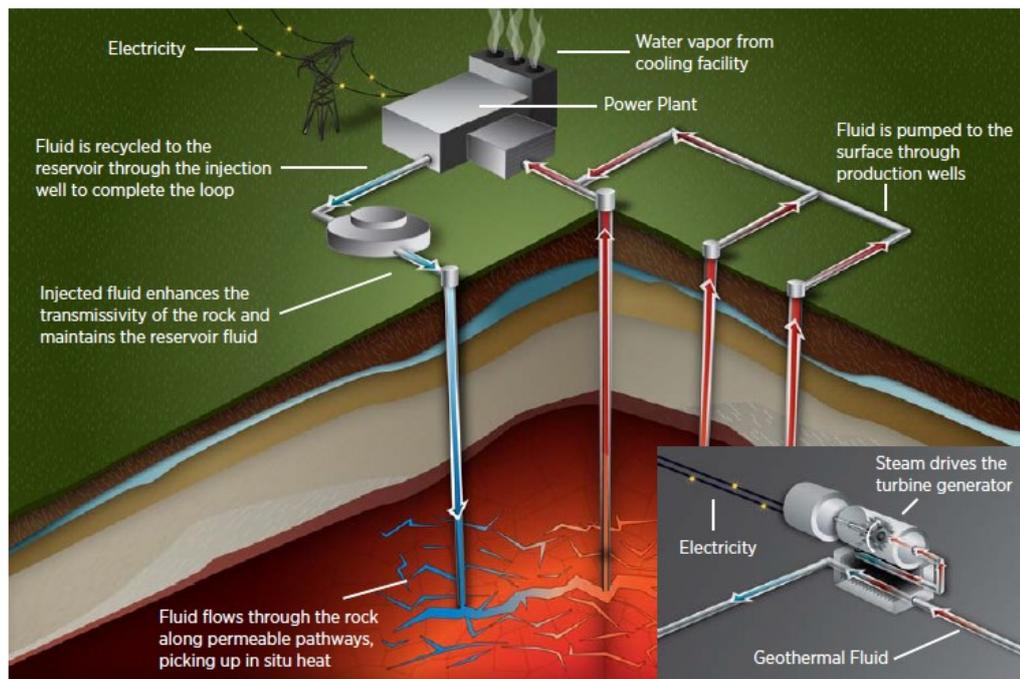


Figure 2.3 Geothermal electricity plant ([www.wikimedia.com](http://www.wikimedia.com))

Electrical power usually requires water heated above 175 °C to be economical, for this reason it needs depths of 4 km and more. In geothermal plants using the Organic Rankine Cycle (ORC), a special type of binary-cycle technology that utilizes lower-temperature heat sources (such as biomass combustion and industrial waste heat), water temperatures as low as 85–90 °C may be used.

The first geothermal electric power generation took place in Larderello, with the development of an experimental plant in 1904. The first commercial use of that technology occurred there in 1913 with the construction of a plant that produced 250 kW.

**2.2.3 Geothermal heat pumps (GHPs):** this one takes advantage of the relatively stable moderate temperature conditions that occur within the first 300 meters of the surface to heat buildings in the winter and cool them in the summer. In that part of the lithosphere, rocks and groundwater occur at

temperatures between 5 and 30 °C. At shallower depths, where most GHPs are found, such as within 6 meters of Earth's surface, the temperature of the ground maintains a near-constant temperature of 10 to 16 °C. Consequently, that heat can be used to help warm buildings during the colder months of the year when the air temperature falls below that of the ground (Figure 2.4). Similarly, during the warmer months of the year, warm air can be drawn from a building and circulated underground, where it loses much of its heat and is returned.

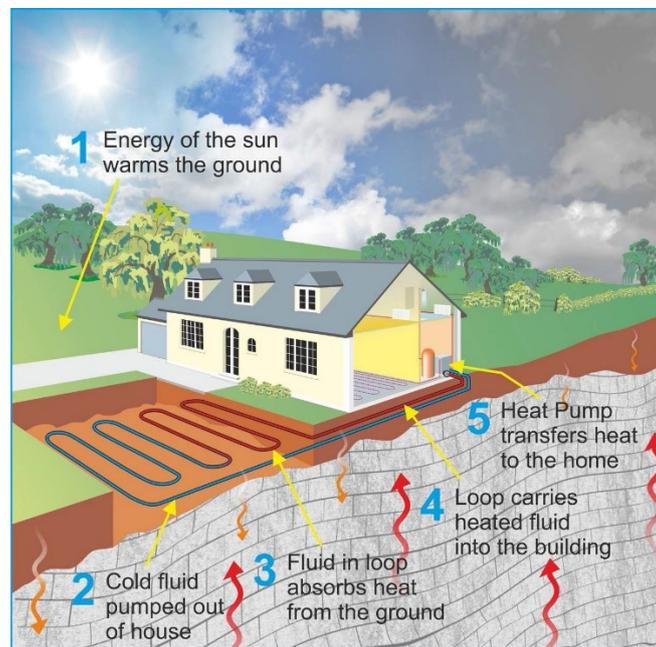


Figure 2.4 Residential heat pump operation for winter heating ([www.isabelbarrosarchitects.ie](http://www.isabelbarrosarchitects.ie))

A GHP system is made up of a heat exchanger (a loop of pipes buried in the ground) and a pump. The heat exchanger transfers heat energy between the ground and air at the surface by means of a fluid that circulates through the pipes; the fluid used is often water or a combination of water and antifreeze. During warmer months, heat from warm air is transferred to the heat exchanger and into the fluid. As it moves through the pipes, the heat is dispersed to the rocks, soil, and groundwater. The pump is reversed during the colder months. Heat energy stored in the relatively warm ground raises

the temperature of the fluid. The fluid then transfers this energy to the heat pump, which warms the air inside the building.

GHPs have several advantages over more conventional heating and air-conditioning systems. They are very efficient, using 25–50 % less electricity than comparable conventional heating and cooling systems, and they produce less pollution. The reduction in energy use associated with GHPs can translate into as much as a 44% decrease in greenhouse gas emissions compared with air-source heat pumps (which transfer heat between indoor and outdoor air). In addition, when compared with electric resistance heating systems (which convert electricity to heat) coupled with standard air-conditioning systems, GHPs can produce up to 72% less greenhouse gas emissions.

Clearly there are many advantages of geothermal energy. It can be extracted without burning a fossil fuel such as coal, gas, or oil; geothermal fields produce only about one-sixth of the carbon dioxide that a relatively clean natural-gas-fueled power plant produces; binary plants release essentially no emissions; unlike solar and wind energy, geothermal energy is always available, 365 days a year. It's also relatively inexpensive; savings from direct use can be as much as 80% over fossil fuels. For these reasons, geothermal energy is starting to spread worldwide, with peaks of concentration in Europe and United State of America, as shown in Figure 2.5. Nevertheless, there are some countries that do not have any geothermal implants because of the maybe only disadvantage that geothermal energy present: initial costs. Indeed, a geothermal implant for a house can reach the initial cost of 15-20 thousand euros, which is twice the photovoltaic implant cost. Nevertheless, they can allow an annual economic saving on operating costs compared to a traditional system (natural gas boiler and split air

conditioner) of about 50% and about 70-80% compared to a boiler plant fueled by LPG or diesel oil. Therefore, the cost disadvantage it can be seen as a long-term investment from which you can reap the benefits from 2 to 8 years.

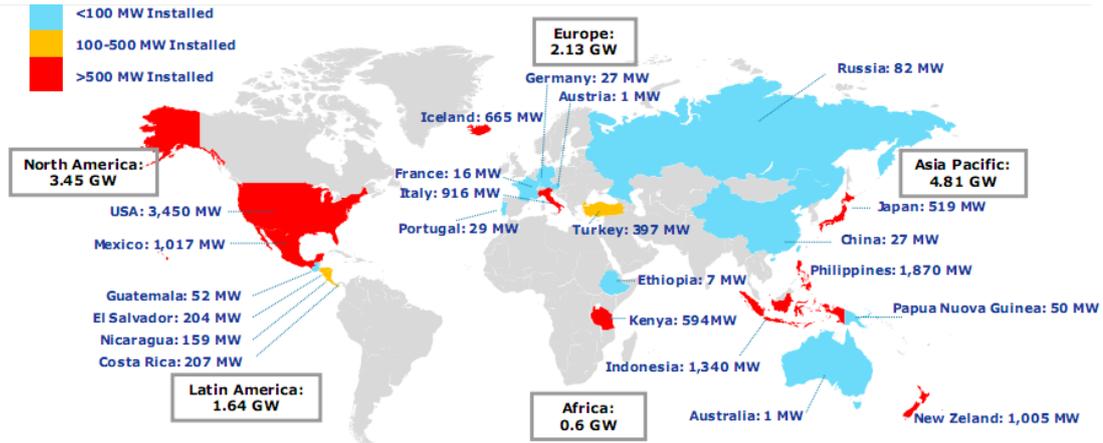


Figure 2.5 Geothermal installed capacity (MW) 2015 ([www.oilprice.com](http://www.oilprice.com))

### 2.3 Low enthalpy geothermal systems

Clearly, the core of the system is the geothermal heat pump (GHP) which consist of:

- a compressor that increases the pressure and temperature of the circuit fluid that enters inside the compressor in the vapor state;
- a heat exchanger (condenser) in which the steam is heated, giving heat to the building to be heated (in the heating mode) or to the outside (in the case of cooling mode), condensing and passing to the liquid state;
- an expansion valve that further cools the liquid temperature and lowers the pressure;

- a further heat exchanger (evaporator) in which the low-pressure and low-temperature liquid exiting from the expansion valve is able to absorb heat (either from a "cold" source - such as the subsoil - in the operating mode for heating, or from the building when the system operates in cooling mode) and then switch back to the steam state, from which a new work cycle resumes.

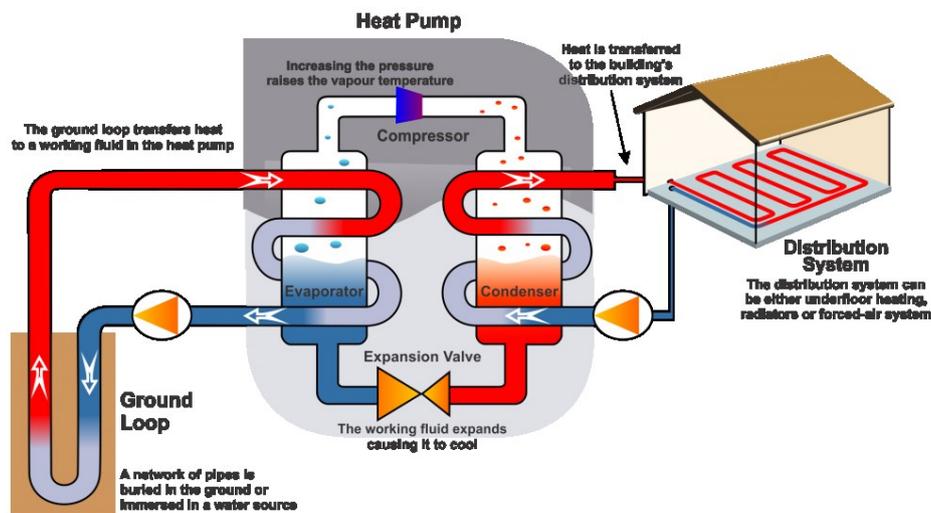


Figure 2.6 Scheme of a Geothermal Heat Pump ([www.tidewatermechanical.com](http://www.tidewatermechanical.com))

Geothermal systems are efficient, environmentally-sensitive, comfortable, and economical. Operating savings often provide paybacks of considerably less than five years, sometimes less than two years. However, this type of plants can work only if the temperature is lower than 50°C, hence, in heating mode, they must necessarily be coupled with low temperature systems such as radiant panels (wall or floor) or fan.

### 2.3.1 Types of Geothermal Heat Pump system

There are four basic types of ground loop systems. Three of these (horizontal, vertical, and pond/lake) are closed-loop systems. The fourth type of system is the open-loop option. Which one of these is best depends

on the climate, soil conditions, available land, and local installation costs at the site. All of these approaches can be used for residential and commercial building applications.

The ground-coupled heat pump system consists of a reversible vapour compression cycle that is coupled with a heat exchanger in the form of bore holes in the ground. These types of systems can use both a water-to-air heat pump or a direct-expansion heat pump.

***Ground-coupled heat pump system:*** Also referred to as a closed-loop heat pump, the water-to-air configuration circulates water or a water and antifreeze solution through a liquid-to-refrigerant heat exchanger and a series of buried thermoplastic piping. In comparison, the direct-expansion heat pump circulates a refrigerant through a series of buried copper pipes. Both vertical and horizontal heat exchanger configurations are used in these applications.

- *Vertical* wells generally consist of two small (1.2 m to 30 cm) diameter high-density polyethylene tubes in a vertical borehole filled with a solid medium, commonly referred to as grout. Boreholes typically range from 15 m to 200 m, depending on the local site conditions, including soil thermal conductivity and availability of equipment. Because of this configuration, vertical wells require relatively small areas of land compared to horizontal trenches.
- *Horizontal* wells generally require the greatest amount of ground area and it can be further divided into three subgroups: single-pipe, multiple pipes, and spiral-slinky. Single-pipe horizontal ground-coupled heat pumps are typically installed in a single trench to a depth of 1.2 m to 2 m and require the most ground area of the three.

While the required ground area required for multiple pipes, consisting of two to six pipes placed in a single trench, can be reduced, the total pipe length must be increased to overcome the interference from adjacent pipes. Recommended trench lengths for the spiral pipe configuration can be 20% to 30% of single pipe trench lengths, but may be increased to achieve greater thermal performance.



Figure 2.7 Closed loop system: vertical  
([www.firstgeothermalenergy.com](http://www.firstgeothermalenergy.com))



Figure 2.8 Closed loop system: horizontal  
([www.firstgeothermalenergy.com](http://www.firstgeothermalenergy.com))

While the vertical well configuration can yield the most efficient ground-coupled heat pump performance, due to reduced variability in soil temperature and thermal properties along with reduced piping and associated pump energy, costs associated with vertical wells are typically more. The expense of equipment required to drill the boreholes along with the limited availability of skilled contractors also contributes to the higher costs. Because of the reduced installation costs, horizontal trenches are widely used in residential applications. However, these systems generally operate at a reduced efficiency due to the impact of seasonal soil property fluctuations and higher pumping energy requirements. Vertical systems are typically installed in large buildings with limited land area.

***Groundwater Heat Pump Systems:*** Preceding the development of ground-coupled heat pump systems, groundwater heat pump one were the most widely used type of geothermal heat pump system. This type of process uses well or surface body water as the heat exchange fluid that circulates directly through the heat pump system. Once it has circulated through the system, the water returns to the ground through the well, a recharge well, or surface discharge.

A typical groundwater heat pump system design consists of a central water-to-water heat exchanger between the groundwater and a closed water loop that is connected to water-to-air heat pumps located in the building. An alternate strategy is to circulate the ground water through a heat recovery chiller that is isolated with a heat exchanger and used to heat and cool the building through a distributed hydronic loop.

Under the right conditions, groundwater heat pump systems can cost less than ground-coupled heat pump one. For this reason, along with the compact space requirements for the water well and availability of water well contractors, this technology has become popular in large commercial applications and has been used for decades.

Nevertheless, potential corrosion issues may require the installation of an intermediate plate-type heat exchanger to protect the heat pump unit; but the hitch is site-specific and should be evaluated where the technology is to be installed.

Last but not least, an open loop system can be used only where there is an adequate supply of relatively clean water and all local codes and regulations regarding groundwater discharge are met.

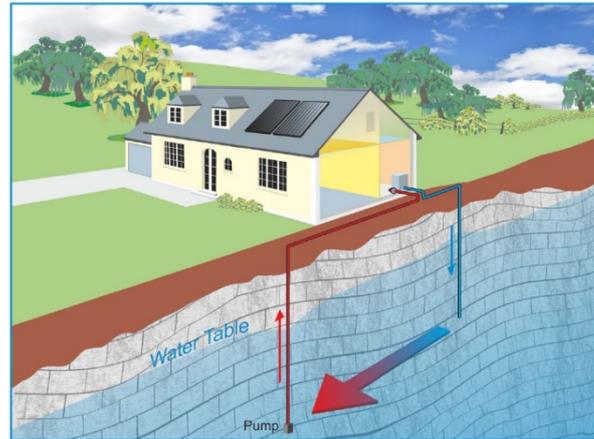


Figure 2.9 Open loop system ([www.gsi.ie](http://www.gsi.ie))

**Surface water heat pump system:** While the thermal properties of surface water bodies are quite different than other geothermal heat pump technologies, the applications and strategies are similar. Surface water heat pump systems can be either closed-loop systems, similar to ground-coupled heat pumps or open-loop systems, similar to groundwater heat pumps.

Closed-loop surface water heat pumps consist of water-to-air or water-to-water heat pumps connected to piping loops placed directly in a lake, river, or other open body of water. A pump circulates water or a water and antifreeze solution through the heat pump water-to-refrigerant heat exchanger and the submerged piping loop which transfers heat to or from the body of water.

Open-loop surface water heat pumps can use surface water bodies in a similar way that cooling towers are used, but without the fan energy and required maintenance. Lake water can be pumped directly to water-to-air or water-to-water heat pumps.

Because of reduced excavation costs, closed-loop surface water heat pumps can cost less than typical ground-coupled heat pump systems. While these systems have reduced pumping energy and operating costs along with low maintenance requirements, there is the possibility of coil damage in public lakes and variable performance in small and shallow bodies of water resulting from the wide fluctuation of water temperature.



Figure 2.10 Pond loop system ([www.waterfurnace.com](http://www.waterfurnace.com))

### 2.3.2 Efficiency of a GHP

Regardless of the application, the best way to measure the efficiency of a heat pump itself is to report the amount of energy that is pumped relative to the amount that must be added to do the pumping. This ratio is called the Coefficient of Performance:

$$\text{COP} = \frac{\text{quantity of heat delivered [kW]}}{\text{energy required by pump [kW]}}$$

In spite of the first law of thermodynamics, which tells us that energy can neither be created nor destroyed, a GSHP in a good installation can yield up to four units of heat for each unit of electricity consumed. The heat pump is not creating this energy, but merely separating a medium temperature from the ground into warmth (which can be used for heating) and cold (which

can be returned to the ground). A COP=4 it is not always achievable, indeed, a typical efficient air conditioner has a COP of about 3.5: this means it can remove heat at a rate of about 3.5 kW while consuming about 1 kW of electrical energy.

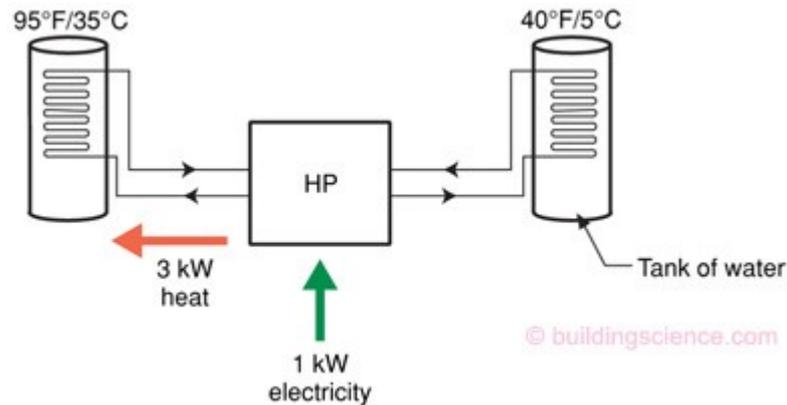


Figure 2.11 Efficiency of a GHP: COP ([www.buildingscience.com](http://www.buildingscience.com))

The COP will vary with each installation, but the lower the output temperature to the heat distribution system is, the higher the COP will be. If an output temperature of 60°C is needed to heat radiators the COP is likely to fall to level of only 2.5. If the heat distribution is to a well-designed underfloor heating system that works well at an output temperature of 40°C, then the COP can rise to a level of 4.

The input temperature is also critical to the COP of the heat pump. The higher the input temperature from the ground, the lower the amount of work needed from the heat pump, the higher the COP will be. In fact, the critical factor is the “uplift” between the source temperature and the output temperature.

GSHP are unique in that their reported COP efficiency may not include the energy of the fluid or water pump required to move the fluid through the tubes in the ground. This electrical energy can be significant, particularly if

the loop is long, the pipes are small, or the flow resistance within the heat pump unit is large. The largest factor in pump energy use is design: if the designer and installer of the loop and the pump are not careful, a major amount of energy can be consumed. Heat also needs to be removed by a fan or a pump and distributed to the home. To improve heat pump COP, the hot temperature of the liquid produced is often much lower than for a boiler or furnace, i.e. the lift is less. Hence, fan energy can be increased over that of a furnace. This effect is very small in systems that use low temperature radiant heating systems (circulation pumps consume relatively little electrical energy).

This leads to a more accurate definition of efficiency for a GSHP system (System Coefficient of Performance):

$$SCOP = \frac{\text{useful heat delivered}}{(\text{loop pump energy} + \text{heat pump energy} + \text{distribution fan or pump energy})}$$

In heating mode in a cold climate, the system COP of a heat pump rated at COP=4+ can easily drop to COP=3. In our experience, a system COP of 3 for a heat pump in heating mode would be considered good in cold climates (cold soil) even with very efficient heat pump equipment and well-designed and installed pumps. Field heating mode COP values of as high as 4 are possible in warmer climates (warmer soil) and with the best design and best equipment.

In cooling mode in mixed and cool climates, summer time system COP values tend to be higher because the ground temperature in summer are close to the desired air conditioning coil temperature, whereas during winter, the heating coil temperature is far from the winter ground temp. That said, the electrical energy to run the pumps, fans and compressor of the whole system is useful heat in the winter (the inefficiency in the motors

results in heating, which is the whole purpose) and increases the cooling load in summer (all of the inefficiency results in heat, which then has to be removed by the heat pump).

## 3. Energy geostructures

### 3.1 Introduction to energy geostructures

The geostructures are structures designed from the point of view of geotechnics, i.e. they are structures designed to transfer loads to the soil and some of them, like tunnels, are used to integrate engineering with nature. Some practical examples of geostructures are: retaining wall, tunnels, foundation piles and diaphragm walls.

In the last century, it was thought to fuse together the need for ever-increasing renewable energy and geotechnical engineering. Hence, energy geostructures were designed.

Energy geostructures can link the geostructural role to the energy supply, using the principle of a ground source heat pump system. Indeed, energy geostructures present pipes directly installed in the reinforced concrete structural element, usually fastened to the steel bars to guarantee continuity and reinforce the structure (Amis et al., 2010). Moreover, the only use of elements conventionally designed and realized to perform a structural function, assure success in term of cost.

Brandl (2006) explains, in a simple way, how a thermo-active system works. Basically there are two circuits: the primary circuit contains closed pipework in earth-contact concrete elements (piles, diaphragm walls,

columns, etc.) through which a heat carrier fluid is pumped that exchanges energy from the building with the ground. The fluid is a heat transfer medium of either water, water with antifreeze (glycol) or a saline solution. It is shown that glycol–water mixtures are the best option, especially because containing also additives to prevent corrosion in the header block, of valves, of the heat pump, etc.

The secondary pipework is a closed fluid-based circuit embedded in the floors and walls of buildings or bridge decks, road structures, etc. A heat pump connects the two closed circuits, in which heat exchange occurs, as it is shown in the figure below. The main charge of the pump is to increase the temperature level from 10-15°C to 25-35°C. Hence, a low electrical energy is required to raise the originally non-usable heat resources to a higher, usable temperature.

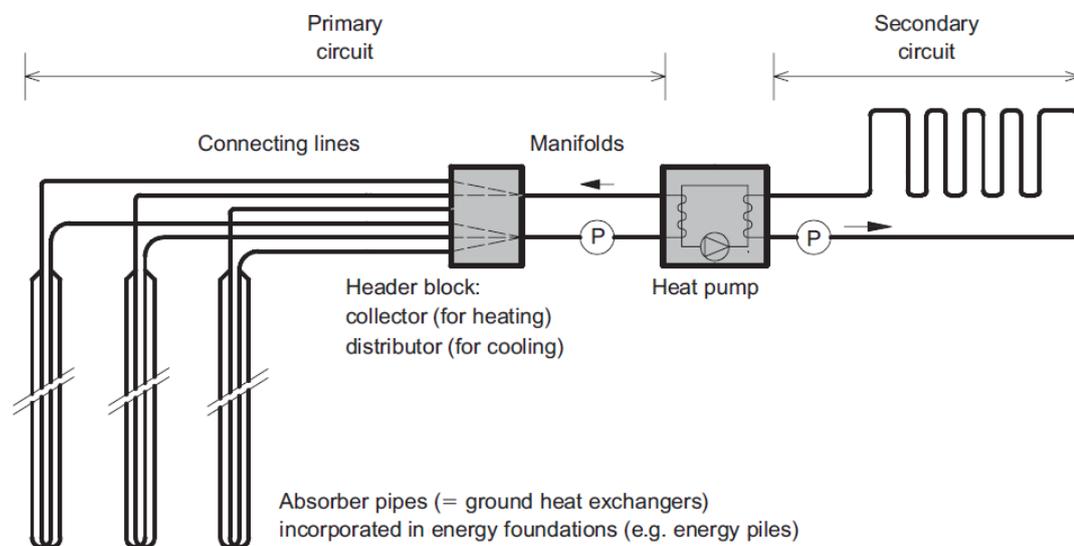


Figure 3.1 Thermo-active system of energy geostructures (Brandl, 2006)

The use of civil engineering structures that are in contact with the ground to replace the more conventional heat-exchange methods is creating great interest in many countries. Bearing piles have been used for this purpose

since the mid-1980s and since the mid-1990s, retaining walls also (Brandl, 2006). Energy geostructures are now common in Austria, Germany and the UK. However, the lack of technical evidence regarding the impact of the thermal cycles on the serviceability and safety performance of the geostructures is one of the major obstacles that are preventing the complete acceptance of the system by the countries.

For this reason, many authors have conducted studies related to energy geostructures to strengthen their efficiency. Brandl (2006) described the use of energy walls at a rehabilitation centre in Austria and Section LT24 of the Lainzer tunnel near Vienna, both of which involved the use of piled retaining walls, and underground stations on the Vienna Metro U2 line that used diaphragm walls. Suckling and Smith (2002) describe the first use of energy walls in the United Kingdom where an installation at Keble College, Oxford included a thermally-activated, bored pile retaining wall in addition to thermally-activated bearing piles. A bored pile type wall was also used in a shallow geothermal energy system installed in the Palais Quartier development in Frankfurt, Germany (Katzenbach et al., 2013). Amis et al. (2010) describe the UK's first thermally-activated diaphragm wall system that was constructed for the new Bulgari Hotel in Knights bridge, London. Diaphragm walls and bearing piles formed as part of the construction for the new Shanghai Museum of Natural History have been thermally-activated to provide heating and cooling to the museum (Xia C. et al., 2012).

As just said, some articles were published to highlight strength and weakness of geothermal system, however, being a relatively new field, there is still much to analyze. To do this, first it is necessary to report specific examples of each geostructures, in particular: tunnels, piles and diaphragm walls.

### 3.2 Energy Piles

Figure 3.2 gives a partial view of the absorber pipes fitted to the reinforcement cage of a large-diameter bored energy pile.



*Figure 3.2 Energy Pile (Brandl, 2006)*

The percentage of (large-diameter) bored piles has been steadily increasing since the year 2000. The piles consist of 5 m long standard elements that can easily be assembled to longer sections during the driving procedure. The tubes are filled under pressure with concrete and shaft grouting to increase friction is also possible.

Austria is the main promoter of this type of energy geostructures, indeed, since 1985 more than 1 million metres of cast iron piles have been installed. At present, about 130000 m are driven every year, with an increasing proportion of energy piles. As known, the heat exchangers are inserted into the fresh concrete, and have to be secured against uplift until the concrete has sufficiently hardened (Brandl, 2006). The standard diameter of such driven piles is  $d = 42.5$  mm, but this can be increased significantly by shaft grouting. Nevertheless, the geothermal effectiveness of such thin energy

piles is smaller than that of driven precast concrete piles or large-diameter bored piles, despite the high thermal conductivity of cast iron. The small diameter enables the installation of only one pipe loop and no coiled piping. Moreover, the contact area with the ground is relatively small. In soft soils, buckling of the piles also has to be considered.

Di Donna and Laloui (2014) investigated, numerically, the behaviour of energy piles foundations during heating-cooling cycles, through combined effects of mechanical and thermal loading on both single pile and raft deep foundations. What it is take into account in this section, are the displacements due to thermal cycles of a raft deep foundation, as figure 3.3 shows.

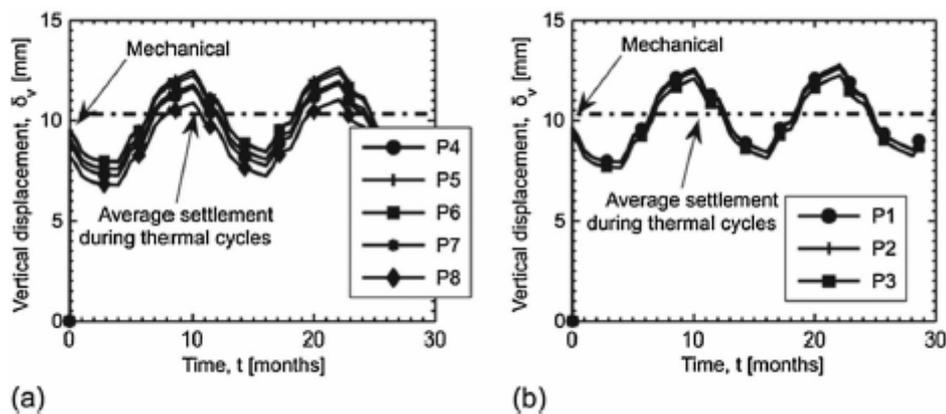


Figure 3.3 Evolution of vertical displacements during thermal cycles at the piles head for (a) central piles and (b) external piles (Di Donna and Laloui, 2014)

The central piles (P1, P2 and P3) start from the same mechanical-induced settlement of roughly 1 cm, and their response during heating and cooling is definitely similar. The effect of the thermoplastic response of the soil corresponds to 1 mm additional irreversible settlement, but it is negligible with respect to the mechanical one.

The vertical reversible displacement due to the thermos-elastic deformation of the pile (upwards during heating and downwards during cooling) has total amplitude of 4 mm. The external piles (P4, P5, P6, P7 and P8) have a differential displacement, although small, between them and with respect to the central ones. However, the thermal loading does not enhance it, and for these piles, the same conclusions drawn for the central ones can be made. The same observation has made for a single pile.

In the design practice, is important to analyse this aspect, i.e. displacement, hence stresses. When subjected to a temperature variation, a pile deforms thermally but a portion of its free thermal deformation is prevented and generates additional stresses in the pile that are compressive during heating and tensile during cooling.

Moreover, the interface shear stress, which is mobilized upwards during axial compressive mechanical loading, is mobilized both upwards and downwards during thermal loading depending on the pile deformation and position of the null point. Whereas the heating-induced compressive stress, is admissible with respect to the concrete strength and the cooling-induced reduction of compressive stress inside the central pile is observed. The admissibility of the maximum compressive stress during heating with respect to the concrete strength, as well as the development of tensile stress during cooling, depends also on the entity of the mechanical induced stress. The last observation reported, is the important difference between a single pile and a group of them. For a single pile it is valid the theory according to which the higher the thermal-induced observed deformation and the lowest the thermal-induced stress, but for a group of energy piles is not the same. This is attributed to the presence of the slab and to the consequent redistribution of stresses from the external piles to the central ones that

result to be consequently more charged. The response is likely to be sensitive to the slab stiffness: the more rigid the slab, the more the response will be governed by it and the less rigid the slab, the more the response will be governed by the single pile behaviour. Nevertheless, the simulations show that the problem of the eventual development of tensile stress inside the piles after the cooling phase might be enhanced by the presence of a rigid slab with respect to the case of an energy pile considered alone.

### **3.3 Energy tunnels**

During the last years, considerations were made how the technology can be extended to tunnels. In comparison with building foundations, substantially larger ground volumes can be activated for geothermal heat use. In high overburden tunnels, significantly higher temperatures can also be utilized. In addition, shallow tunnels, like those for metros, can be used profitably for geothermal heat production. The first application of this kind can be found in the Lainzer tunnel in Austria (Adam & Markiewicz, 2009). For the installation of absorbers in tunnels, cut-and-cover and mined tunnels have to be differentiated. For cut-and-cover tunnels, the well proven methods already used in deep foundations are tapped. For mined tunnel construction, new developments are necessary (Unterberge et al., 2005). Moreover, with existing methods, the equipment of the invert of tunnel tubes can be realized and research activities for the development of suitable absorber systems were performed to use the inner lining.

When mechanized tunnelling is used, the tunnel segmental lining optimized for heat exchange is precast in factory and then placed on site by the tunnel boring machine (TBM) (Frazius and Pralle, 2011; Barla and Perino, 2014). The system could also allow cooling the tunnel using the heat

produced internally by fast moving trains or vehicles. The heat exchanged at the tunnel level can be transferred to the surface by placing pipes into the ventilation shafts or through the portals (Barla and Di Donna, 2018). The stations of metro tunnels can also be used for this purpose.

The pipe line length can be optimized in order to reduce heat losses (Barla et al., 2016) and the system can be used to allow heat distribution at the district scale.

It is possible to do a distinguish between “cold” and “hot” tunnels in base of their thermal conditions.

In cold tunnels, all year round, the air temperature is roughly 15°C, and it is not increased by the passage of trains. Generally, the diameter of this type of tunnel is large (around 10-12 m).

The prevailing temperatures in the tunnel only have a limited effect on the temperature in the surrounding ground.

Indeed, hot tunnels, usually present high internal temperatures. Urban tunnels (diameters around 7 m), during summer, can reach an air temperature of 30°C. Rapid cycle frequency of trains leads to additional heat, therefore the air temperatures in the tunnel, which warms the ground. Moreover, deep tunnels could be heated by the ground itself, which can achieve a temperature of 50°C.

Barla et al. (2016) studied the thermal activation of the South extension of the Metro Torino line 1. The line connects Fermi station to Porta Nuova since 2006, while a second section was constructed between 2006 and 2011 to connect Porta Nuova and Lingotto stations, for a total length of 13.4 km.

The portion considered to test the energy tunnel technology, with the ENERTUN patent, is the new south extension of the line toward Piazza Bengasi (Figure 3.4), which is currently under construction.



Figure 3.4 Map of Turin Metro Line 1 along with a picture of the Enertun experimental site (Barla et al., 2019)

The tunnel has approximately 8 m of diameter, excavated by shielded EPB TMB (Earth Pressure Balance Tunnel Boring Machine). The tunnel lining is made of precast concrete rings (thick-ness 30 cm), each constituted by 7 segments mounted by the TBM itself (Barla et al., 2016). Cement foam is injected to guarantee full contact with the ground and the segments are appropriately sealed in order to avoid groundwater ingress. The average cover of the tunnel is 21.5 m and excavation takes place below the water table. From the thermal point of view, the tunnel is of a cold type as ventilation is guaranteed by a number of wells that inject external air into it. All the knowledge on the Turin subsoil properties and conditions is supported by various amounts of data (Bottino and Civita, 1986; Barla and Barla, 2005, 2012; Barla and Vai, 1999). In addition, in order to allow for easy

inspection during the tunnel lifetime, with the metro system in service, the inflow pipe and the outflow pipe is located in the sidewalls of the tunnel, below the security pedestrian footpath. In the specific case, the described system would allow to activate a total length of tunnel of 1350 m.

Regarding the pipes are able to withstand high pressures and temperatures, resist to corrosion and guarantee high durability. Furthermore, the ENERTUN patent, leaded by Barla and Di Donna, suggest a layout of pipes perpendicular to the tunnel axis (Figure 3.5) . Thus, thanks to the groundwater flow perpendicular to the tunnel axis, imply a head losses reduction of 20-30% (Barla et al., 2016).

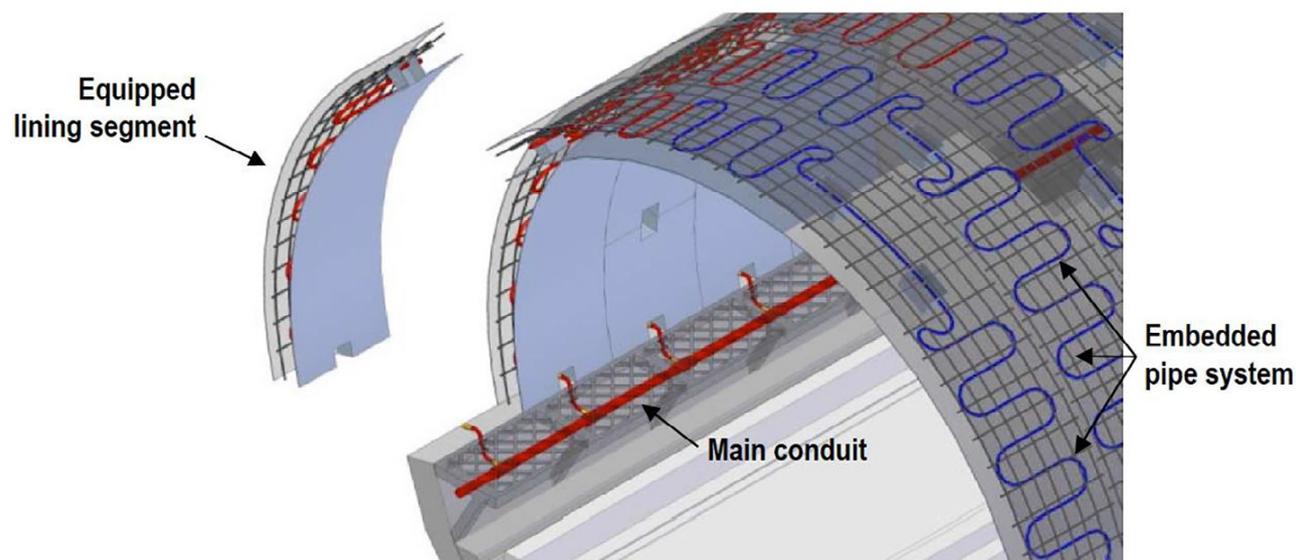


Figure 3.5 Schematic representation of a tunnel segmental lining equipped as ground heat exchanger (Barla et al., 2016)

Two rings of segmental lining were fully equipped with the ground and air net of pipes for a total of 12 ENERTUN segments. The two nets of pipes, one close to the extrados (tunnel surface in contact with the ground), and the other close to the intrados (tunnel surface in contact with the air) allowed to test alternatively three different configurations of the ENERTUN energy tunnel precast segmental lining (Barla et al., 2019). The figure below shows the main steps that characterized the preparation of the segments.



Figure 3.6 Preparation stages of energy segments: (a) moulding, (b) casting, (c) demoulding and (d) circulation test. (Barla et al., 2019)

For this case, it was used as thermo-fluid circulating into the pipes, a propylene glycol mixed with water that can work down to a temperature of  $-20^{\circ}\text{C}$ . The inlet temperatures of  $4^{\circ}\text{C}$  for winter (heating mode) and  $28^{\circ}\text{C}$  for summer (cooling mode) were assumed.

One of the many studies done on the Line 1 South Extension is about the changing of soil's temperature around the tunnel due to geothermal system in a time frame of 3 years (Figure 3.5).

As shown in Figure 3.7, at 2 m distance from the tunnel contour, there is the most changeable area and to avoid the progressive heating or cooling of the ground with time, the most optimised solution is to use the system both for heating and cooling.

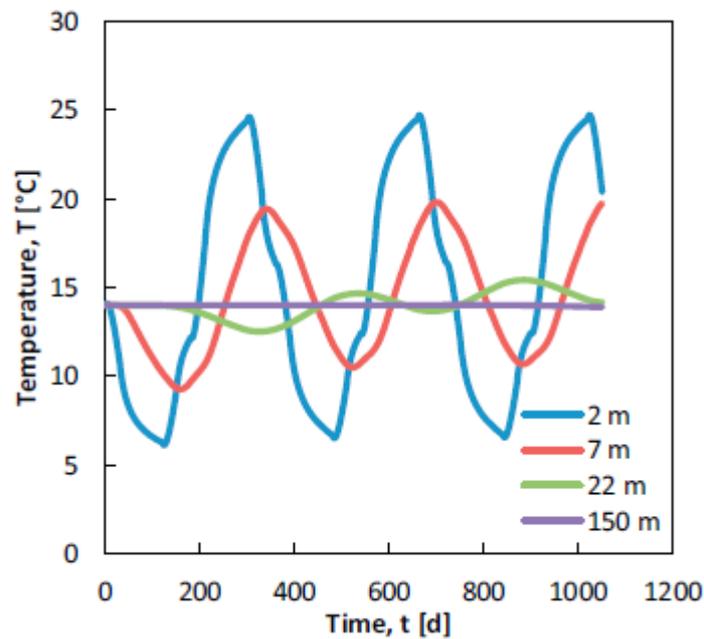


Figure 3.7 Temperatures in the soil at different distance from the tunnel during three years of cycling heating and cooling (Barla, Di Donna, & Perino, 2016)

Moreover, the energy tunnel system would allow exchanging between 53 and 74 W/m<sup>2</sup> of tunnel lining in winter and in summer respectively. If it is considered the total length of the tunnel, the extracted heat is 1.67 kW (heating mode) and injected 2.34 kW (cooling mode). Owing to the favourable underground water flow conditions in Torino, which allows a continuous thermal recharge of the ground, significant improvement of the heat extraction and injection efficiency is guaranteed.

In conclusion, it has been demonstrated that the additional cost required to activate the tunnel lining is less than 1% of the total cost of the project so that the thermal activation of the tunnel lining is 41% less expensive than using vertical piles with ground source heat pumps to cover the same energy requirement.

Because of the very promising results, a test site was recently installed in the tunnel under construction to validate the results found and provide quantitative information for future installations (Barla, Di Donna, & Insana,

2017). In terms of heat exchange, for example, thermally active tunnels could allow exchanging from approximately 10–20 W/m<sup>2</sup> when no groundwater flow is present, and up to 50–60 W/m<sup>2</sup> when there is significant groundwater flow.

Finally, from Di Donna et al. (2017) paper, it is possible to highlight some key aspects for energy geostructures such as tunnels. Indeed, with respect to cut-and-cover tunnels and underground tunnels in urban areas, these are more likely to be constructed in saturated soils and will be less influenced by the external air temperature variation as a result of their higher cover, this should at the same time improve their heat exchange potential. An additional aspect which must be considered specifically for tunnels, that is not necessary with energy piles, is the effect of temperature and speed of the air inside the tunnel or underground space (Nicholson et al., 2014). These energy geostructures will exchange heat not only with the ground, but also with the air inside the underground space. In the case of hot tunnels this might represent an additional source of heat during winter, but a drawback during summer. Some examples of heat exchange in real energy tunnel are plotted in the following chart, where it is evident to understand what is was said before.

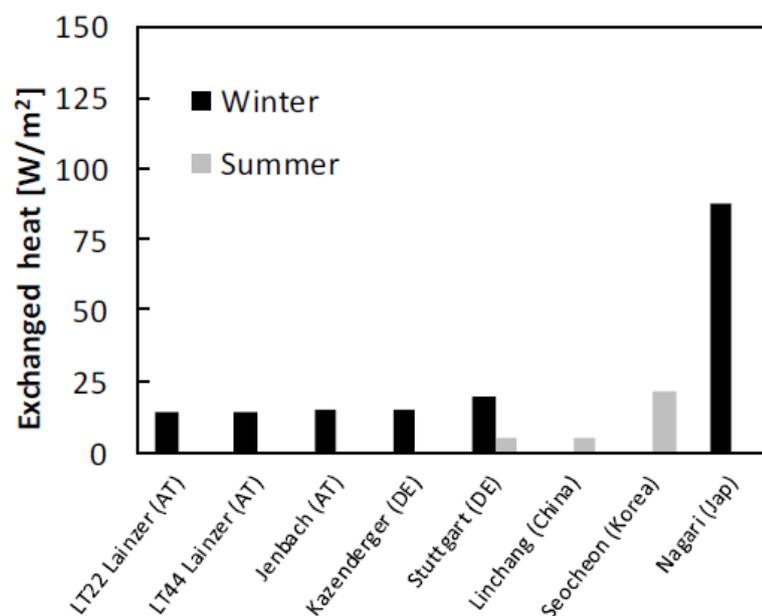


Figure 3.8 Heat exchange per square meter of wall in real energy tunnels. (Di Donna et al.,2017 )

### 3.4 Energy diaphragm walls

A diaphragm wall is a vertical structure, partially or entirely embedded in the ground, which function is to supporting the soil.

Generally, it is a prefabricated structure or cast in place, designed to support artificial temporary or definitive excavations, preventing the slipping of the soil inside the digging.

The diaphragm walls are generally made with alternating modules of 2.5 m, with thicknesses ranging from 0.4 m to 1.5 m. Beyond the excavation, the execution of the actual diaphragms covers, common steps, consisting of the setting of the reinforcement cages and the concrete casting. The reinforcement cages, generally preassembled to transportable modules with a maximum length of 12 m, consist of longitudinal irons, brackets and diagonal bracing bars. The completion of the diaphragms occurs with the construction of a head beam that connects the walls and has the function of

solidifying the various elements constituting the diaphragm and making them collaborating to share local actions.

For the realization of this type of structures, it is preferable to use the hydromill, and the implementation phases include:

- preparation of the area;
- pre-excavation activity (2 ÷ 3 m depth using a clamshell bucket and bentonite support);
- milling of alternate panels;
- lower the armature cage;
- concrete casting with bentonite recovery;
- head beam construction.

The phases just described are shown in figure 3.9.

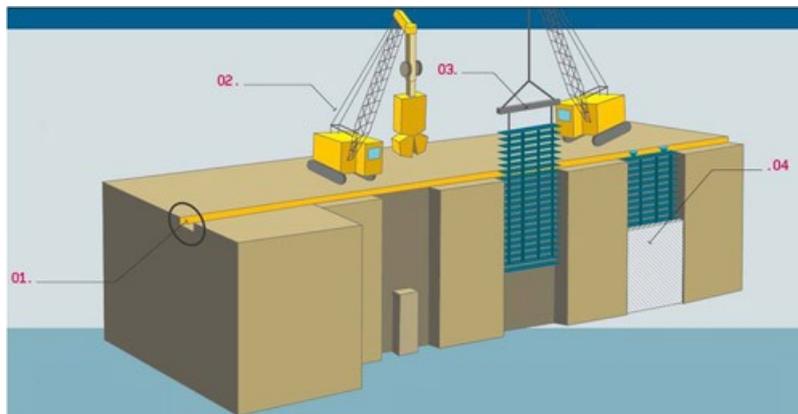


Figure 3.9 Construction phases of a diaphragm wall in reinforced concrete ([www.omranista.com](http://www.omranista.com))

The energy diaphragm walls, unlike conventional diaphragms, have bundles of polyethylene pipes necessary for the transport of the heat transfer fluid which is responsible for the heat exchange. Where geothermal loops are also incorporated in the wall, the loops are installed onto the cage as it is being lowered into position; the loops have to be secured to ensure the pipes are not snagged during the construction of the wall. In addition,

the free ends of the loop have to be protected until being exposed for connection when the head beam is constructed. The last step is to immerse the loops in the concrete to ensure good thermal contact. As a reminder, the effective area of the concrete wall is only marginally reduced by the introduction of geothermal loops and can be ignored in the capacity calculation (Amis, 2010).

The construction phases are a bit different in comparison to the ones described before, indeed they can be summed like following:

- quality control and pre-installation testing;
- lifting of the diaphragm armature cage;
- installation of the pipes;
- fixing the pipes to the cage as it is lowered;
- cutting of excess pipes and their protection;
- aptitude test of the pipes before casting concrete;
- casting (of the diaphragm) of concrete.



Figure 3.10 Inserting the geothermal pipes into the diaphragm cage (Amis et al., 2010)

Two important precautions must be kept in mind when the pipes are setting up. The first is that the pipes are not inserted inside the reinforcement cage in the prefabrication plant, as during the transport phases, they could be irreparably damaged, with difficulty of identification,

evidence of damage and consequently laying of pipes malfunctioning (Amis et al.,2010).

The second provides that, once the reinforcement cage has been installed correctly (also containing the heat exchanger tubes), the pipes are subjected to pressure to verify their integrity and ensure that there has been no damage during installation; the pressurization must be applied during the concrete casting phase of the panel and kept constant for the following day (Amis et al., 2010).



Figure 3.11 Coupling of the pipes to the cage (Amis et al.,2010)



Figure 3.12 Pressure testing geothermal loops once reinforcement cage installation (Amis et al.,2010)

At the end of the construction, the arrangement of coils on the entire surface of the bulkhead is noted: several exchangers are thus arranged along the diaphragm wall in the longitudinal direction (Figure 3.13). Generally, they are placed only along the surface in contact with the ground in conditions of low damping of the diaphragm and optionally, in case of further internal coatings, the exchanger pipes can also be arranged on both sides of the diaphragm.

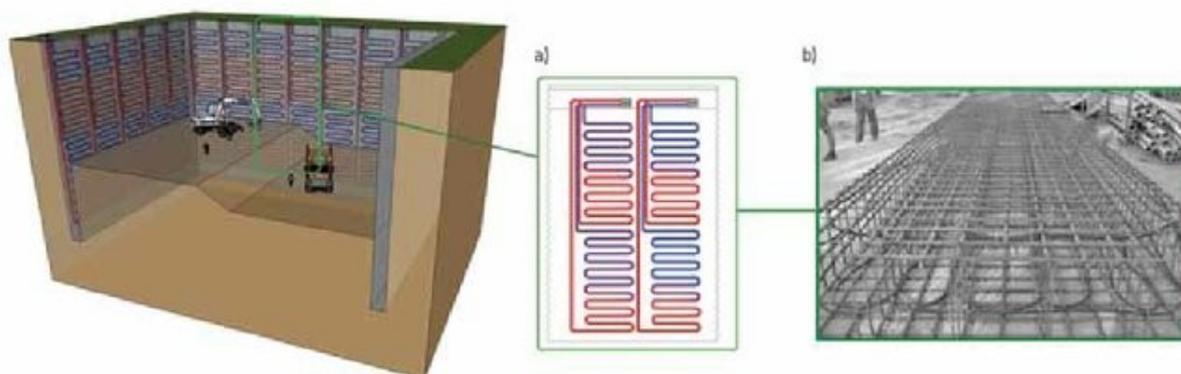


Figure 3.13 Energy DW scheme position (Kovacevic, Bačić, & Arapov, 2013)

In reference to the soil, Brandl (2006), through actualized projects in Austria, underlines the non-influence of the geothermal system to the surrounding ground in terms of shaft resistance, base pressure and bearing resistance. Moreover, the temperature induced settlement or heave is negligible.

On the other hand, the diaphragm walls, carrying out its function, is mainly subjected to lateral pressure of the ground, therefore the internal stresses to the section, from the side of the ground, are mainly traction, while they are of compression on the side of the excavation. Moreover, the flow of liquid inside the heat exchangers is always changing and in the project, the maximum and minimum temperature of the liquid must be set considering the possible evolutions. Once the heat exchanger tubes have been incorporated into the concrete, the fluid inside them transports the heat-carrying fluid with a variable temperature during the year and, due to the temperature difference between the fluid and the concrete, is thus generated a thermal stress around the tube. The temperature range induced inside the diaphragm wall is uniformly distributed around the tubes and the influence region is quite limited. Furthermore, in areas away from heat exchangers, the thermal stress in the structure is mainly caused by the

temperature of the surrounding soil; the value of over voltages will therefore be small and can be neglected, since it does not have a negative impact on the structure.

Following all these considerations, would be smart to evaluate the thermal influence in the structural analysis, as the thermo-mechanical effects on the DW should be investigated during the design and verification of the geotechnical work.

The application and research of heat exchanger buried in diaphragm wall are so far relatively rare. Only in 1996, absorber tubes were first embedded in diaphragm walls as heat exchanger in Austria and Switzerland (Brandl, 2006). For the first time, in 2003, in the sections of Viennese Metro Line Extension U2, absorber tubes were applied as heat exchanger in diaphragm wall, foundation floor and linings of sector tunnel, proving the power of the type of system.

Suckling and Smith (2002) described the first embedded energy wall in the UK at Keble College, Oxford, while Amis et al. (2010) dealt with the installation of the first energy diaphragm wall for the new Bvlgari Hotel in London. Farther, the new underground railway line in London has been equipped with geothermal technology in diaphragm walls (Amis and Loveridge, 2014).

Diaphragm walls formed as part of the construction for the new Shanghai Museum of Natural His-tory have been thermally-activated to provide heating and cooling to the museum in the new Shanghai Museum of Natural History (Xia et al., 2012). In Frankfurt, Germany, a bored pile type wall was installed in the construction of the Palais Quarter development (Katzenbach et al., 2017).

The efficiency of an energy diaphragm wall depends on many factors such as: the arrangement of the loops inside the cage, the spacing between two consecutive pipes, the concrete and soil thermal conductivity, the length of the bulkhead, the presence of groundwater flow, the velocity of the inlet fluid, boundary conditions and, obviously, the temperature difference between the soil and the inlet fluid of loops in the DW. Almost all these parameters were taken into account from different authors during the last years.

For example, Xia et al. (2012) analyzed the new technology on the *Shanghai Museum of Nature History* from the point of view of heat exchanger type, water velocity, inlet water temperature and operation mode.

First of all, three different types of underground heat exchangers were considered: W-shaped, improved W-shaped and single U-shaped (Figure 3.14). For each of them, three different inlet fluid temperatures were coupled to the sundry loops and the heat exchange rate per meter of tube is marked. Results showed an increasing of 20-40% of the heat rate for the type (a) and (b) over (c). Moreover, the type (b) demonstrated a better performance, roughly 10% more, over (a). Hence, for the W-shaped tubes in this experiment, by enlarging the distance of branch tubes near the soilward face, the heat transfer rate increased by 11%. Therefore, to enlarge the distance of branch tubes is an effective way to improve the heat transfer performance.

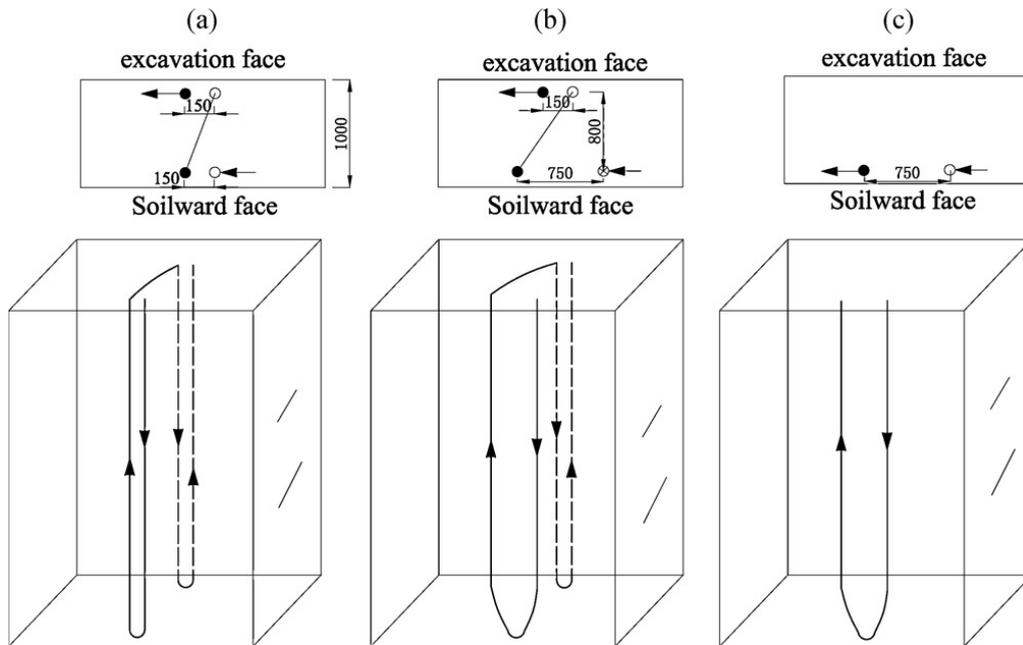


Figure 3.14 Types of underground heat exchangers: a) W-shaped type, b) improved W-shaped type, c) single U-shaped (Xia et al., 2012)

About internal water flow, the paper shows a rising of the heat exchange rate with the increasing of water velocity when it remains below  $0.9 \frac{m}{s}$  and changes slightly when it is larger than this value. In the design of heat exchanger in diaphragm wall, it is suggested to find a reasonable velocity pursue instead of an extensive high water velocity.

The last observation made by Xia et al. (2012), reported here, is about temperature: if the inlet water temperature increases  $1^{\circ}\text{C}$ , the heat transfer rate improves by 15%. This remark is valid for all different shaped pipes.

Bourne-Webb et al., (2016) demonstrated the non-conservative effect, with respect to heating capacity, of a simple constant temperature boundary condition at the wall-air void surface, although airflow in the excavation is faster than  $3$  to  $5 \frac{m}{s}$  as for instance in a tunnel.

The last work here mentioned, is the one of Di Donna et al. (2016) who was able to analyze the fundamental aspects that influence an energy

diaphragm wall: DW width, depth of excavation, spacing between two consecutive loops, concrete cover, inlet fluid velocity, excess temperature, concrete thermal conductivity. Furthermore, all the parameters were taken into account in four time frames: 3,5,30 and 60 days after the activation of the geothermal system. The geometry considered for the model analysis is reported in the figure below, jointly with the different spacings considered.

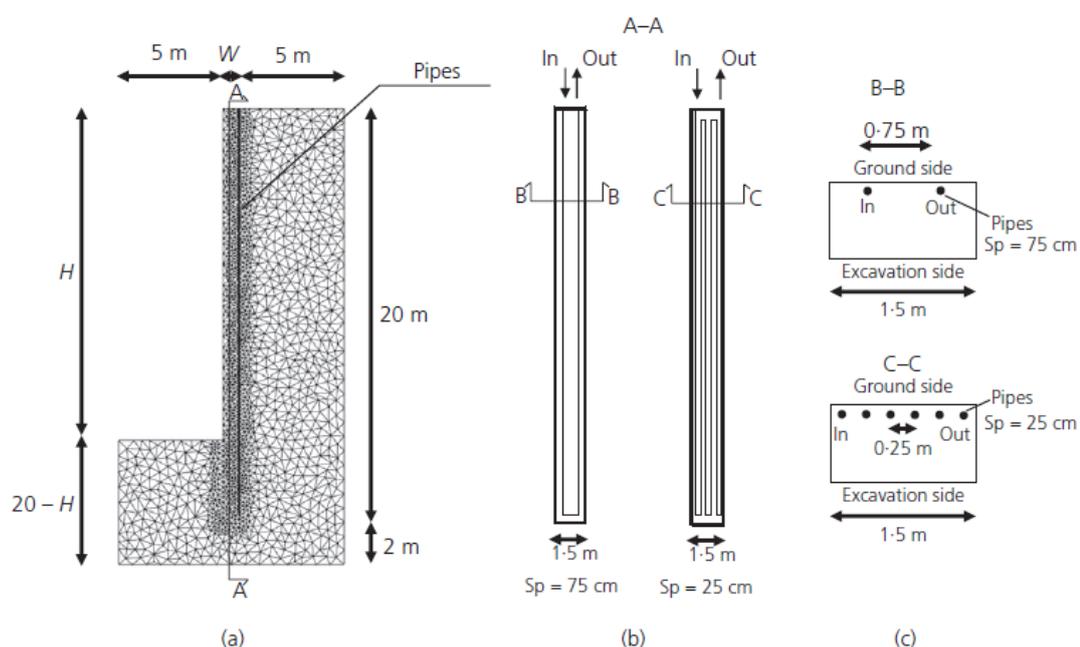


Figure 3.15 Geometry of parametric analysis: (a) vertical cut of the FE model, (b) vertical and (c) horizontal cut of the DW assuming upper and lower values of pipe spacing (Di Donna et al., 2016)

The coupled numerical simulation and statistical analysis led to state that the most important factor that improves significantly the energy efficiency is the pipe spacing reduced, i.e. increasing the number of pipes is the primary route to be considered in order to optimise the design. Nevertheless, this kind of influence goes into the background in a long-term prospective, where other factors take the lead. Indeed, the temperature excess between the wall and the excavation is the long-term parameter which governs the energy efficiency. This is consistent with the long-term

steady-state analysis proposed by Bourne-Webb et al. (2016) where the interface with the inside of the excavation governs heat transfer. Of course, the thermal conductivity is crucial too, i.e. the concrete mix should be the optimal one in terms of maximum thermal conductivity.

As it is shown in Figure 3.16, spacing and temperature excess are the most important one above the other factors. For this reason, Di Donna et al. (2016), suggests to equip both sides of the DW with pipes over the wall's full depth in order to increase energy efficiency. An optimal pipe spacing of 40 to 60 cm is suggested by ICConsulten (2005) ensuring a long-term pay-back periods and a balance between heating and cooling applications.

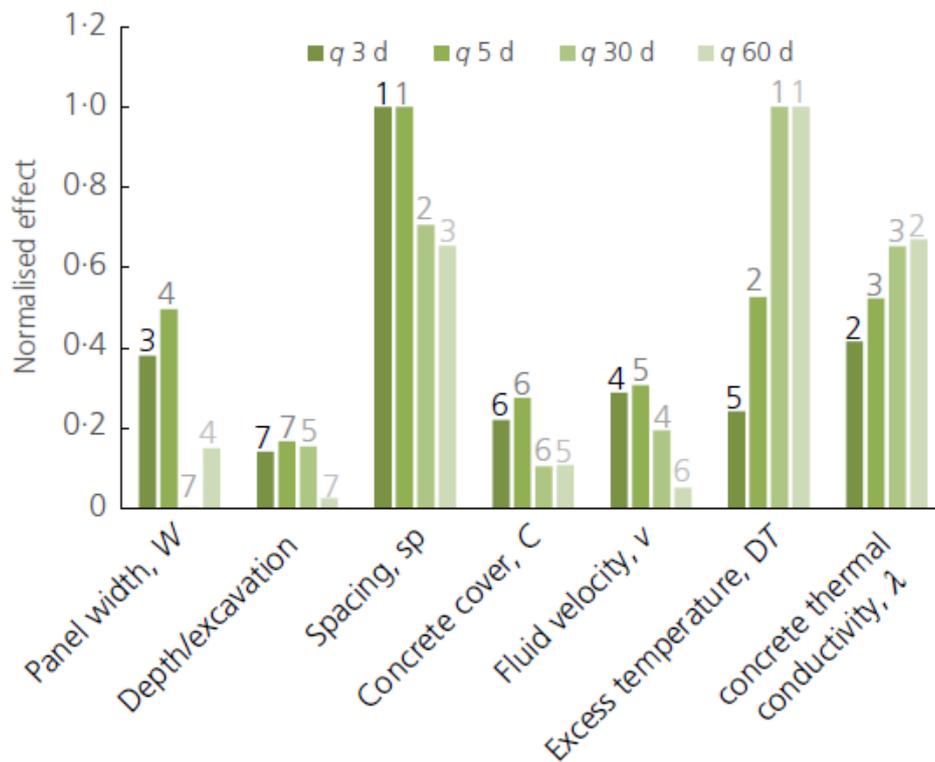


Figure 3.16 Normalised effect of each parameter in terms of heat exchanged (Di Donna et al., 2016)

The ensemble of this analysis, allows to not be too far in error assuming that the technology is mainly governed by the inlet temperature, the shape of the loops, the spacing and the excess temperature. Award of this, an efficient energy diaphragm wall can be design in order to exploit the shallow geothermal energy.

As done for tunnels, refer to real cases regarding the heat exchange is almost an obligation. In Figure 3.17 it is shown the efficiency, in term of heat exchange, of a several energy diaphragm walls present all around the world. Moreover, it can be seen that the heat exchange is generally in the range between 10 to 50 W/m<sup>2</sup>, with some exceptions, i.e. EA Center in Austria. It is anticipated that the differences might depend on the depth of the installation and on soil thermal and hydraulic properties and underground conditions, especially the presence of groundwater flow.

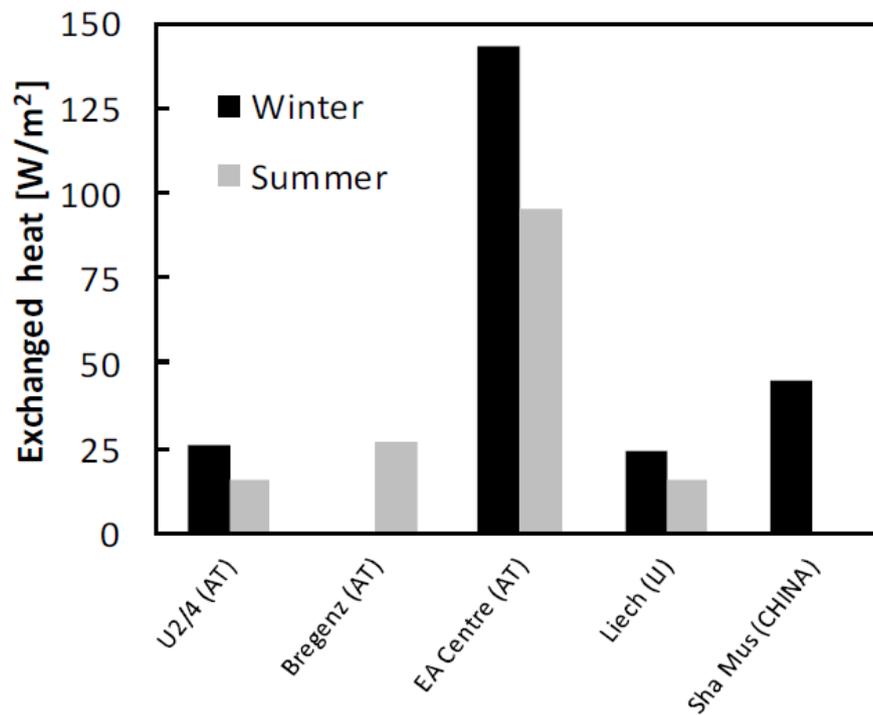


Figure 3.17 Heat exchange per square meter of wall in real energy walls. (Di Donna et al.,2017 )

Moreover, it is important to make thermo-mechanical observations and not just thermal capacity considerations. Indeed, although the energy capacity of these geostructures has only advantages, it is also necessary to analyze the mechanical variations induced by thermal variations and guarantee the stability of the structure. To achieve this goal, some studies have been conducted and will be reported here.

Based on the study of the section LT24 of the Lainzer Tunnel in Austria, P.J. Bourne-Webb et al. (2015) suggests that, after the end of construction, the next major alteration in the behaviour of the wall system is the thermal equilibration to the imposed ground surface and tunnel wall boundary conditions. Operation of the absorber pipes appears to make very little difference to the wall response. Furthermore, as shown in Figure 3.18, the effect of heating (or cooling) operations on the mechanical behaviour of the

wall system examined appears to be largely benign, with the major changes being attributable to climatic variations (ground and tunnel environments) that will occur anyway.

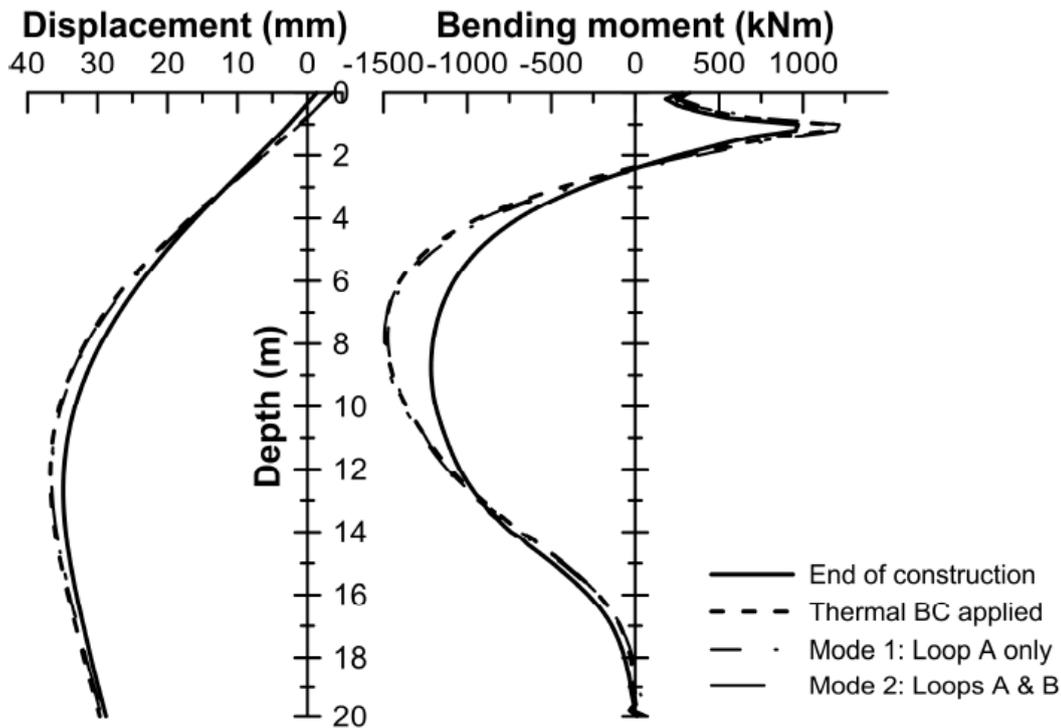


Figure 3.18 Wall response to heat injection with differing heating modes (P.J. Bourne-Webb et al., 2015)

Another interesting and complete study done concerning thermo-mechanical behaviour of an energy diaphragm wall is the one of Barla et al., (2018). Displacements and bending moment of a possible energy diaphragm wall in Turin was analysed. As Figures 3.19 and 3.20 show, thermal induced horizontal displacements are negligible, while the corresponding stress change rises up producing an increase of 17% of bending moment during winter. On the other hand, bending moment is minimum during summer, when the displacement is maximum. However, the stress variations computed in the analyses are largely below the strength limits of the structure.

Moreover, this is a clear (and rather obvious) indication that the mechanical effects of thermal loading on diaphragm wall are strictly function of the structural conditions. This implies that the proper construction sequence and structural behaviour need to be properly simulated in the numerical analysis to allow for reliable results to be obtained.

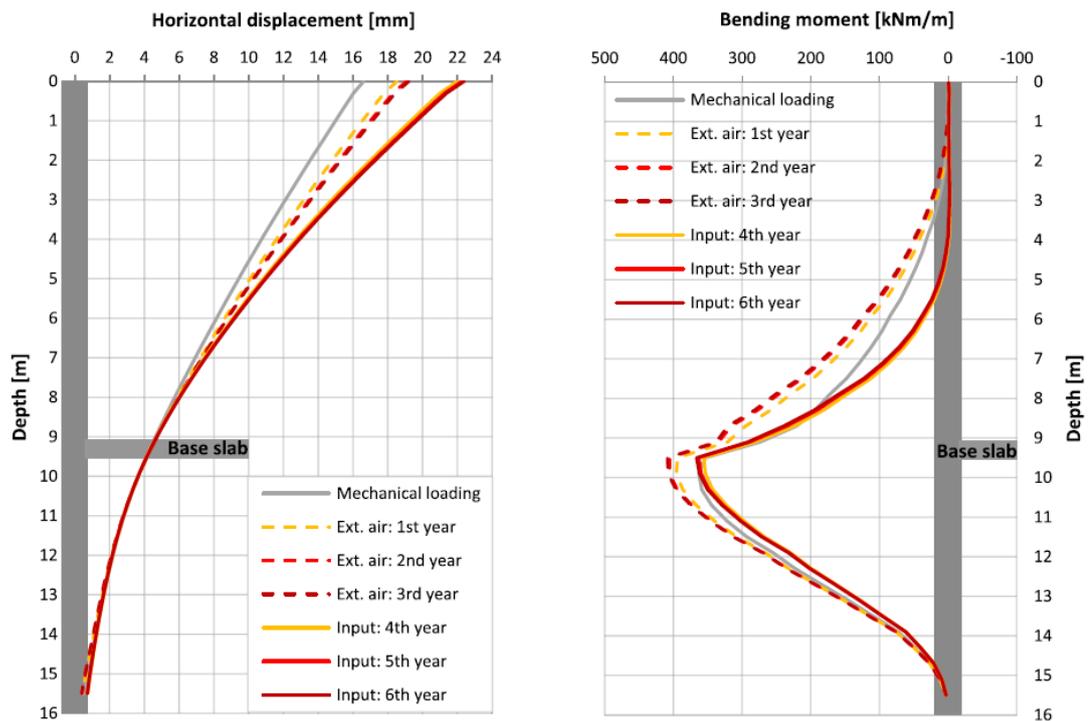


Figure 3.19 Bending moment and horizontal displacement change with: mechanical loading, external air and the activation of the geothermal system in Summer (August) (Barla et al., 2018)

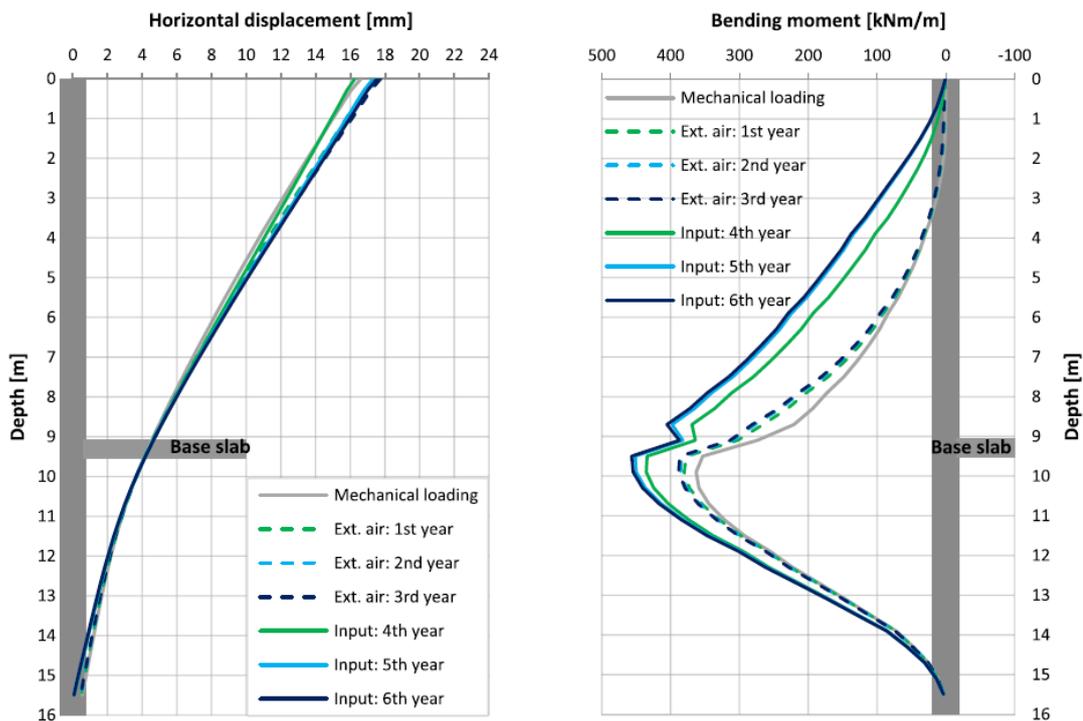


Figure 3.20 Bending moment and horizontal displacement change with: mechanical loading, external air and the activation of the geothermal system in Winter(February) (Barla et al., 2018)

### 3.5 How much does an energy structures cost?

One of the main problems that an engineer faces designing a structure is the amount of money needed for it. Indeed, generally speaking, the client wants to save as much as possible. For this reason, proposing an energy geostructure, at the beginning, doesn't seem convenient at all because of the additional costs of pipes and test needed. Nevertheless, the advantage of an energy geostructures is clear in a long-term view.

Barla et al. (2016) reported an interesting comparison, in terms of costs, between different kinds of heating-cooling geothermal plants used in tunnels. Specifically, it is remarked that traditional heating-cooling systems present an annual operating costs about 75-145% higher than the geothermal one. The great advantage is achieved with an additional initial

cost, in this analysed case, for tunnel thermal activation of 0.78% of the total cost of the tunnel construction project total costs. In addition, the pay-back time for the additional cost is maximum 5 years. Figure 3.21 shows the cost saving if a geothermal system is favoured over other choices, e.g. gas, LPG, oil and pellet.

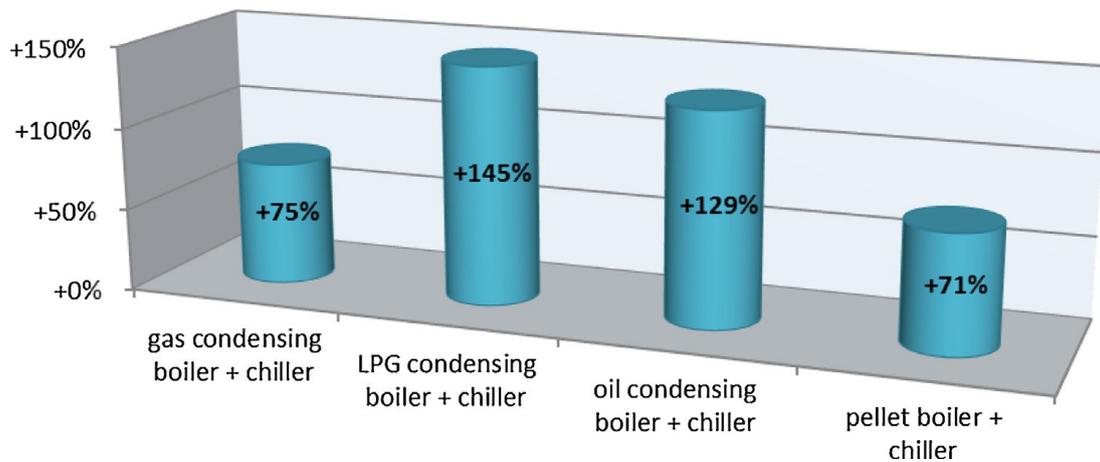


Figure 3.21 Annual operating cost savings with respect to other heating/cooling system (Barla et al., 2016)

Another observation was made by Barla et al. (2016) about open and closed loop system. Considering a borehole heat exchangers (BHE), an open loop method is more economically convenient with respect to the energy tunnel system. However the energy tunnel is a closed loop system and will avoid direct influence on the groundwater, reducing the concurrent environmental problems.

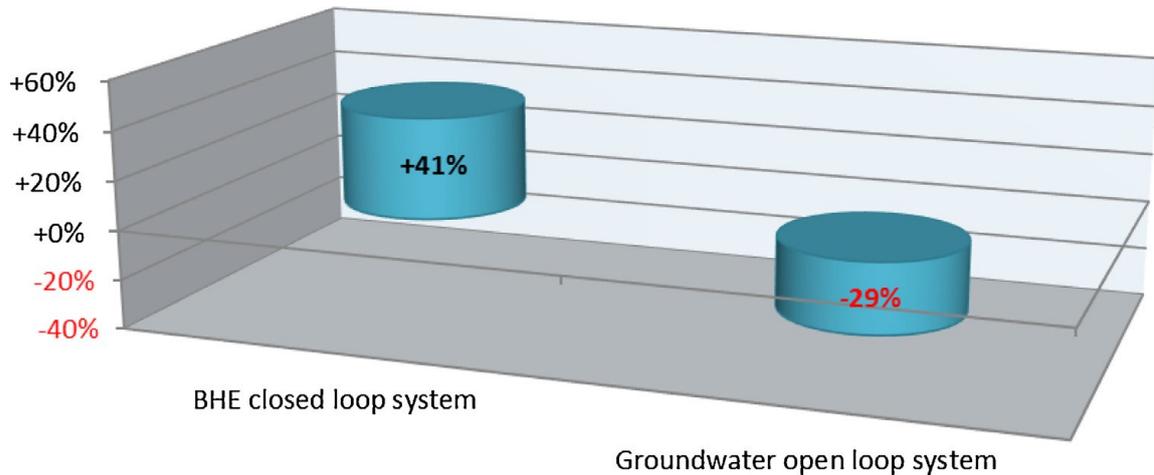


Figure 3.22 Economic convenience with respect to the other geothermal exchangers (Barla, Di Donna, & Perino, 2016)

For doing a practical example, if a tunnel about 1 km long, from the project to the final realization, may cost around 400'000/500'000 €, the addition of a geothermal system; i.e. pipes (included labour and test) will add around 1% at the sum, in this case 5'000 € more. This amount of money can seem a lot taken apart, but, for a work like a tunnel, it can be considered negligible especially considering the long-term benefits which are derived from the new technology. In addition, if it is taken into account that a tunnel has a nominal life of operation of roughly 100 years, such as the polyethylene pipes used for the geothermal implant, and that a geothermal system needs 5 years to reach the expected pay-back, it points out that the proposed system guarantees success in many ways, from being environmental-friendly to be a cost-effective solution.

## **4. Numerical modeling for thermo-hydro- mechanical analysis**

### **4.1 Coupled Thermo-hydro-mechanical problem**

Energy geostructures need specific analysis, different from the one taken into account for standard structures, because of their complexity. Indeed, a numerical modeling of coupled thermo-hydro-mechanical analysis is required in order to predict the distribution of stresses, strains, displacements and interstitial pressure around the construction.

For an energy geostructure, the problem is presented by elements in reinforced concrete, such as bulkheads, piles, foundation slab, subjected to a mechanical component of stress given by the load and able to exchange heat with the surrounding environment. Both the soil and the concrete are considered porous materials composed mainly of a solid and fluid phase; in our study, the whole material is considered to be saturated with water. The three aspects, thermo-hydro-mechanical, are coupled since the variations of the solid volume are influenced by the presence of temperature gradient, the heat exchanged depends on the presence of water flow, the density of the water varies with the heat load and the mechanical response of the materials depends both on the interstitial pressure of the fluid (concept of

effective tensions) and on the variation in temperature. Consequently, a correct formulation of the complete Thermo-Hydro-Mechanical coupling (THM) is necessary in order to analyze the problem. Thus, it is usual, based on investigations needs, to take into account only a partial analysis. Indeed, this thesis will study only the thermo-mechanical behavior of the diaphragm wall. However, in order to give a general overview of the problem, all the equations that governs a THM analysis will be introduced, bearing in mind that the knowledge of these equations offers the opportunity to do all the analysis desired.

#### 4.1.1 Governing equations

The analysis carried out for this thesis is based on the hypothesis of an elastic behaviour, thus it is necessary introduce a set of equations and boundary conditions dictated by THM problem.

- Mechanical field:
  - Equilibrium equations
  - Congruence equations
  - Constitutive laws
- Hydraulic field
  - Mass conservation equation
  - Darcy's laws
- Thermal field
  - Energy conservation equation
- Boundary conditions

#### *Equilibrium equations*

Timoshenko and Goodier (1951) equations must be satisfied by the soil:

$$\text{div}(\sigma_{ij}) + \rho g_i = 0 \quad (4.1)$$

Where the *div* operator is the divergence,  $\sigma_{ij}$  is the tensor of the total stresses,  $\vec{g}_i$  the gravity vector and  $\rho$  the density of the material, which includes the density of the water  $\rho_w$  and the solid particles  $\rho_s$ . Through the porosity  $n$ , we can define:

$$\rho = n\rho_w + (1 - n)\rho_s \quad (4.2)$$

The definition of effective stress allows to consider the hydraulic component, thus the hydro-mechanical coupling is introduced and the equation is transformed as:

$$\text{div}(\sigma'_{ij}) + \nabla p_w + \rho g_i = 0 \quad (4.3)$$

$\nabla$  is the gradient,  $p_w$  the pore water pressure and  $\sigma'_{ij}$  the effective stress tensor that can be written in incremental form by introducing the constitutive law.

### ***Compatibility equations***

It has been assumed the theory of small deformations and a convention of positive sign for the compression. As know, the deformations  $\varepsilon$  can be written in terms of displacements  $u$  along  $x$  axis, displacement  $v$  along  $y$  axis and displacement  $w$  along  $z$  axis:

$$\begin{aligned} \varepsilon_x &= \frac{\partial u}{\partial x} & \varepsilon_y &= \frac{\partial v}{\partial y} & \varepsilon_z &= \frac{\partial w}{\partial z} \\ \gamma_{xy} &= \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} & \gamma_{yz} &= \frac{\partial v}{\partial z} + \frac{\partial w}{\partial y} & \gamma_{xz} &= \frac{\partial w}{\partial x} + \frac{\partial u}{\partial z} \end{aligned} \quad (4.4)$$

Since deformations are a function of only three displacements, these are not independent. Mathematically it can be demonstrated that for the existence of a compatible displacement field, all the above mentioned deformation components and their derivatives must exist and be continuous for at least

the second order. The displacement field must satisfy any displacement or condition imposed on the contour.

In these equations all terms are related to the mechanical part of the coupled system THM.

### *Constitutive laws*

In order to obtain a solution for the system, other equations must be introduced: constitutive laws relate stresses to strains. For an elastic material, they are:

$$\begin{aligned}
 \sigma_x &= \frac{E[(1-\nu)\varepsilon_x + \nu\varepsilon_y + \nu\varepsilon_z]}{(1+\nu)(1-2\nu)} \\
 \sigma_y &= \frac{E[(1-\nu)\varepsilon_y + \nu\varepsilon_x + \nu\varepsilon_z]}{(1+\nu)(1-2\nu)} \\
 \sigma_z &= \frac{E[(1-\nu)\varepsilon_z + \nu\varepsilon_x + \nu\varepsilon_y]}{(1+\nu)(1-2\nu)} \\
 \tau_{xy} &= G\gamma_{xy} \quad \tau_{yz} = G\gamma_{yz} \quad \tau_{zx} = G\gamma_{zx}
 \end{aligned} \tag{4.5}$$

Where, for homogeneous, linear, isotropic, elastic materials, E is Young's modulus,  $\nu$  is the Poisson coefficient, while G is the Lamè constant (shear modulus) which is linked to E and  $\nu$  through the formulation:

$$G = \frac{E}{2(1+\nu)} \tag{4.6}$$

In order to consider the thermal coupled effects, the vector form is introduced:

$$d\sigma'_{ij} = C_{ijkl}(d\varepsilon_{kl} + d\varepsilon^T_{kl}) \tag{4.7}$$

Where  $C_{ijkl}$  is the stiffness matrix composed by 36 elements, which can be written in function of only  $E$  and  $\nu$  in case of isotropic, linear, elastic material:

$$C_{ijkl} = \frac{E(1-\nu)}{(1+\nu)(1-2\nu)} \begin{bmatrix} 1 & \frac{\nu}{1-\nu} & \frac{\nu}{1-\nu} & 0 & 0 & 0 \\ \frac{\nu}{1-\nu} & 1 & \frac{\nu}{1-\nu} & 0 & 0 & 0 \\ \frac{\nu}{1-\nu} & \frac{\nu}{1-\nu} & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1-2\nu}{2(1-\nu)} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{1-2\nu}{2(1-\nu)} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1-2\nu}{2(1-\nu)} \end{bmatrix} \quad (4.8)$$

Thermal deformation is defined as:

$$d\varepsilon_{kl}^T = \beta_{kl} dT \quad (4.9)$$

Where  $\beta$  is the linear coefficient of thermal expansion [ $^{\circ}\text{C}^{-1}$ ] and  $dT$  is the temperature increment.

### *Mass conservation equation*

The principle of conservation of mass postulates that the mass of fluid  $M$  does not change with the motion of an arbitrary volume  $V$ , i.e. that the material derivative of  $M$  over time is always identically equal to zero. The mass conservation equation was obtained using some theorems of fluid mechanics and using Darcy's law. The latter describes the motion of a fluid within a porous material and it is expressed as:

$$\vec{v} = -K\vec{\nabla}h \quad (4.10)$$

$v$  is the velocity,  $k$  the permeability of the soil and  $\vec{\nabla}h$  the hydraulic load.

The mass conservation equation in transitory conditions can be mathematically described by Poisson's equations:

$$K \left( \frac{\partial^2 h}{\partial x^2} + \frac{\partial^2 h}{\partial y^2} + \frac{\partial^2 h}{\partial z^2} \right) = \frac{\partial \varepsilon_v}{\partial t} \quad (4.11)$$

$\varepsilon_v$  is the volumetric deformations.

If the conditions of stationary regime exist, the volume does not change over time and the previous equation is reduced to that of Laplace:

$$\left( \frac{\partial^2 h}{\partial x^2} + \frac{\partial^2 h}{\partial y^2} + \frac{\partial^2 h}{\partial z^2} \right) = 0 \quad (4.12)$$

The latter one describes a decoupled problem, since there are no mutual influences between the mechanical problem and the hydraulic one, therefore the field of interstitial pressure can be determined independently from the solution of the mechanical problem. In vector form, the Poisson equation becomes:

$$\begin{aligned} \operatorname{div}(K \vec{\nabla} h) &= \frac{\partial \varepsilon_v^M}{\partial t} && \leftrightarrow && (4.13) \\ K \vec{\nabla}^2 h &= \frac{\partial \varepsilon_v^M}{\partial t} \end{aligned}$$

Where the Laplacian operator  $\vec{\nabla}^2$  is defined as divergence of the gradient.

Adding the thermal rate, the final equation is:

$$K \vec{\nabla}^2 h = \frac{\partial \varepsilon_v^M}{\partial t} + \frac{\partial \varepsilon_v^T}{\partial t} \quad (4.14)$$

Where the thermal deformation is defined as:

$$\varepsilon_v^T = 3\beta \Delta T \quad (4.15)$$

The equation number (3.14) presents the hydraulic contribution to the first member, while the components of the mechanical and thermal field are at the second one.

### *Energy conservation equation*

It is possible to do an energy balance between the temperature  $T$  and the heat flow  $q$ , as it was already done for the mass and the water flow.

Firstly, it is necessary to introduce some concepts about heat transmission. The latter, is guaranteed by a difference of temperature between two interactive systems, in accordance with the principle of energy conservation.

Experience has shown that the heat transmission is a complex phenomenon which involves many material properties where the transmission takes place. However, there are three different ways or better mechanisms of transmission, described in the following.

*Conduction* is an energy transporting way which is proper of solid or liquid phase in a porous material, no fluid's macroscopic movement is required. Fourier's law governs this mechanism where the transfer of kinetic energy takes place from high temperature zones to the adjacent low ones, and the heat transfer  $[\frac{W}{m^2}]$  expressed as:

$$q_{cond} = -\lambda \vec{\nabla} T \quad (4.16)$$

Where  $\lambda$  is the thermal conductivity of the material  $[\frac{W}{mK}]$  and  $\vec{\nabla} T$  is the temperature gradient. The sign “-” is related to the way of decreasing temperatures (Bonacina et al., 1980).

*Convection* happens through a fluid in movement, hypothesis of saturated material was made, always with different temperature; the transfer energy with macroscopic transportation is equal to:

$$q_{conv} = c_w \rho_w \vec{v}_w \Delta T \quad (4.17)$$

Where  $c_w$  is the specific heat of water [ $\frac{J}{kgK}$ ] and  $\Delta T$  is the difference of temperature between the two systems.

Clearly, this rate can be taken into account only if there is a fluid flow. In a soil, for example, convection gives an important contribution in incoherent soils, i.e. sand and gravel, on the other hand is negligible for cohesive soils, i.e. clays.

*Radiation* is the mechanism of transfer between two surfaces with different temperatures. In this context it is not relevant, indeed its contribute is minor than 1% for sand and even less for clays (Ree et al.,2000). For this reason, it will not be taken into account in our analysis.

The equation of conservation of energy under steady-state conditions in the case of only conduction is provided by the Laplace equation:

$$\vec{\nabla}^2 T = 0 \quad (4.18)$$

On the other hand, in the case of transitory conditions, always only by conduction, the mass conservation equation can be described mathematically by the Poisson equation:

$$\lambda \vec{\nabla}^2 T = \rho c \frac{\partial T}{\partial t} \quad (4.19)$$

The second member is the accumulation of heat and it is formed from:

$$\rho c = n \rho_w c_w + (1 - n) \rho_s c_s \quad (4.19)$$

That is the specific heat of the soil in which water specific heat  $c_w$  and solid skeleton one  $c_s$  are included;

Conduction and convection can be blended together and, in the case of transitory conditions, the final equation would be:

$$\lambda \vec{\nabla}^2 T + \text{div}(\rho_w c_w \vec{v}_w \vec{\nabla} T) - \rho c \frac{\partial T}{\partial t} = 0 \quad (4.20)$$

### ***Boundary conditions***

It is known that, to solve a problem, boundary conditions are necessary firstly to reproduce a real condition, e.g. symmetry, secondly to reduce the unknowns, i.e. to be sure to have a determined system. A THM problem can involve a large number of variables between fields and material properties coupled between them. Thus, doing an associated analysis, requires a heavy computation but it may be unnecessary from an engineering point of view. For this reason, it is fundamental to understand which field, mechanical, thermal or hydraulic, is more important in our analysis in order to create an appropriate model and reduce costs.

Generally speaking, boundary conditions are referred to:

- Forces and/or displacements for the mechanical field;
- Hydraulic conditions for the hydraulic field;
- Temperature for the thermal field.

## **4.2 Numerical modeling and FE method**

The numerical modelling is born with the purpose to create virtual models of physical reality to approximate the behaviour and be able to perform analyses in order to predict the in situ behaviour of the system response to a specific action. This tool is very powerful, as it allows to solve increasingly complex problems from the geometric, the constitutive behaviour and the stresses point of view, succeeding in involving fields of application that are increasingly broader and more competitive. Nevertheless, it is just a tool that a good engineer must use wisely and interpret the results critically.

In the field of geotechnical engineering a problem can be studied in three different ways: continuous, equivalent-continuous or discontinuous. The latter, is used when discontinuities govern the stress-strain behaviour. Whilst, the continuous model is valid when the presence of macrostructures is negligible in order of global behaviour. On the other hand, an equivalent-continuous takes into account the global characteristics, thus it is common to scale the properties of intact rock to the rock mass using empirical formulations.

Based on the approach chosen, a numerical method is associated:

- Continuous method: finite element (FEM), finite difference (FDM), boundary element (BEM);
- Discontinuous method: distinct element (DEM);
- Equivalent-continuous method: finite discrete element (FDEM).

*Boundary element method* (BEM) uses a constitutive model only for elements on the contour, whereas, differential displacements between elements are allowed in *Distinct element method* (DEM). On the other hand, Finite discrete element method (FDEM) guaranties differential displacements between two elements with the discretization to finite elements inside of them.

Actually, the most common methods used are FEM and FDM. The latter, is perhaps the oldest numerical technique for the solution of boundary problems. In the FDM every derivative in the set of governing equations is replaced directly by an algebraic expression written in terms of the field variables (e.g. stress or displacement) at discrete points in space; these variables are undefined within elements. In contrast, the FEM has a central requirement that the field quantities vary throughout each element in a prescribed fashion, using specific functions controlled by parameters. Both

FDM and FEM methods produce a set of algebraic equations to solve. The FE programs often combine the element matrices into a large global stiffness matrix, whereas this is not normally done with finite differences because it is relatively efficient to regenerate the finite difference equations at each step.

The FE method used in this thesis can be easily described through 6 steps:

1. Element discretization: modelling the geometry of the problem by assemblage of finite elements;
2. Primary variable approximation: a primary variable must be selected as well as how it should vary over a FE. In geotechnical engineering it is usual to adopt displacements as the primary variable;
3. Element equations: use of an appropriate variation principle to derive element equations;
4. Global equations: combine element equations to form global equations;
5. Boundary conditions: formulate boundary conditions and modify global equations;
6. Solve the global equations: to obtain the displacements at all the nodes, from which secondary quantities such as stresses and strain are evaluated.

The fundamental step is the construction of the mesh. First of all, the geometry of the boundary value problem must be approximated as accurately as possible and the discretization process need be performed carefully. Moreover, a denser mesh, i.e. high number of elements, in relation to the type of element adopted (triangular or rectangular) should be used where higher stress gradients are expected, e.g. near holes, in

corner zones. If non homogeneous zones occur, it is essential that nodes are located along the contours from one zone to the other one. Whereas, the dimensions of the mesh should be chosen big as much as to avoid influences from boundary restraints. The shape chosen for the element is important too. Indeed, if the behaviour of a structure such as a diaphragm or a pile, wants to be performed, a rectangular mesh should be selected, otherwise a triangular shape is the best choice, e.g. to model soil or a tunnel.

Contrary to the FDM, which sees the domain to be analysed as a series of points in a grid, the FEM sees dominance as the union of many subdomains of elementary form.

In the FEM, the differential equations are unchanged (relative to each finite element) while the domain comes discretized. In a continuous problem of any dimension, the field variable, such as pressure, displacement, temperature, velocity or density, it is a function of each generic point of the definition domain. As a result, the problem presents an infinite number of unknowns. The finite element discretization procedure reduces it to a problem with a finite number of unknowns, by dividing the domain into finite elements and expressing the unknown field in terms of approximate functions, defined within each element. The term finite elements was used in a 1960 Clough article where the method it was presented for the solution of a state tension plan. The term derives from the fact that the integration domain comes divided into a determined number subdomain, within which the differential equations governing the problem are solved through the approximate functions.

The latter, also called shape functions, are identified through the values that the dependent variable has in a specific points called nodes. The nodes are usually placed on the outline of the elements, in points common to two or

more elements. In addition to the boundary nodes, an element can have nodes inside it. Values that vary on the of field assumed on the nodes, they unequivocally define the trend within the element. In the representation to the finite elements of a problem, the nodal values of the field variable represent the new unknowns.

As mentioned, the discretization of the domain then leads to the generation of nodes and finite elements. The nodes, in the applications of the FEM, are extremely important entities because the solution of the whole structure is referred to them: in order to extend the values of the field of unknowns on the whole body, some functions are used that with the desired approximation report the nodal values in each subdomain. It is evident that as the number of nodes increases, increases the degree of the polynomial used for interpolation of data at the nodes and, therefore, also increases the quality of the approximation. The choice of shape functions, which are generally polynomial (or at least to known behaviour) is another fundamental point that allows to obtain a solution of the FEM model more or less close to the desired reality. In order to correctly represent the value at the nodes, the shape functions must assume unit values in the considered node and null values on the rest of the nodes. The field of unknowns for a three-dimensional problem can be represented by the following general report:

$$[u(x, y, z)] = [H(x, y, z)][u]_e \quad (4.22)$$

Where  $[H(x,y,z)]$  is the element shape function which interpolates the solution between the discrete values obtained at the mesh nodes.

As said earlier, displacements are the primary variable favourite in geotechnical field. Stress and strain are treated as secondary quantities

which can be derived from the displacements. Thus, the main approximation in the FEM, is to assume a particular form for the way the primary variable varies over the domain under study. Clearly, this assumed variation must satisfy the conditions of compatibility.

The solving equations can be written in explicit or implicit form. FDM often use an explicit, time marching method to solve the algebraic equations, while implicit, matrix-oriented solution schemes are more common in FEM.

The explicit approach uses a time-dependent differential equation that considers other parameter beyond that mass, displacements and applied load:

$$[m][\ddot{u}] + [c][\dot{u}] + [k][u] = [F] \quad (4.23)$$

$m$  is the mass of the system,  $c$  is the damping,  $k$  is the stiffness and  $u$  the displacement with its temporal variables.

On the other hand, implicit form is favoured by the FE method. In this case, the displacements are not dependent by time, i.e. acceleration and velocity are equal to zero and the damping and mass matrices can be neglected. Indeed, in order to solve the equation, it is necessary to invert the global stiffness matrix  $[k]$ , thus the computational burden can be really high:

$$[K][u] = [R] \quad (4.24)$$

Indeed, the main effort for the software is to assemble the entire element's stiffness matrix into the global one and then invert it, multiplied by matrix force, to obtain the displacement desired. Moreover, the global stiffness matrix is equal to:

$$[K] = \sum_e \int [B]_e^T [C]_e [B]_e dV_e \quad (4.25)$$

Where  $[B]$  contains only derivatives of the shape function and  $[C]$  is the elastic matrix.

Lastly, in equation (4.24), the  $[R]$  is the vector of the forces at the nodes and it is a sum of all the forces possibly present in a system.

The use of the FEM is established as one of the best tools for the investigation those complex problems, for which investigations and experiments in the laboratory would involve excessive expenses, logistical difficulties and difficulties related to the physical measurement of the various quantities. If the first automatic approaches to the solution of the differential equations that governing physical phenomena, are affirmed with finite differences, the FEM evolves the possibilities of solution by giving one possibility of application that has no equal, thanks to its incontrovertible flexibility. The generality of the method, initially developed by engineers and subsequently demonstrated also by mathematicians, it has allowed many studies and applications, paving the way for new lines of research that currently address notional issues the interest of a theoretical and practical nature.

### **4.3 Calculation software**

In this thesis the LAGAMINE software was used to compute the Thermo-Mechanical analyses. The introduction and explanation of the FEM, allows to understand how the calculation program works. As a matter of fact, LAGAMINE is a finite element code developed by the department MSM of University of Liege since 1982 (Charlie R., 1987, Collin F., 2003). It is a solid, nonlinear, great deformations code that has been adapted to numerous finite elements and constitutive laws. The code has been developed along with innovations and science for the last forty years. The continuous work

of researchers around the world, in university as well as in the industry, has maintained it at the leading edge of technology and research. More specifically, LAGAMINE is able to deal with complex nonlinear constitutive models, multiphysical coupling, strain localization and multiscale approaches for applications in the fields of environmental geotechnics, engineering geology, reservoir engineering and metal forming (“2nd International Workshop on the Finite Element Code LAGAMINE,” 2018).

The program is presented as shown in the figure 4.1 and the interface is user-friendly as well as funny because of the cartoon-shaped buttons. Nevertheless, do not be fooled by the appearance because the software is able to solve really complex problems, such as a THM analysis with the option 2D or 3D without too many difficulties.

As most calculation programs, it is necessary to pay attention to what is asked and how it is done, indeed, due to the fact that the program reads text files, spaces and numbers are fundamental.

The steps to follow are exactly the same of all those necessary in a numerical model:

1. Discretizing the model with the creating of a finite element mesh;
2. Define boundary conditions;
3. Assign material properties to the elements;
4. Assign the initial stress state to the nodes;
5. Define computational stages, in order to reproduce construction sequence;
6. Compute;
7. Interpret the results.

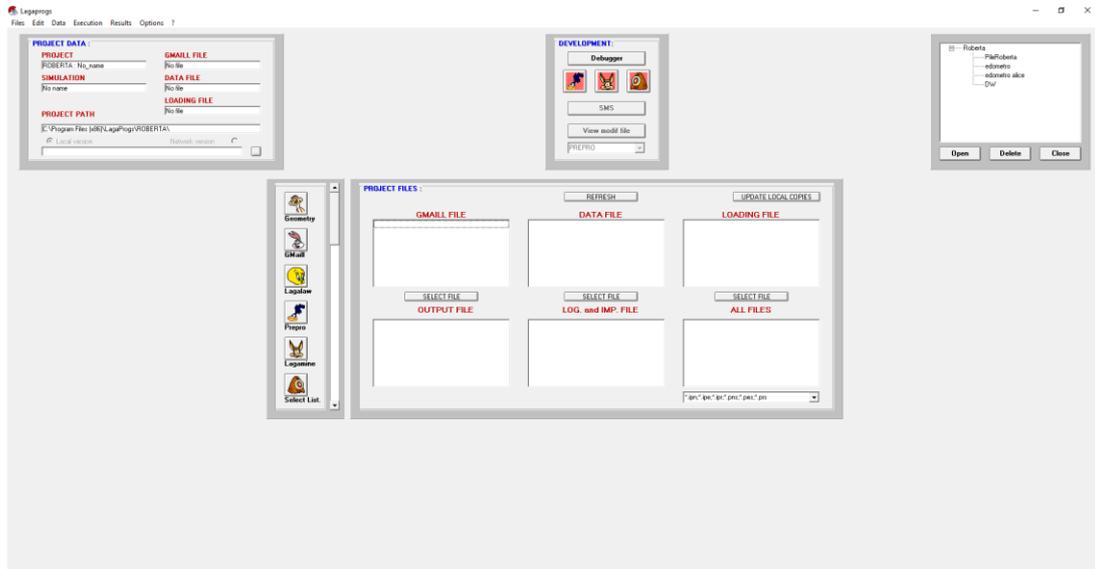


Figure 4.1 LAGAMINE's interface

The first step required by the software is the definition of the geometry, understood as domain, segment division, type of mesh and boundaries, e.g. fixed points, foundation, structured mesh or internal contour. All these information are saved in the “GMAIL file”.

After choosing the type of analysis, the material properties and initial stress state assignment is the next step doable through the *Lagalaw* button. Mechanical, thermal, flow and coupled laws are available, around 444 choices, on the base of the kind of elements, 66 choices, selected for the geometry. All these selections are drafted in “DATA file” which is the complete one, i.e. it contains the whole information of the defined model from the node's coordinates to the list of different elements chosen. The *Prepro* button let the program checks the *DATA file*, if everything is appropriate for LAGAMINE, it is possible to proceed with the “LOADING file”. Here the type of load, the first increment, the number of steps and strategy parameters are defined. *Lagamine* runs applying the *LOADING file* to the *DATA file* and then results are proposed.

A useful capacity is to print the results in terms of tensions and deformations, for examples, of only the elements and nodes required. Moreover, it is possible to “turn of” some elements, e.g. to simulate the stage of an excavation, all this always through a text file.

#### **4.4 Software validation**

In order to understand how the program works, it was decided to run a simulation of a loading step if an oedometric test for 3 different problems: mechanical, hydro-mechanical and thermo-hydro-mechanical. Due to the fact that LAGAMINE uses text file, i.e. can be really complex to understand it at the beginning, the considered choice was made of starting from a simple analysis and then arriving at the more complex one of interest for the thesis. Thus, the following subchapters will describe the preliminary analysis made for an oedometric test of a sample of sand, high 2 cm with a radius of 3 cm and subject to a uniform vertical load of 1 MPa (Figure 4.2). Each side was divided into 10 segments so a mesh of 10x10 and 8-nodes quadrangular element was created and axysimetry problem is considered, i.e. the left side is the axis of symmetry. An elastic law was chosen to make easier the comparison between the results given by LAGAMINE and hand-made one, to validate the software; properties are reported in table 1. Clearly, to simulate the behaviour of an oedometer, rollers were set as lateral and bottom boundaries. In this way, the lateral deformation of the soil is prevented, i.e. only vertical variations are allowed.

Table 1 Mechanical-fluid-thermal properties of oedometer sample

Parameter	Symbol	Unit	Value
Young modulus	$E_d$	[MPa]	215
Poisson coefficient	$\nu$	[-]	0.3
Specific weight	$\gamma$	[kN/m <sup>3</sup> ]	19.5
Thermal conductivity	$\Lambda_s$	$Wm^{-1}K^{-1}$	2.8
Specific heat coefficient	$\rho_s$	$Jkg^{-1}K^{-1}$	1053
Coefficient of linear thermal expansion	$c_s$	[-]	$10^{-5}$
Intrinsic permeability	$k_p$	[m <sup>2</sup> ]	$3.78 \cdot 10^{-10}$
Porosity	$N$	[-]	0.4

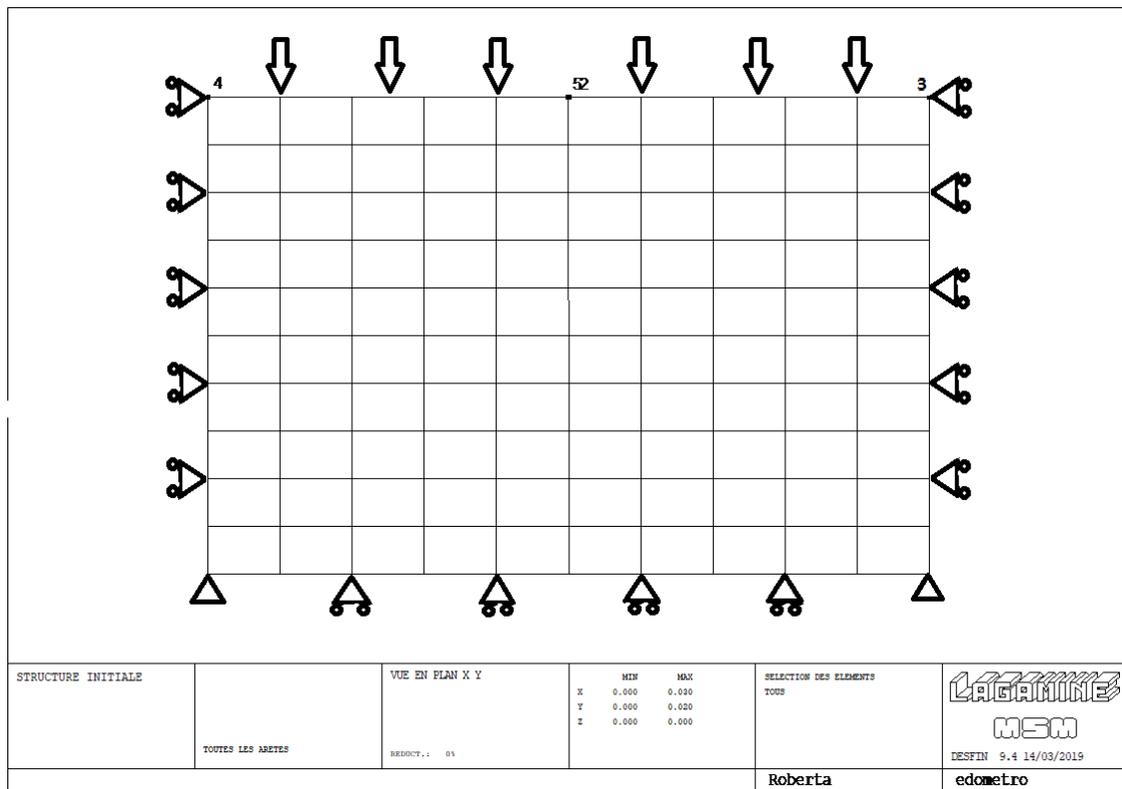


Figure 4.2 Initial structure with boundary conditions and load

#### 4.4.1 Oedometer: mechanical problem

The first preliminary analysis is the mechanical one, means that temperature and water pressure are blocked. Thus, the load is applied through a manual strategy which divided the 1 MPa force in 10 steps each of 0.1 MPa and the loading-time is chosen equal to 100 seconds.

The figure 4.3, shows the comparison between the initial and the deformed structure. As expected, the oedometer undergoes a vertical along x lowering equal to  $6.89 E^{-05}$  m and a fast check is made in base of the elastic relationships:

$$\varepsilon_x = \frac{1}{E} [\sigma_x - \nu(\sigma_y + \sigma_z)] \quad (4.26)$$

Inasmuch as an oedometer simulation is proposed, the lateral deformation must be equal to zero and the stresses in the two directions y and z must be the same. Thus, it is possible to write:

$$\sigma_z = \sigma_y = \frac{\nu}{1 - \nu} \sigma_x = \frac{0.3}{1 - 0.3} 1 = 0.429 \text{ MPa} \quad (4.27)$$

Considering a material with Poisson's ratio of 0.3, Young modulus of 215 MPa and a vertical stress equal to 1MPa, the lateral stress the one represented in (4.27).

Knowing the stresses, it is possible to calculate the vertical deformation, i.e. the displacements:

$$\varepsilon_y = \frac{1}{215} [1 - 0.3 * 2 * 0.429] = 3.46 E^{-03} \quad (4.28)$$

Multiplying the result in the (4.28) for the high of the oedometer, i.e. 2 cm, the displacement is obtained

$$u_y = 3.46 E^{-03} * 0.02 = 6.9 E^{-05} m \quad (4.28)$$

The vertical displacement calculated is exactly the same proposed by the software, visible at the bottom of Figure 4.3 and, as a trend in Figure 4.4.

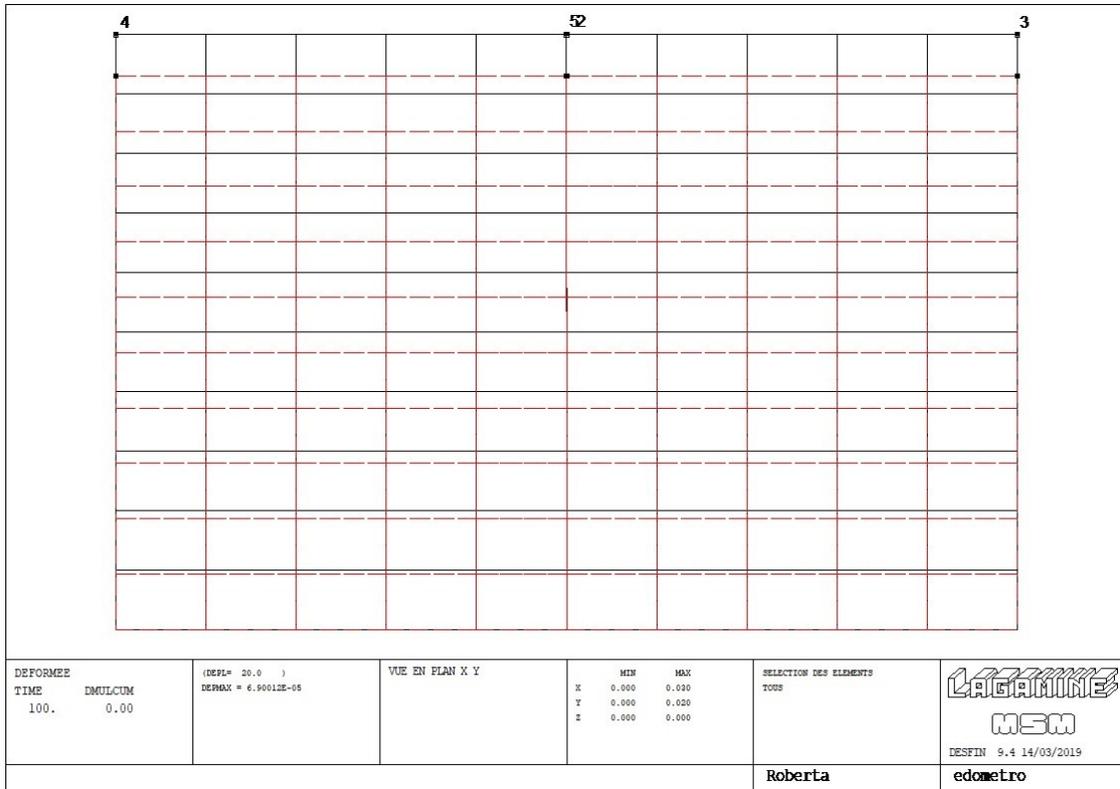


Figure 4.3 Initial structure in black, deformed structure in red

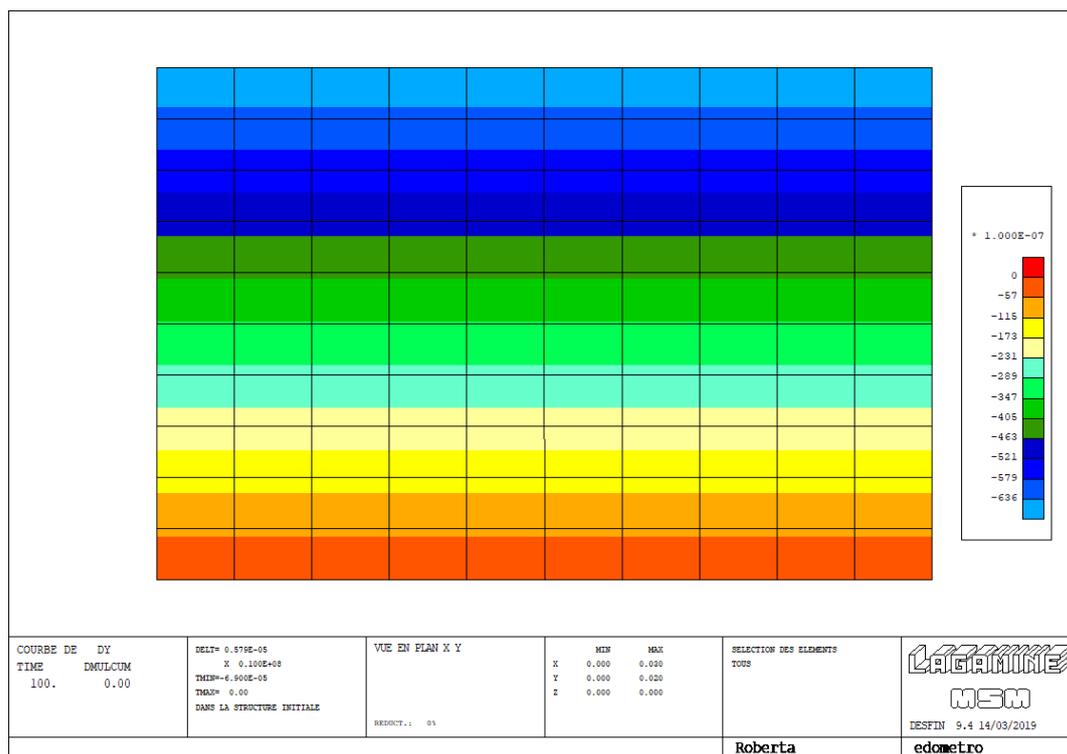


Figure 4.4 vertical displacement for mechanical problem

#### 4.4.2 Oedometer: hydro-mechanical problem

The second simulation is a hydro-mechanical analysis. To reach the purpose, the water pressure has been blocked only at the bottom and only at the right side, because of the axisymmetric problem. Beyond the usual mechanical properties, hydraulic ones are introduced, table 1. Thus, being the sample saturated, interstitial pressures will arise within the material and their trend is highlighted in the Figure 4.6. For this analysis, the time has been increased of 20 seconds to check the behaviour after the application of the load and the chart of displacement versus time for the point 4, i.e. the node at the top of the axis of symmetry, is shown below.

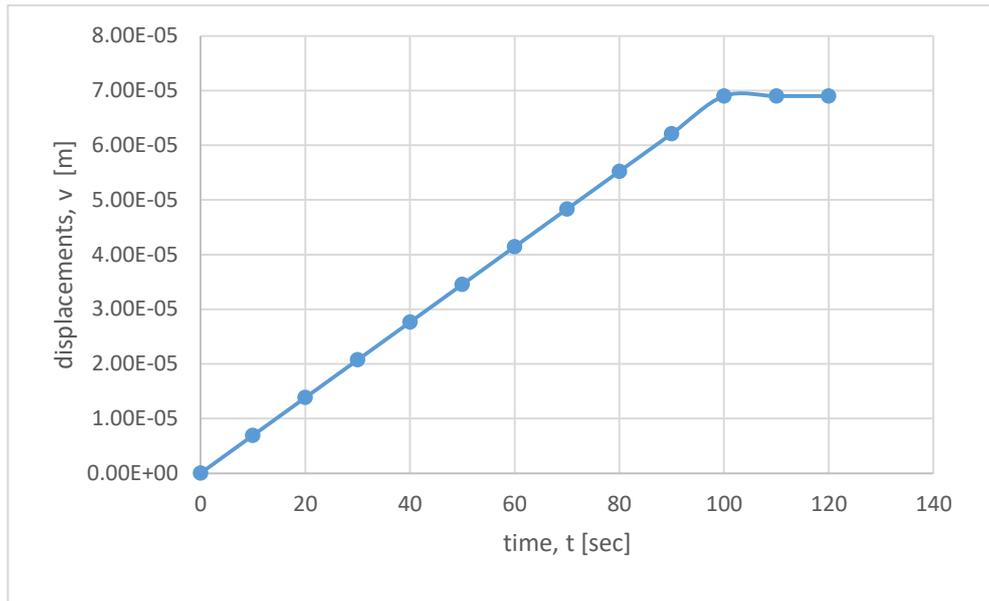


Figure 4.5 Vertical Displacements of point 4 for HM problem

As expected and as Figure 4.5 points out, the displacements increase linearly until the end of the application of the load, i.e. 100 seconds, after which, a plateau appears. The same trend is observed for the vertical stresses.

Regarding the water pressure, due to the fact that our sample is coarse sand, the material quickly dissipates overpressure, which is very low as value, and, as soon as the application of the load ends, water pressure drops to zero. This phenomenon is glaring watching the two figures below.

The figure 4.6 represents the water pressure within the sample at the first step, i.e. 10 seconds; it is possible to notice the concentration of overpressures at the axis of symmetry, according to the imposed conditions.

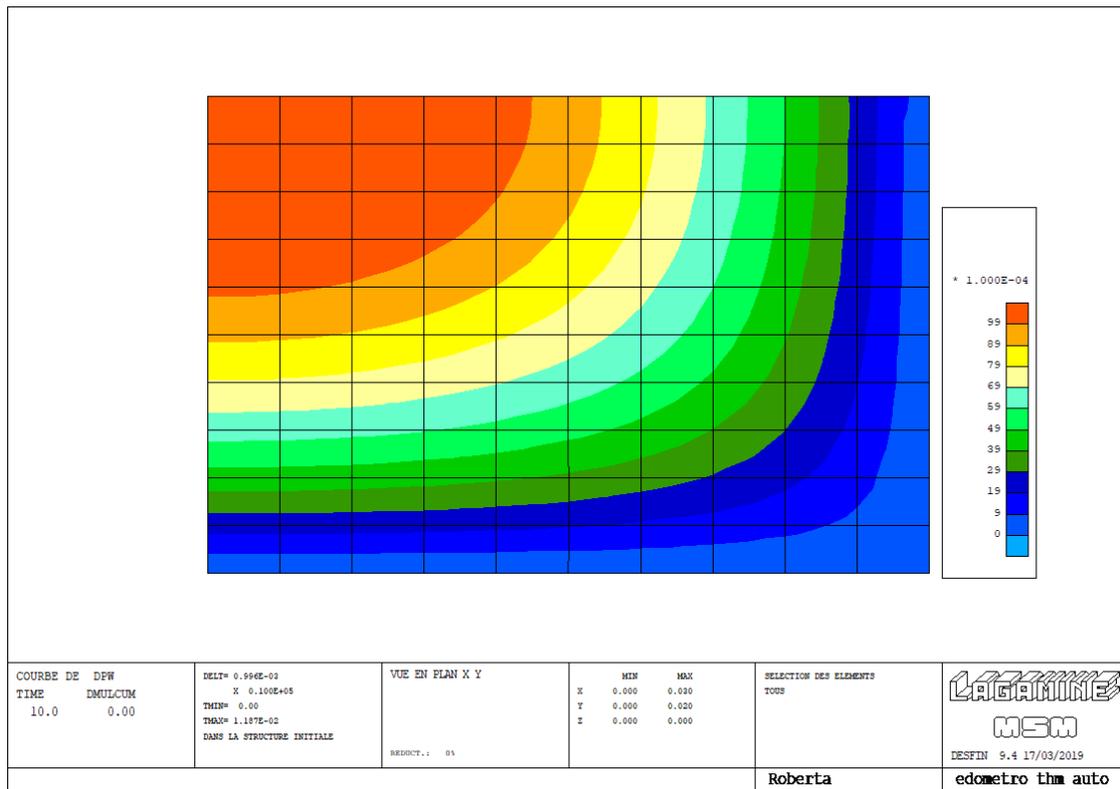


Figure 4.6 Interstitial pressures in a HM problem, at time 10 sec

At the end of the simulation, the water pressure is completely dissipated and, what is shown in the figure 4.7 is only a numerical trend because the overpressure has value of the order of  $10^{-14}$ , i.e. zero.

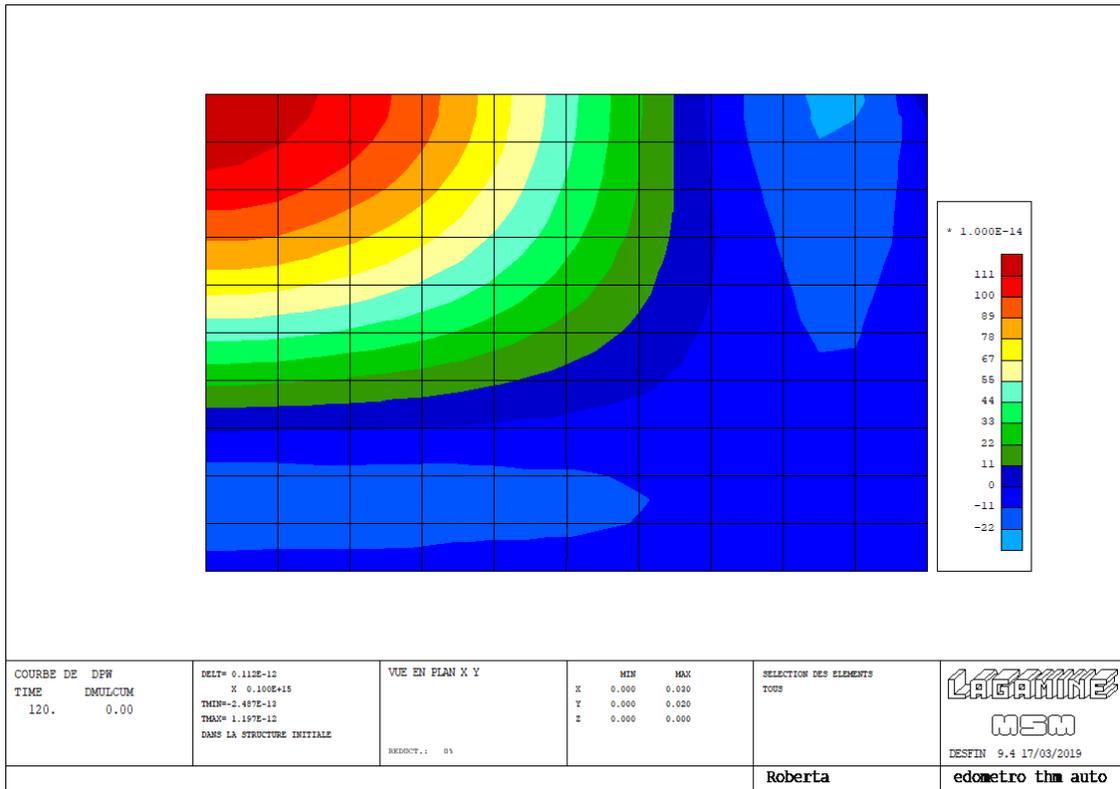


Figure 4.7 Interstitial pressures in a HM problem, at time 120 sec

#### 4.4.3 Oedometer: thermo-hydro-mechanical problem

The last preliminary analysis is focused on the THM problem. The difference from the other analysis is that the variation of temperature is imposed only for the nodes of the right side, i.e. the right side is heated from 20°C to 40°C. The temperature is imposed equal to 20°C at time 150 seconds, i.e. after the hydro-mechanical analysis, and equal to 40°C at time 500 seconds.

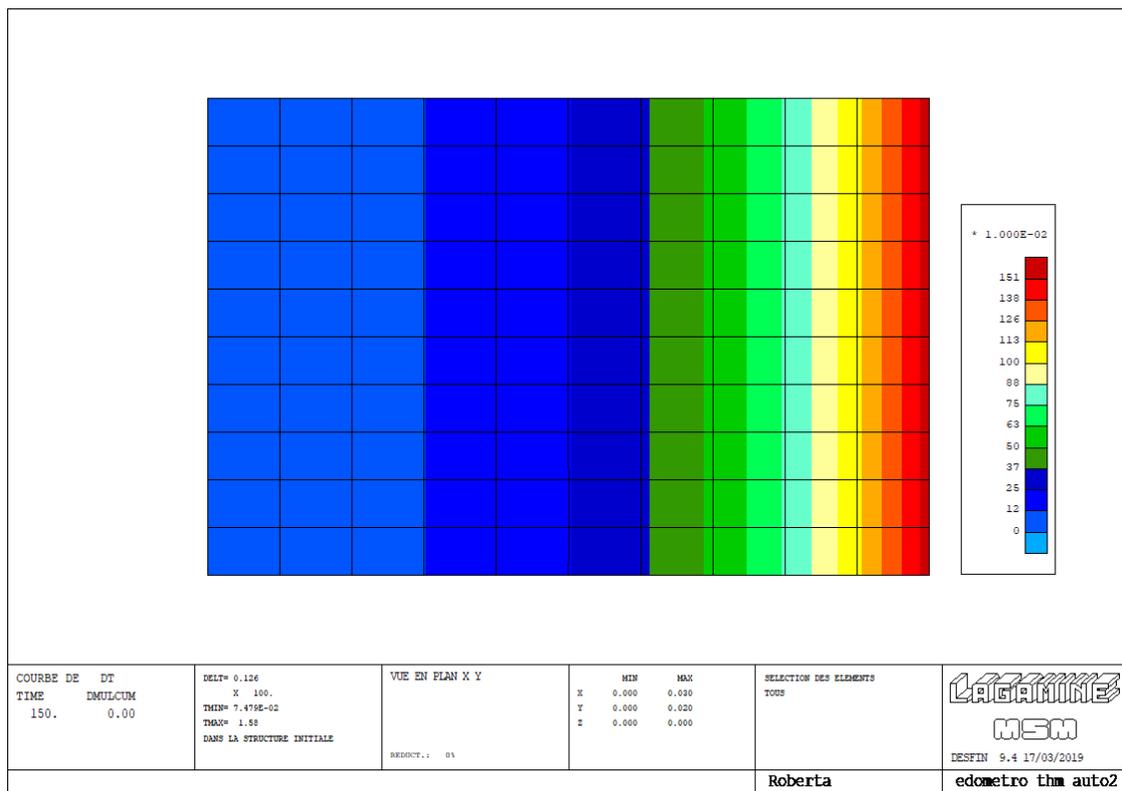


Figure 4.8 Variation of temperature in a THM problem, at 150 sec

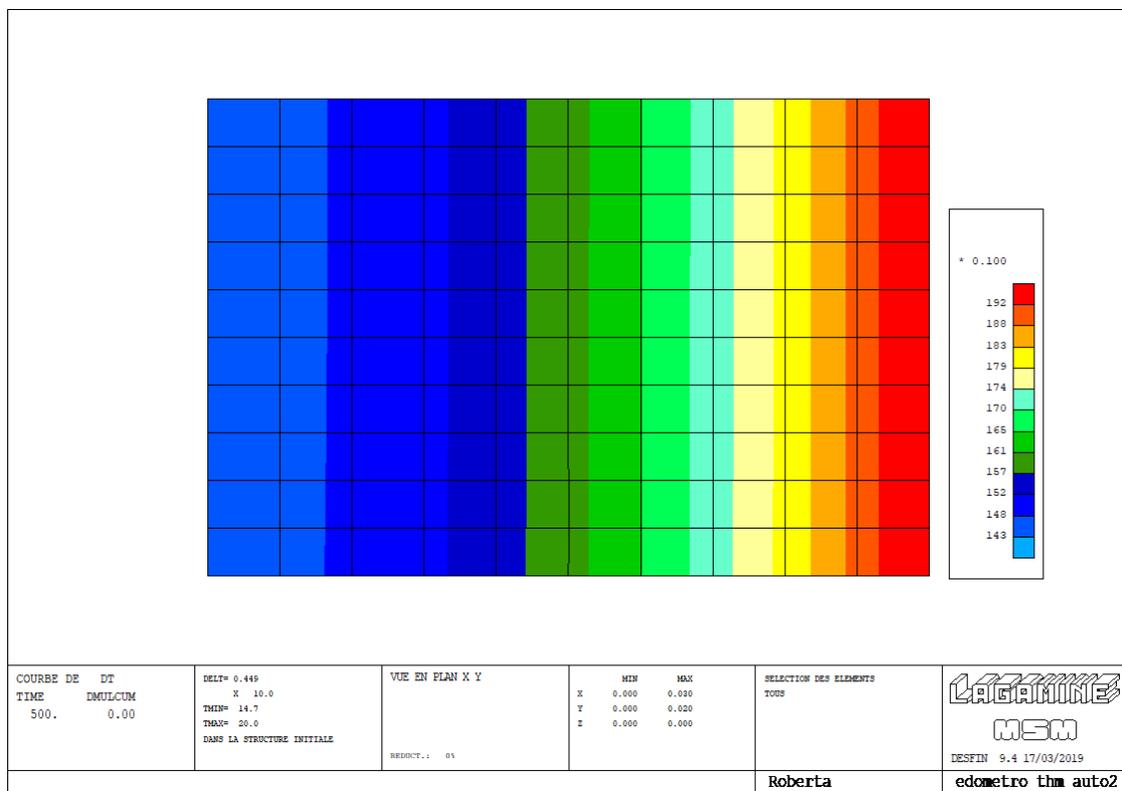


Figure 4.9 Variation of temperature in a THM problem, at 500 sec

The two figure above, show the heat diffusion through the sample at the two different time-steps, and the following one, highlights the variation of temperature as a function of time, for three point at the top of the sample: in the middle and in the two ends of it. Point 3 has a linear trend because the temperature there is imposed, on the other hand, point 4 and 52 present a non-linear trend because the variation of temperature is dictated by the thermal properties of the material.

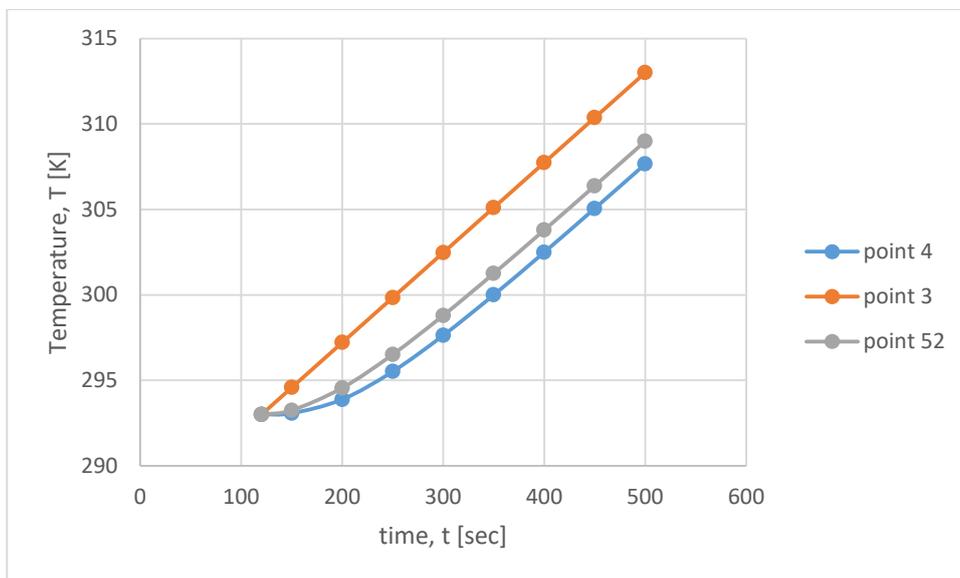


Figure 4.10 horizontal variation of temperature of points 4, 52, 3

Interesting observations can be made by observing the displacement graph of point 4, Figure 4.11. Indeed, the vertical displacements, understood as lowering of the specimen, decrease because of the heating that, instead, tends to make the soil expand.

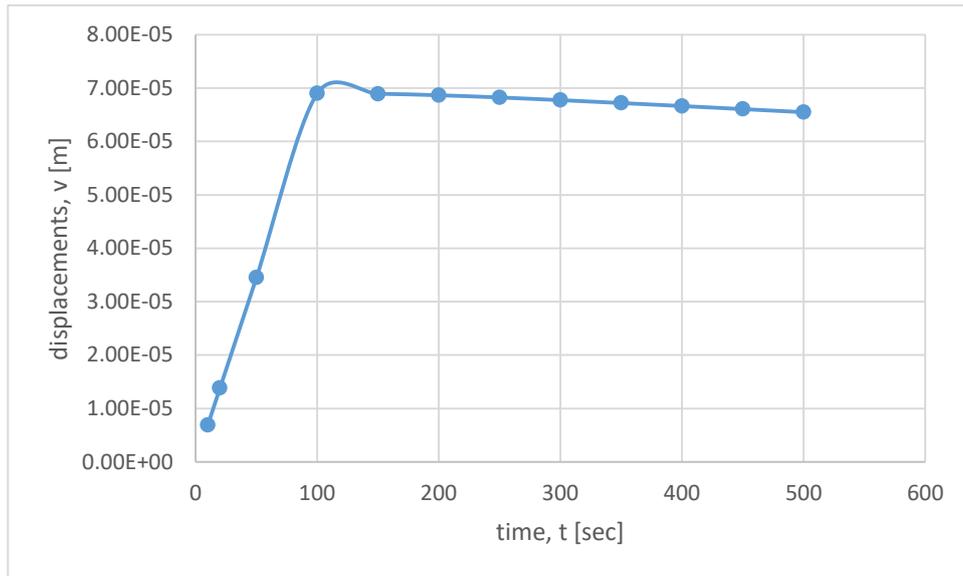


Figure 4.11 Displacements of point 4 in a THM problem

About the pressure, always of point 4, the same observations made for the displacements can be reported, i.e. the heating induces an increase of them as Figure 4.12 shows.

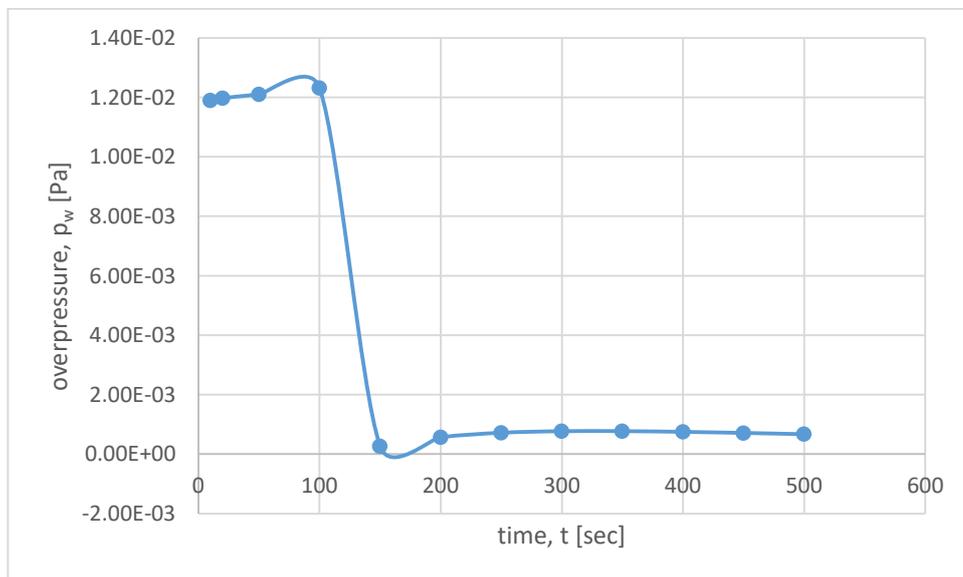


Figure 4.12 Interstitial pressure of point 4 for a THM problem

It is also worth bearing the variation in pressure as a function of temperature, and therefore indirectly of time. Indeed, as Figure 4.13 points out, the water pressure increases due to heating until around 27°C are

reached. After this value, it is possible to notice decreases of the overpressure due to the fact that the sample is sand and it can easily dissipate the interstitial pressure until the imposed temperature of 40°C is reached and its value stops at 308 Pa.

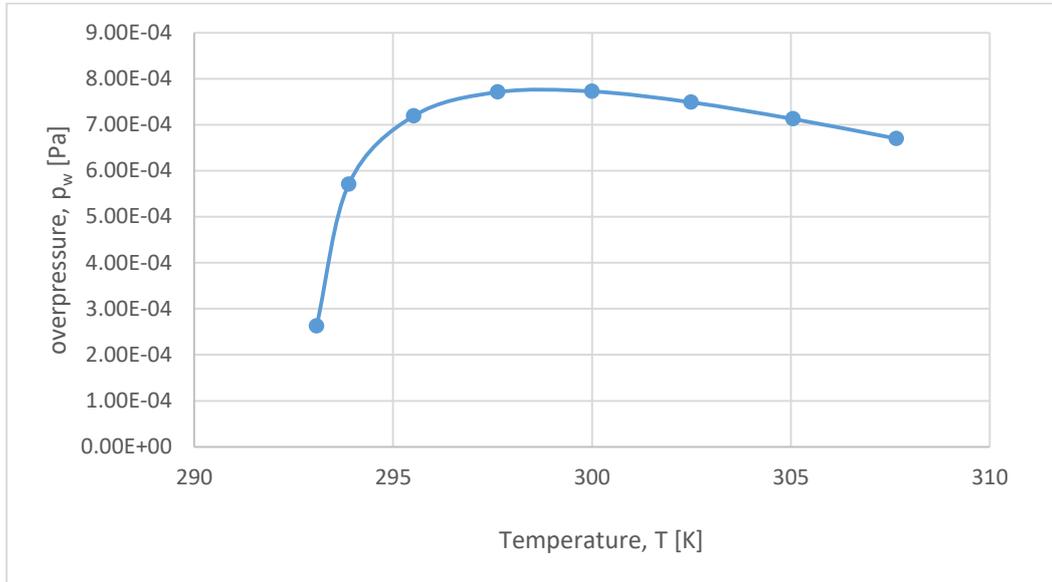


Figure 4.13 Overpressure of point 4 in function of temperature for a THM problem



## **5. Case study: thermo-mechanical analysis of the diaphragm wall of the underground car park in Turin**

### **5.1 General overview**

As explained in the previous chapters, e.g. 3.5, coupling the structural functionality with the geothermal one has various advantages. Especially, when considering structures embedded in the ground with an extended contact surface, such as diaphragm walls, the probability of success of the geothermal system is considerable.

For these particular structures, in addition to the geothermal study, required to monitor the exploitable thermal capacity, a thermo-mechanical analysis must be performed. The last one, it is fundamental to evaluate and control the stresses and deformations caused by the presence of an implant inside the diaphragm wall itself.

The aim of this thesis is to study the behaviour of an energy diaphragm wall, for this reason, the possible realization of the underground car park of via Ventimiglia, in Turin, will be analysed in this chapter, using the LAGAMINE software. Indeed, adjacent at the Unipolar Spinal Unit of the

T.O.C hospital (Turin Orthopedic Trauma Center), the idea of building an underground car park is being launched. The suggestion to introduce a geothermal system into the structure could represent added values as an incentive to carry on the work.

The underground car park, designed but not yet completed, will replace the current two-storey car park in front of the spinal unit of via Ventimiglia. To the study of the geothermal system and the foundation of the Ventimiglia parking lot, financed by the Piedmont Region - Enermhy Innovation Center, took part: the Polytechnic of Turin, Resolving srl and Teknema Progetti srl.

The geotechnical and structural project is supplied by Teknema Progetti srl and includes support structures along the entire external perimeter. About the geographical setting, the area is close to the Po river, i.e. presence of groundwater; on one side, the parking lot is in contact with the basement of another structure, the Unipolar Spinal Unit, but on the other three sides the diaphragm walls would be in contact with the ground and can be reasonably equipped with heat exchangers, as showed in figure 5.1.

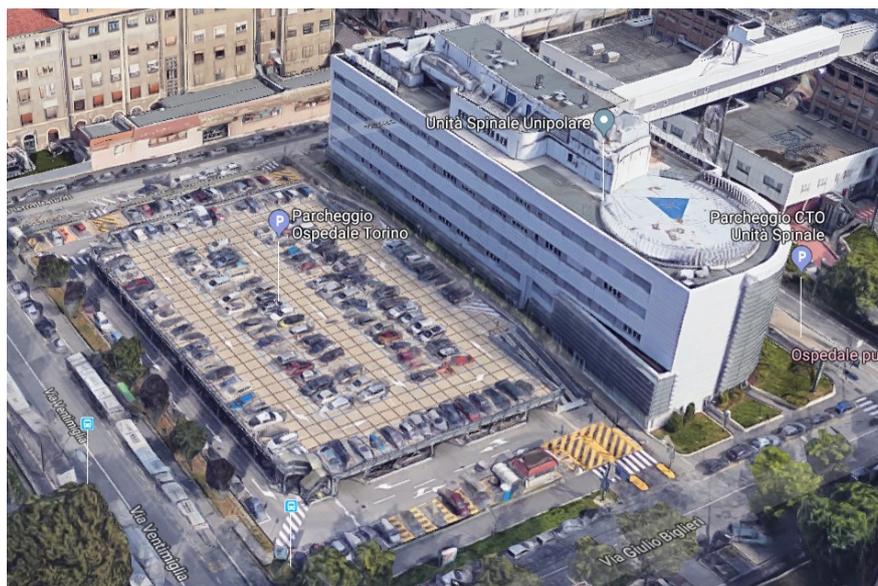


Figure 5.1 Image 3D of current Ventimiglia car park (Google Maps 3D)

Referring to the analyses conducted by Barla & Barla (2012) and  $N_{spt}$  investigations conducted by *Arpa Piemonte*, it is possible to associate the area considered to the geotechnical unit GU2, according to the degree of cementation and the stratigraphy of the soil. Indeed, the material properties will be referred to unit GU2: gravel and weakly cemented sand.

Table 2 Mechanical parameter of geotechnical units (Barla & Barla 2012)

Geotechnical unit	GU1	GU2	GU3	GU4
$C\%$ [%]	-	0÷25	25÷50	50÷75
$D_R$ [%]	50÷60	50÷70	60÷80	60÷80
$\gamma$ [ $kN/m^3$ ]	17÷19	18÷21	19÷22	19÷22
$E_d$ [MPa]	10÷20	190÷240	240÷300	300÷370
$\nu$ [-]	0,35	0,30	0,30	0,30
$\sigma_c$ [MPa]	0	0÷0,03	0,03÷0,14	0,14÷0,67
$m$ [-]	-	3÷4,8	4,8÷7,8	7,8÷12,5
$c$ [kPa]	0	0÷30	15÷80	50÷200
$\varphi$ [°]	36÷37	37÷39	37÷42	39÷48

Hydraulic parameters are introduced to complete the characterization of the Turin soil, always referring to the geotechnical unit 2, showed in table 3, although our analysis does not involve a hydraulic aspect, but only the thermo-mechanical one.

Table 3 Hydraulic properties of the Turin subsoil (Barla 2017)

Parameter	Symbol	Unit	Value
<i>Horizontal hydraulic conductivity</i>	$k_h$	[m/s]	$4.15 \cdot 10^{-3}$
<i>Vertical hydraulic conductivity</i>	$K_v$	[m/s]	$0.21 \cdot 10^{-3}$

<i>Porosity</i>	$n$	[-]	0.25
<i>Thermal capacity</i>	$\Lambda$	$Wm^{-1}K^{-1}$	2.26
<i>Thermal conductivity</i>	$\rho_s$	$Jkg^{-1}K^{-1}$	1053
<i>Longitudinal dispersion</i>	$\alpha_L$	[m]	3.1
<i>Transverse dispersion</i>	$\alpha_T$	[m]	0.3

## 5.2 Technical description of the project

The project consists of a rectangular structure of external sides of 93.25x52.0 m, with three underground levels (Figure 5.2).

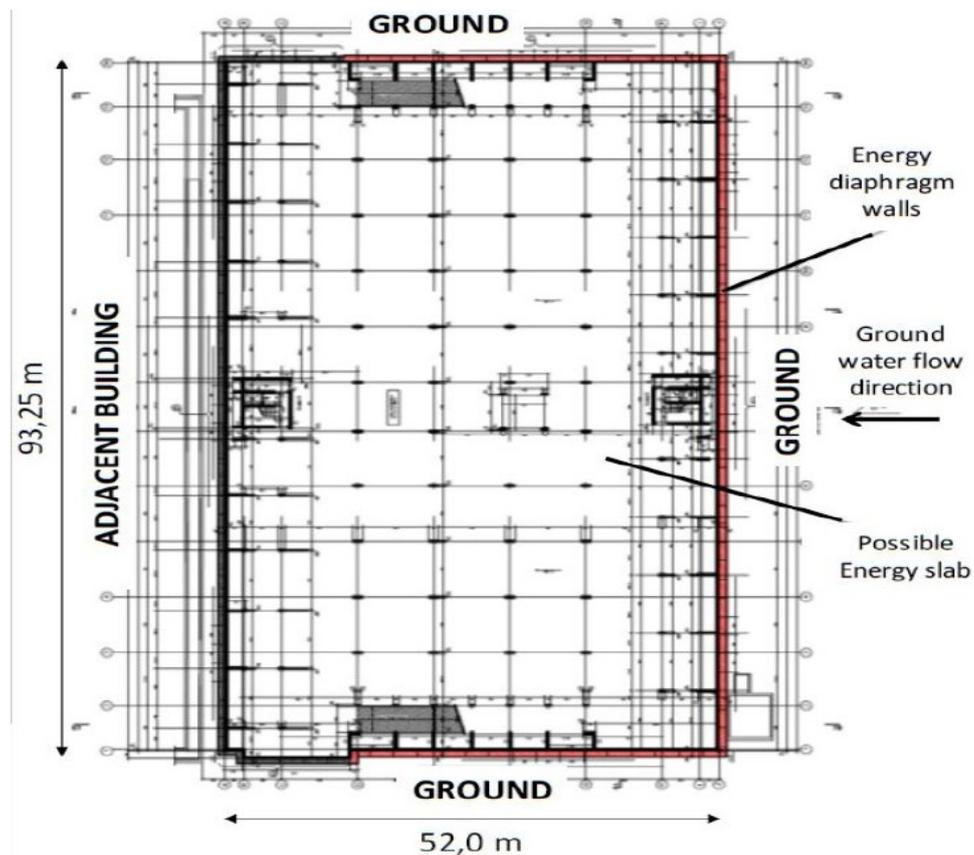


Figure 5.2 Underground car park plan (Di Donna, 2016)

The heights of the interpiano are equal to 2.45 m, with a horizontal covering thickness of 40 cm, intermediate horizontal of 25 cm thick and a bottom slab of 60 cm thick. The building, to support the altimetric variability of the

countryside plan and of the surrounding road network, is designed with a slope perpendicular to the Via Ventimiglia of 1% to go down towards the T.C.O. The diaphragm wall are therefore 15.5 m deep, looking at the figure 5.3 it will be easy to understand the geometry.

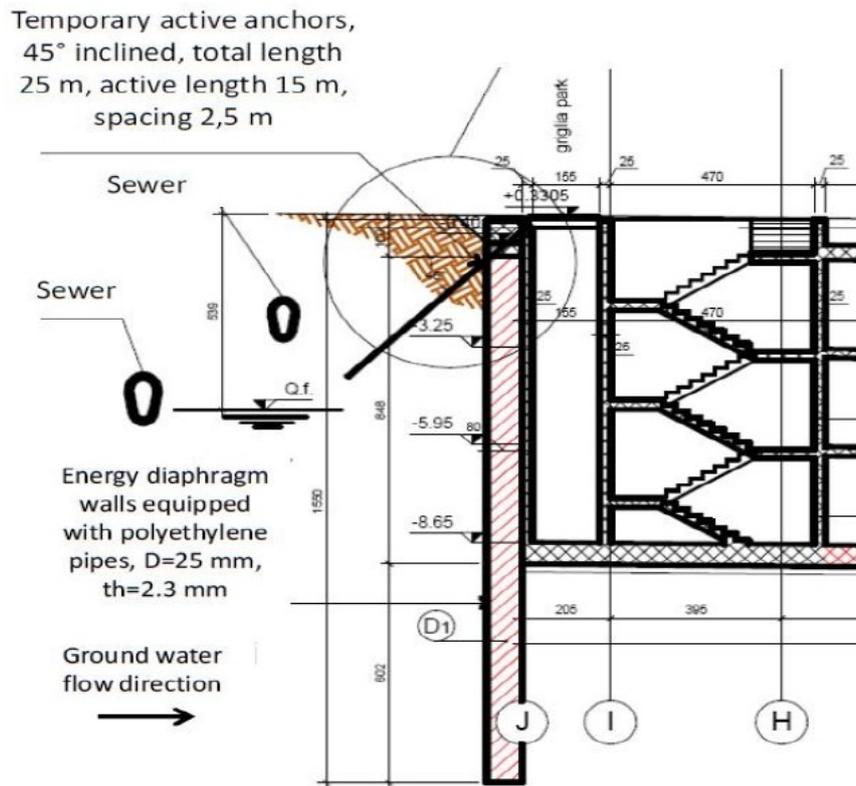


Figure 5.3 Vertical section of the underground car parking (A. Di Donna, 2016)

Regarding the materials used to construct the diaphragm and the bottom slab, concrete and steel were used. The concrete is a C32 / 40, while steel is a B450C. For the elastic modulus values of both materials, reference was made to the New Technical Standards for Construction (NTC; Ministry of Infrastructure and Transport, 2018).

In the diaphragm there are also reinforcements, both longitudinal and transversal. To consider their contribution, an equivalent elastic modulus of the concrete was calculated.

In the LAGAMINE software, concrete has been considered as an elastic, homogeneous and isotropic medium. The mechanical and thermal characterization parameters have been reported in Table 4.

Table 4 Mechanical and thermal properties of the concrete C32/40

Parameter	Symbol	Unit	Value
Young modulus	$E_d$	[MPa]	33 300
Poisson coefficient	$\nu$	[-]	0.2
Specific weight	$\gamma$	[kN/m <sup>3</sup> ]	25
Thermal conductivity	$\Lambda_s$	$Wm^{-1}K^{-1}$	2.3
Specific heat coefficient	$\rho_s$	$Jkg^{-1}K^{-1}$	876
Coefficient of linear thermal expansion	$c_s$	[-]	$1.2 \cdot 10^{-5}$
Intrinsic permeability	$k_p$	[m <sup>2</sup> ]	$10^{-16}$
Porosity	$n$	[-]	0.12

In order to transform a simple diaphragm wall into an energy diaphragm wall capable of exchanging heat, polyethylene exchangers must be installed at the reinforcement cage before the concrete casting. In this case study, 13 exchanger tubes with the heat transfer fluid inside are assumed to have a diameter of 25 mm. The position of the tubes inside the diaphragms was selected based on a preliminary optimization study (Fig. 5.4); these are installed only on the three sides in contact with the ground, omitting the one in contact with the neighbouring structure (Fig. 5.4). The inlet and outlet of the tubes are supposed to be connected to a main circuit that connects the pipes to the heat pumps.

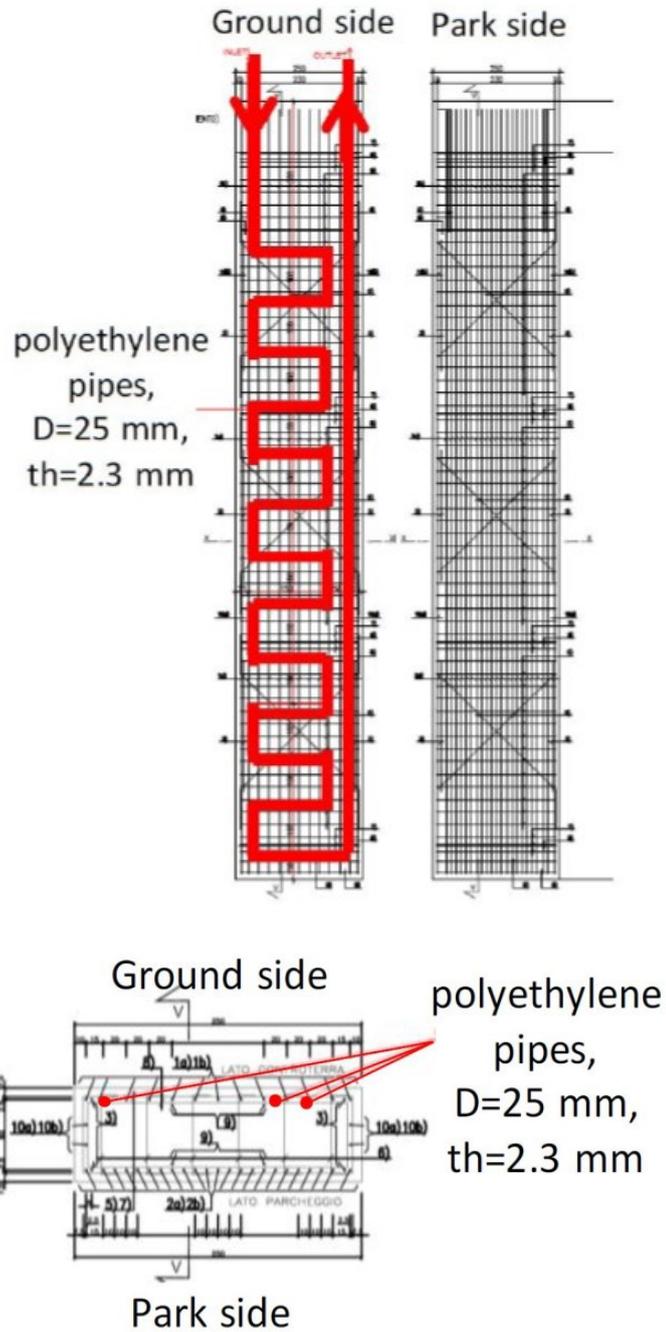


Figure 5.4 Position of the exchanger pipes and reinforcement cage

### **5.3 Identification of the diaphragm wall behavior with analytical calculation**

To implement the model, a single section of the Ventimiglia underground car park was taken into consideration. The chosen section is oriented in the direction E-W and it is orthogonal to the long side of the car park. Furthermore, as a representative section, the one at the center of the diaphragm wall was selected.

It must be said that it was decided to simulate the thermo-mechanical behavior of the diaphragm wall without the surrounding soil. The choice was made to understand if it was possible to simplify the FE analysis in order to reach the purpose. Indeed, from an engineering point of view, the only behavior that matters is the one of the geostructure. Logically, the performance of a geostructure depends on the loading conditions to which it is located, i.e. on the soil. Indeed, after defining the geometry of the structure, the load due to the soil, was applied. Regarding the latter, the concept of active and passive thrust must be introduced.

#### **5.3.1 Active and passive thrusts**

Like all engineering works, retaining structures must be designed to meet safety and functionality requirements. When a retaining structure, or a part of it, does not meet these requirements, it has reached a limit state. The Rankine theory refers to limit state and hypothesizes flat sliding surfaces, but due to the friction between the wall and the ground, the actual sliding surfaces are partially curved and the results are often non-precautionary. For this reason, must use precautions.

The hypotheses underlying the theory are:

- Homogeneous soil ( $\gamma = \text{const}$  along the depth);
- Surface of the G.L. horizontal and infinitely extended;
- Inconsistent soil ( $c' = 0$ );
- Absence of groundwater ( $u = 0, \sigma = \sigma'$ );
- Validity of the Mohr-Coulomb failure criterion ( $\tau_f = \sigma_n' \tan \varphi'$ );
- Absence of overloading at ground level;

All the hypotheses can be considered valid for our case. Indeed, the only two approximations made involve cohesion null, in favour of security, and no groundwater, in any case our analysis is the thermo-mechanical one that does not involve any water.

The Rankine theory presents notable analogies with the solutions deriving from the static theorem of the limit analysis. In it is assumed that the tensional state acting on a vertical wall is the existing one, in limit conditions, on the corresponding vertical arrangement thought to belong to an indefinite half-space. This hypothesis does not allow to take into account the friction at the wall-ground contact, this being a local phenomenon. The tensions acting on the vertical position in the boundary conditions assume a triangular distribution, with a line of action parallel to the ground plane, assumed horizontal.

The roughness of the wall-ground contact produces an inhomogeneous tension state in the ground that interacts with the retaining structure. In fact, while at great distances the friction between the wall and the ground is not affected and the main directions of tension are fixed (for example: vertical and horizontal directions for horizontal ground level), near the wall the presence of tangential tensions on the lying vertical produces a rotation of the main directions. Approaching the wall, therefore, there is a

progressive rotation of the main directions of tension, which can be described by the composition of infinitesimal rotations, each of which can be thought to be produced by an infinitesimal discontinuity of the tension state between two contiguous regions. Once assumed a distribution of tensions congruent with this physical intuition, and compatible with the balance and the law of plasticity, the static theorem of the limit analysis ensures its validity. The solution can be expressed by providing the effective tension acting in the normal direction to the wall-ground contact as a function of the effective tension evaluated in the region distant from the wall (Lancellotta, 2002; Mylonakis et al., 2007). These solutions provide a precautionary estimate of the actions transmitted to the wall in boundary conditions and also have the advantage of being expressed in a closed form.

Wanting to take into account the roughness of the soil - wall contact, a cautionary estimate of the thrusts is obtained by applying the static theorem of the limit analysis (Lancellotta, 2002; Mylonakis et al. 2007) and so the limit effective tensions agents in the normal direction to the wall are expressed in form:

$$\sigma'_{a,p} = \cos \delta \cdot \left[ \frac{\cos \delta \mp \sqrt{\sin^2 \varphi' - \sin^2 \delta}}{\cos i \pm \sqrt{\sin^2 \varphi' - \sin^2 i}} \right] \cdot e^{\mp 2\psi \tan \varphi'} \cdot (\gamma' z \cdot \cos i) = K_{a,p} \cdot \cos \delta \cdot \gamma' z \quad (5.1)$$

With

$$2\psi = \sin^{-1} \left( \frac{\sin \delta}{\sin \varphi'} \right) \mp \sin^{-1} \left( \frac{\sin i}{\sin \varphi'} \right) \mp \delta + i \quad (5.2)$$

where  $\psi$  represents the rotation of the principal directions of tension between the regions distant and close to the wall, and  $i \cdot z \cdot \cos \cdot \gamma'$  is the

effective vertical tension acting, in the region distant from the wall, on a position parallel to the ground plane indefinitely inclined and  $\delta$  is the angle of friction wall-ground chosen as  $2/3$  of the friction angle of the soil ( $38^\circ$ ).

Table 4 reports the parameters of the soil, according to the geotechnical unit 2 define in chapter 5.1, and the corresponding active and passive thrust coefficients, calculated as per formula (5.1).

Table 5 Properties of the soil

Parameter	Symbol	Unit	Value
Young modulus	$E_d$	[MPa]	215
Poisson coefficient	$\nu$	[-]	0.3
Specific weight	$\gamma$	[kN/m <sup>3</sup> ]	19.5
Porosity	$n$	[-]	0.25
Friction angle	$\varphi$	[°]	38
Friction angle wall-ground	$\delta$	[°]	25.3
Active thrust coefficient	$K_a$	[-]	0.24
Passive thrust coefficient	$K_p$	[-]	8.15

The diaphragm considered is unconstrained, i.e. fixed Earth support is the condition considered. In this particular case, the stability is entrusted to the ground detachable. The analysis is to limit state, thus the breaking mechanism is a rotation around a point O called the interlocking section (Figure 5.5).

Aat the moment of collapse, above O active stress is the one on the side of the ground to support (left side), passive stress is the one offered by the ground below the excavation (right side). Below O the stresses are

exchanged and in figure 5.5 it is possible to recognize the active action as the red one and the passive soil action as the green one.

Furthermore, it can be established that the piling depth  $D$  is 20% of the depth of the point  $O$ , from inverse formula the depth of rotation point  $O$  is obtained:

$$y_o = \frac{D}{1.2} = \frac{6}{1.2} = 5 \text{ m} \quad (5.3)$$

To verify that this approximation is correct, a simple check is made through the equilibrium of horizontal translation, in order to obtain the reaction  $R_{eq}$  that will be compared with the real one, i.e.  $R_{real} \geq R_{eq}$ . Where  $R$  is the resultant of active and passive stresses below the point  $O$ .

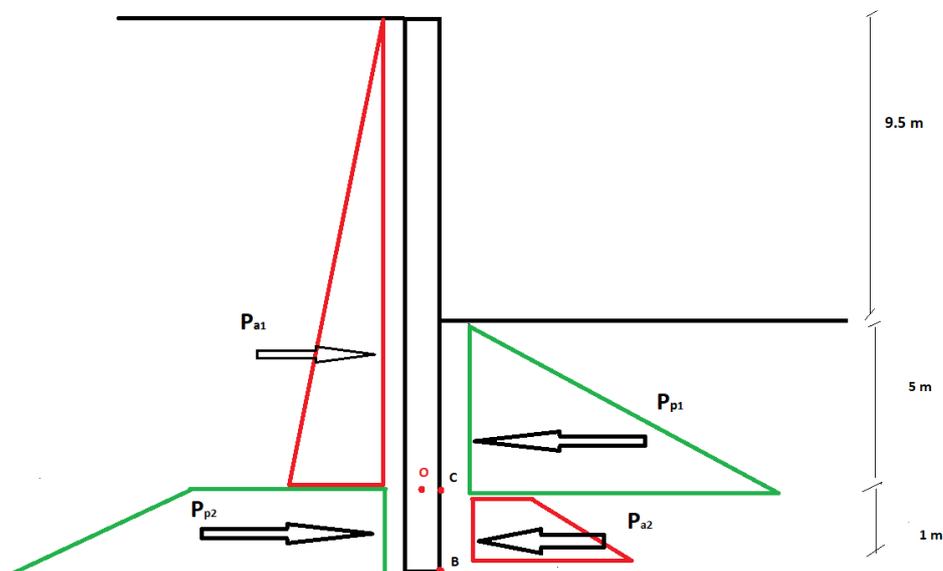


Figure 5.5 Active and passive thrust of the soil

To obtain  $R_{eq}$  the active thrust  $P_{a1}$  and the passive thrust  $P_{p1}$  must be calculated:

$$P_{a1} = \frac{1}{2} \sigma_a H = \frac{1}{2} \gamma K_a H^2 = \frac{1}{2} 19.5 \cdot 0.24 \cdot (9.5 + 5)^2 = 492 \frac{kN}{m} \quad (5.4)$$

$$P_{p1} = \frac{1}{2} \sigma_p y_0 = \frac{1}{2} \gamma K_p y_0^2 = \frac{1}{2} 19.5 \cdot 8.15 \cdot (5)^2 = 1986.56 \frac{kN}{m} \quad (5.5)$$

$$R_{eq} = P_{p1} - P_{a1} = 1986.56 - 492 = 1494.6 \frac{kN}{m} \quad (5.6)$$

The real resultant R is calculated considering the thrust below point O as:

$$\sigma_{a2C} = \gamma K_a H^2 = 19.5 \cdot 0.24 \cdot (5)^2 = 23.4 \frac{kN}{m^2} \quad (5.7)$$

$$\sigma_{a2B} = \gamma K_a H^2 = 19.5 \cdot 0.24 \cdot (6)^2 = 28.08 \frac{kN}{m^2} \quad (5.8)$$

$$P_{a2} = \frac{1}{2} (\sigma_{a2B} - \sigma_{a2C})(D - y_0) + \sigma_{a2C} (D - y_0) = 25.38 \frac{kN}{m} \quad (5.9)$$

$$\sigma_{p2C} = \gamma K_p H = 19.5 \cdot 8.15 \cdot (9.5 + 5) = 2304.41 \frac{kN}{m^2} \quad (5.10)$$

$$\sigma_{p2B} = \gamma K_p H_{tot} = 19.5 \cdot 0.24 \cdot 15.5 = 2463.33 \frac{kN}{m^2} \quad (5.11)$$

$$P_{p2} = \frac{1}{2} (\sigma_{p2B} - \sigma_{p2C})(D - y_0) + \sigma_{p2C} (D - y_0) = 2383.9 \frac{kN}{m} \quad (5.12)$$

$$R_{real} = P_{p2} - P_{a2} = 2383.9 - 25.83 = 2358.1 \frac{kN}{m} \quad (5.13)$$

$$R_{real} \geq R_{eq} \quad 2358.1 \frac{kN}{m} \geq 1494.6 \frac{kN}{m} \quad (5.14)$$

The check is satisfied, thus the rotation point can be considered, with a good approximation, the real one.

Knowing the thrusts and the rotation point, it is possible to chart the bending moment (Figure 5.6 ), useful for doing comparison with the results given by the LAGAMINE software.

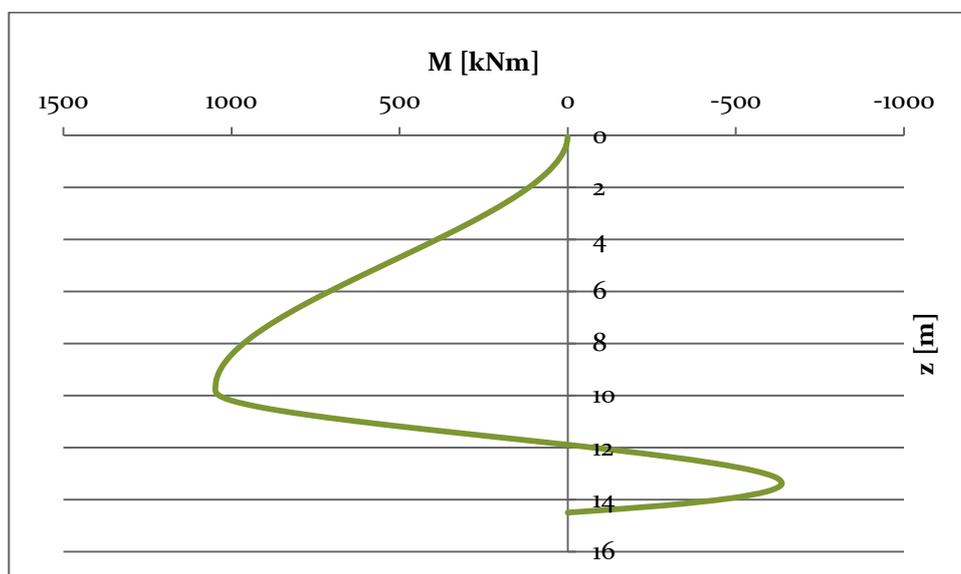


Figure 5.6 Bending moment calculated by active and passive thrusts

#### 5.4 Finite element numerical modeling

The knowledge of the geometry of the diaphragm wall, paragraph 5.2, and the loads acting on it, allows to create the model using the LAGAMINE software. Thus, the geometry and boundary conditions were set into the "GMAIL file". The mesh was created dividing the several segments into an appropriate number to create finite elements of 0.20x0.25 m. Indeed, the upper and lower ends of the diaphragm, 0.8 m thick, have been divided into 4 segments each of 0.20 m. On the other hand, the lateral ends, 15.5 m of the overall length, have been divided into 58 parts. The final mesh is represented in the figure 5.7.

Afterwards, the diaphragm wall has been loaded with the load distributed linearly due to the soil actions, obtained in chapter 5.3.1. In addition,

boundary conditions have been settled, i.e. the translation of point O in the two directions has been fixed and two rollers have been placed at the bottom of the diaphragm wall to simulate the “fixed Earth support” condition (Figure 5.7).

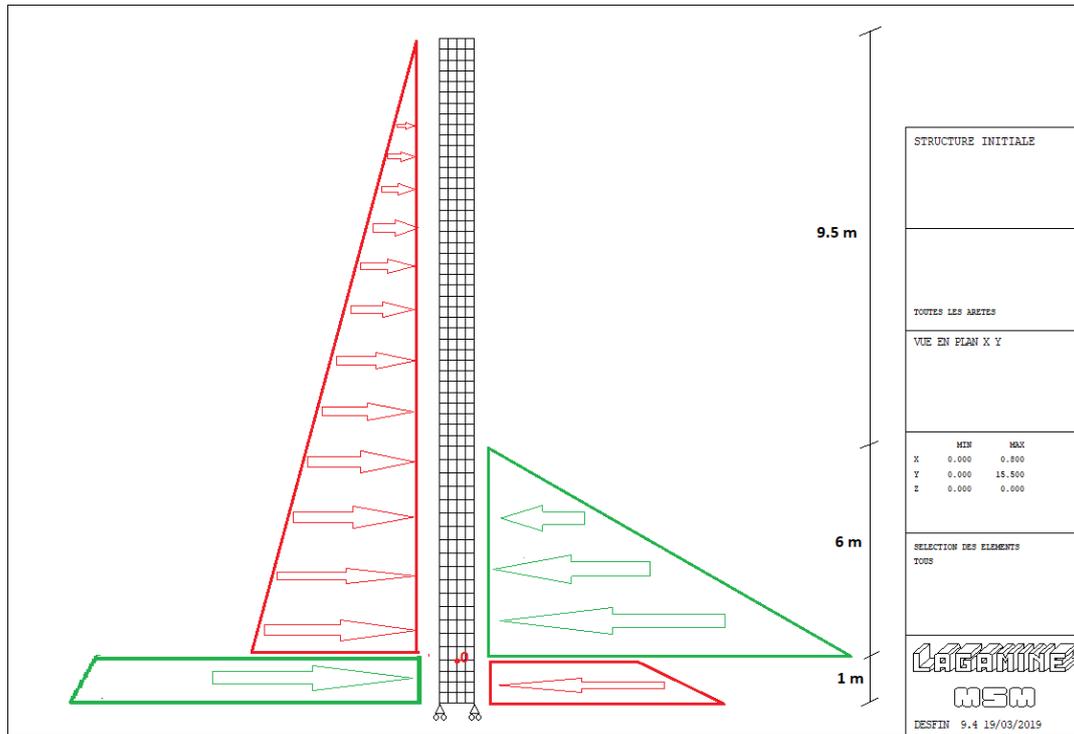


Figure 5.7 Mesh of the initial structure

The next step was to set the properties of the diaphragm wall into the “DATA file”. The type of concrete used has been define in chapter 5.2, table 4. Moreover, the initial condition of temperature has been fixed for all the nodes equal to 14°, according to the Torino subsoil conditions (Di Donna, 2016). Lastly the elements has been defined as “MWAT2”, that allows to do a complete THM analysis, even though only TM analysis will be done.

To be sure that all the information written is correct, *Prepro* button is made to run.

The “LOADING file” is the one where all created files are called up to run the software and get the results. Indeed, into the *LOADING file* are defined

the time steps that are wanted to be reported into the results, the increment of the time calculation decided and here it is imposed to read the “*LIC and DEP files*”.

The *LIC* file is where load times are imposed. As a matter of fact, at time 0 second no load is imposed. Then, to simulate the excavation, the linear distributed loads are made to grow linearly. In fact, at time  $8.64E^{04}$  seconds (1 day), it is imposed a increment of imposed force multiplier equal to 1, i.e. at that time all the loads defined into the *DATA file* are applied to the maximum value.

The “*DEP file*” it is proper to the thermal analysis. The file dictates the times of thermal variation imposed to the nodes chosen, in this case on the exchanger tubes. For the initial mechanical analysis this file is not used.

Another useful file is the “*PRI file*”. Here it is possible to select the values wanted, referred to the chosen nodes and elements, to print them later.

After setting the several files, the program can be run pushing on the *Lagamine* button.

All the files described above can be viewed in the Appendix 1.

## **5.5 Interpretation of the results**

Now that the LAGAMINE software has all the needed files, it is possible to pull out the desired results, export them on Excel and thus analyse them.

### 5.5.1 Mechanical results

The first analysis made is the mechanical one. The simulation of the excavation, on the right side, is done controlling the active and passive thrust of the soil, letting them vary linearly from time 0 sec to time  $8.64 E^{04}$

sec (1day). The value and trend of the trusts is the one reported in the paragraph 5.3.1.

Due to the actions of the soil, the diaphragm wall will suffer a deformation like in Figure 5.8. Moreover, a changing in stress will appear and of course a bending moment will characterize the geostructure.

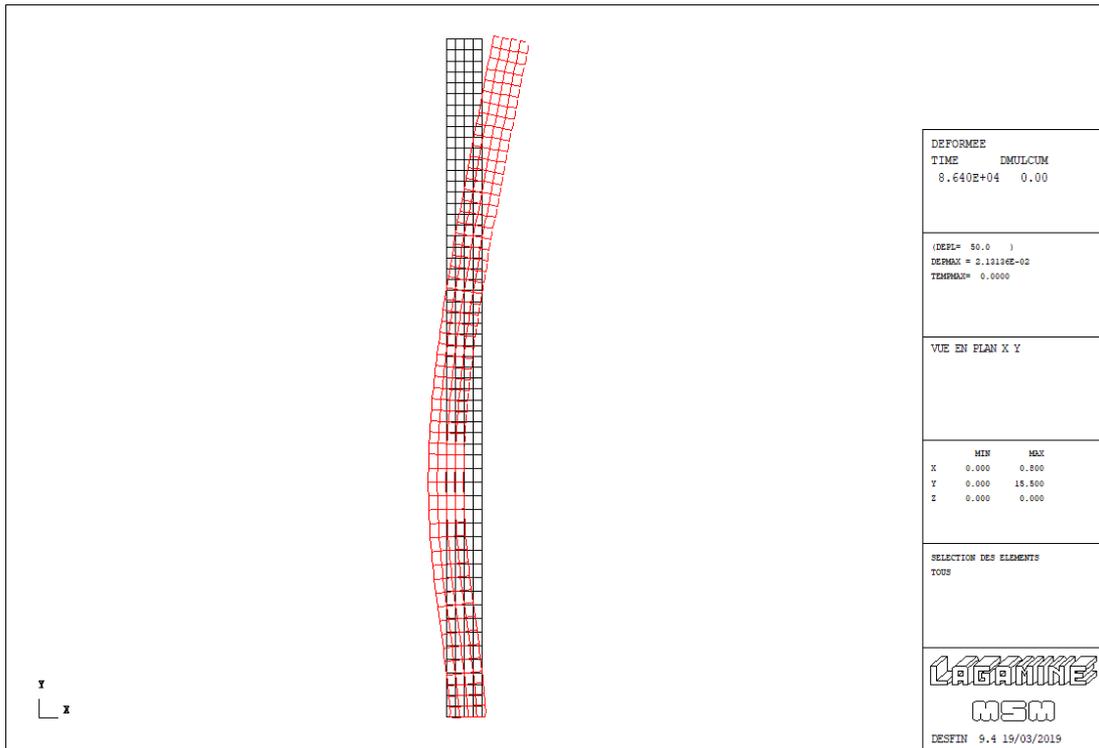


Figure 5.8 Deformed structure due to soil thrusts

When the excavation is finished, the maximum displacement occurs at the top of the structure and it is equal to 20.6 mm, as shown in Figure 5.9.

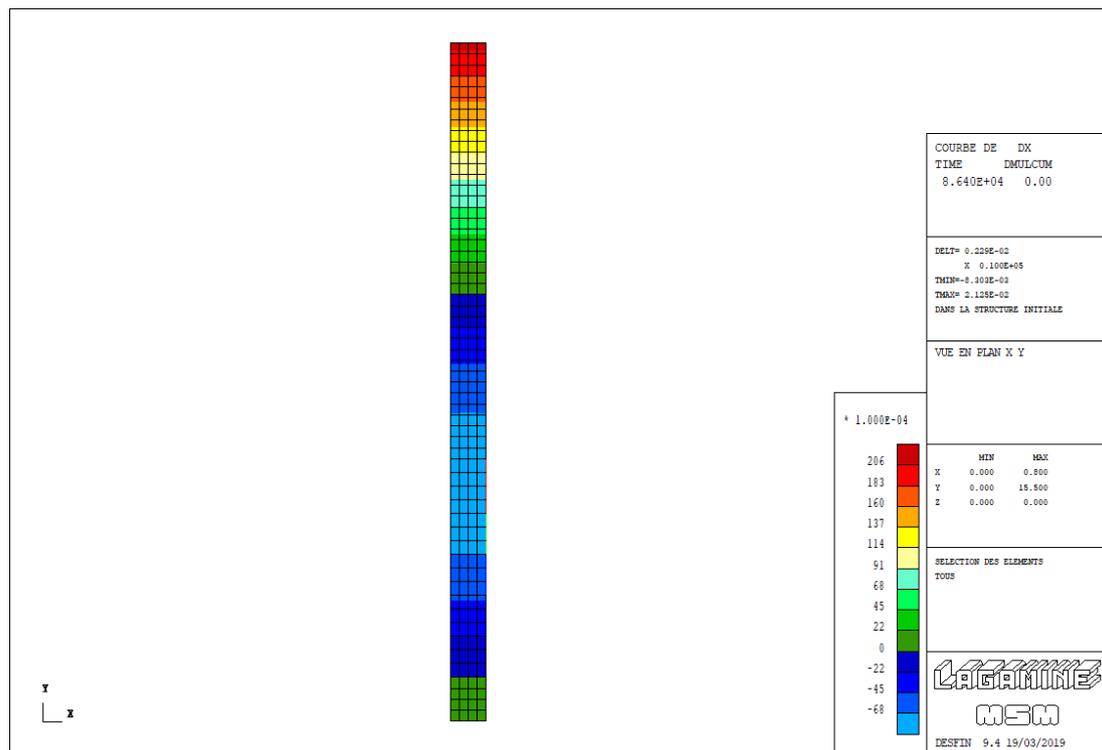


Figure 5.9 Horizontal displacements of the diaphragm wall for the mechanical analysis

Besides the displacements directly provided by the software, it is possible to plot horizontal displacements and bending moment from the value of variation of the coordinate x and the variation of stresses, printed through PRI file (Figures 5.10, 5.11).

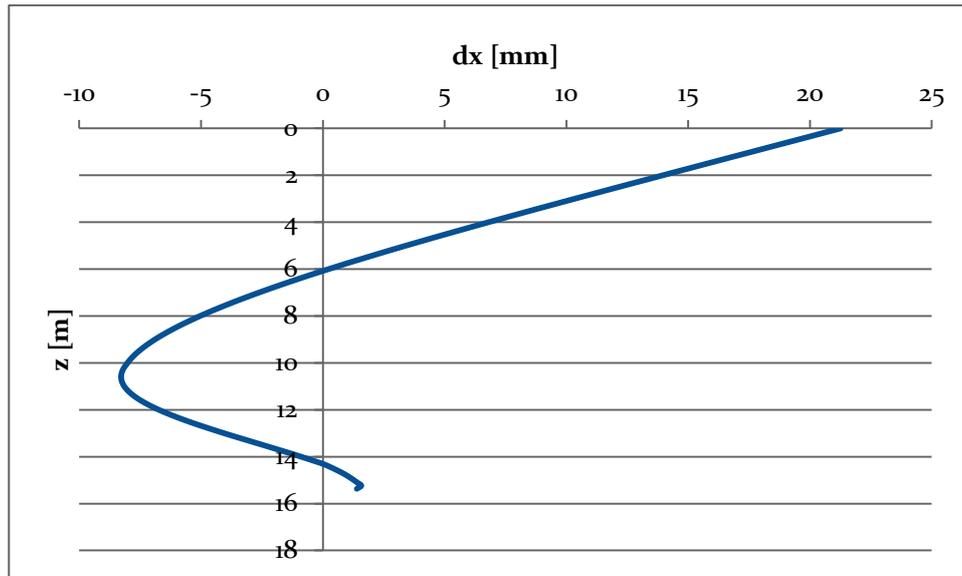


Figure 5.10 Horizontal displacements obtained

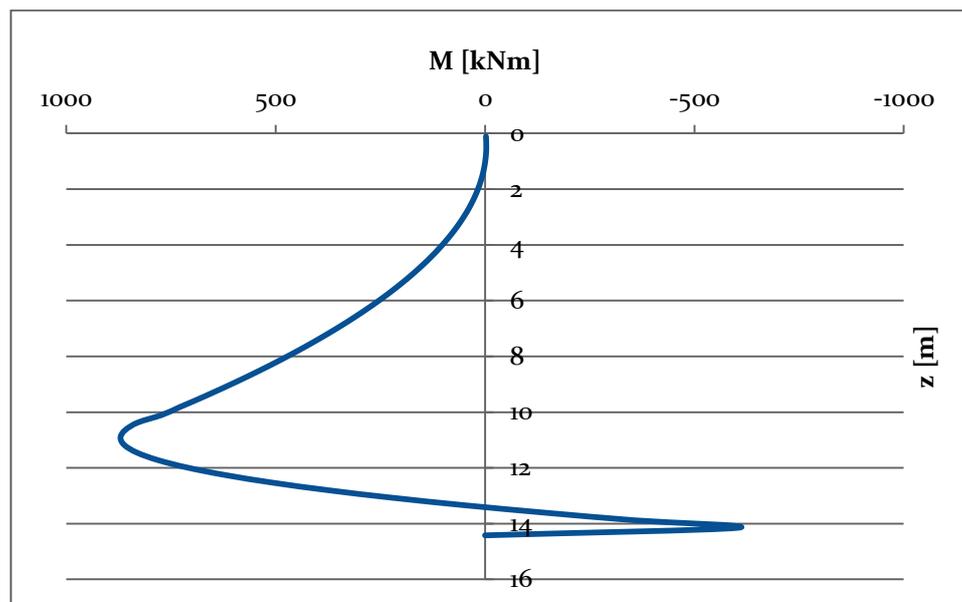


Figure 5.11 Bending moment from mechanical analysis

It is possible to do a comparison with the analysis made by Barla et al. (2018). The paper studies the same diaphragm wall, in the same context, but in the total complex, i.e. with surrounding soil and bottom slab. Even if the constraint conditions are different, i.e. bottom slab, an interesting comparison can be made. Indeed, with the complete model, the displacement at the top of the structure, due to the only excavation, are

equal to 17 mm, comparable in order of magnitude with the result just obtained (Figure 5.12).

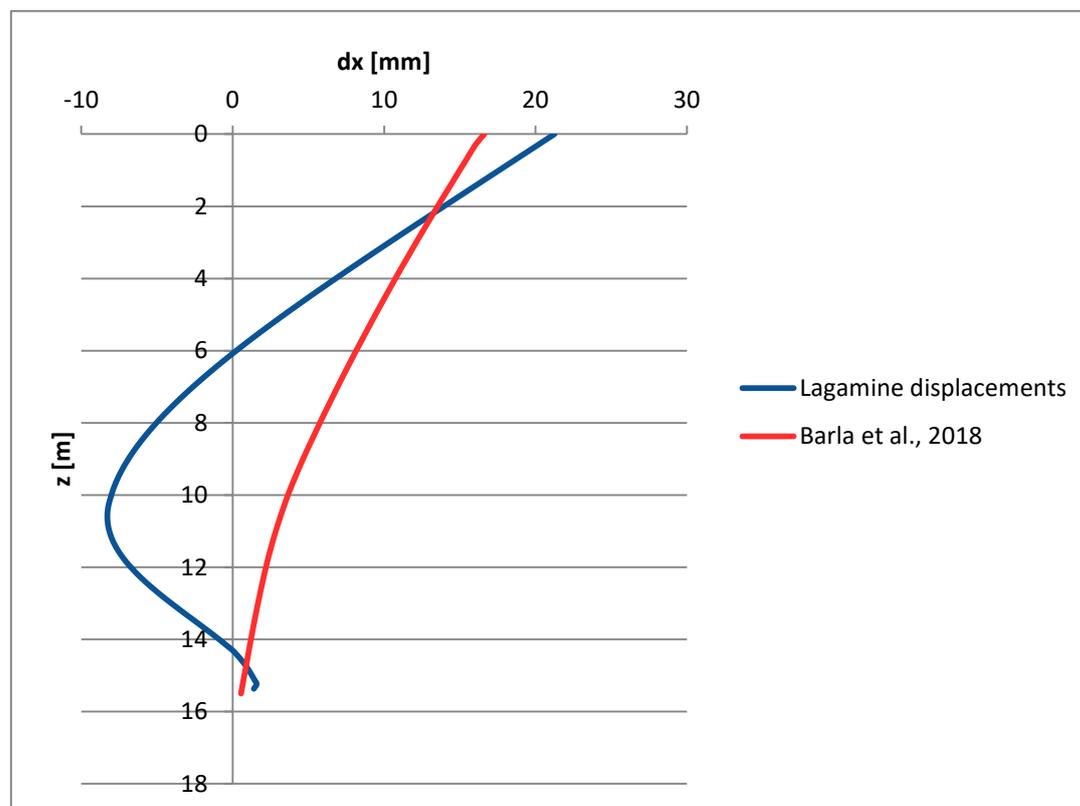


Figure 5.12 Comparison of displacements between Lagamine software and Barla et al. (2018)

Moreover, it is evident that an acceptable comparison can be made by referring to the diagram obtained from the analytical way, the Lagamine analysis and the analysis led by Barla et al. (2018) (Figure 5.13). An important observation must be made about the difference between the three bending moments. Indeed, because of the different boundary conditions, the behavior of the diaphragm wall must be different. The presence of the soil and the bottom slab considered in the analysis of Barla et al. (2018), guarantees a reduced bending moment. Instead, the difference in value of the analytical calculation and the FE analysis, is acceptable due to the thickness of the wall considered in the FEM calculation.

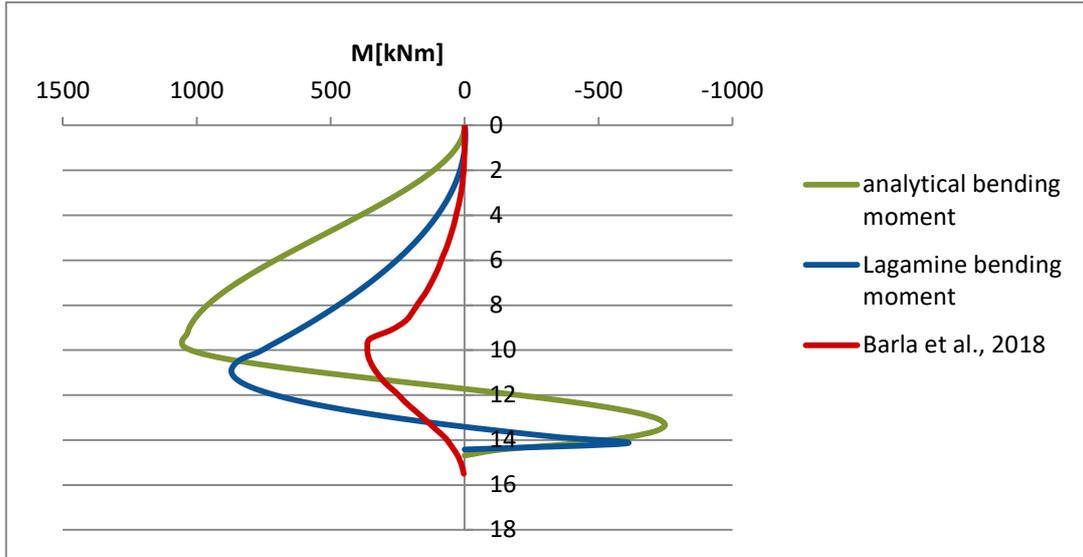


Figure 5.13 Comparison of bending moment between analytical calculation, Lagamine analysis and Barla et al. (2018)

### 5.5.2. Thermal results: activation of the geothermal probes

For the simulation of the geothermal plant, a thermal variation was inserted inside the exchanger tubes, through a time-dependent temperature setting on the nodes where the tubes are supposed to be. Indeed, the 13 pipes are positioned from 2 m below the top of the diaphragm wall, with an interaxis of 1 m one to another. In order to take into account the real position of the tubes, i.e. considering concrete cover, the nodes selected are distant 20 cm from the side (Figure 5.14).

In winter, heat is extracted from the circulating fluid in the pipes, while in summer the reverse process takes place, i.e. the heat is transferred to the fluid. Therefore the temperature trend in the pipes was modeled in a manner consistent with this consideration.

Specifically, a solar year of thermal variation within the probes was divided as follows:

- from day 1 to day 60: constant temperature of 4 ° C;
- from day 60 to day 90: temperature variable linearly increasing from 4 ° C to 14 ° C;
- from day 90 to day 120: constant temperature of 14 ° C;
- from day 120 to day 150: temperature variable linearly increasing from 14 ° C to 26.5 ° C;
- from day 150 to day 240: constant temperature of 26.5 ° C;
- from day 240 to day 270: temperature variable linearly in a decreasing way from 26.5 ° C to 14 ° C;
- from day 270 to day 300: constant temperature of 14 ° C;
- from day 300 to day 330: temperature linearly decreasing from 14 ° C to 4°C;
- from day 330 to day 365: constant temperature of 4 ° C.

To perform the input in the probes for two solar years, 18 analyses cycles were therefore carried out, using the *DEP files* before described, and following reported.

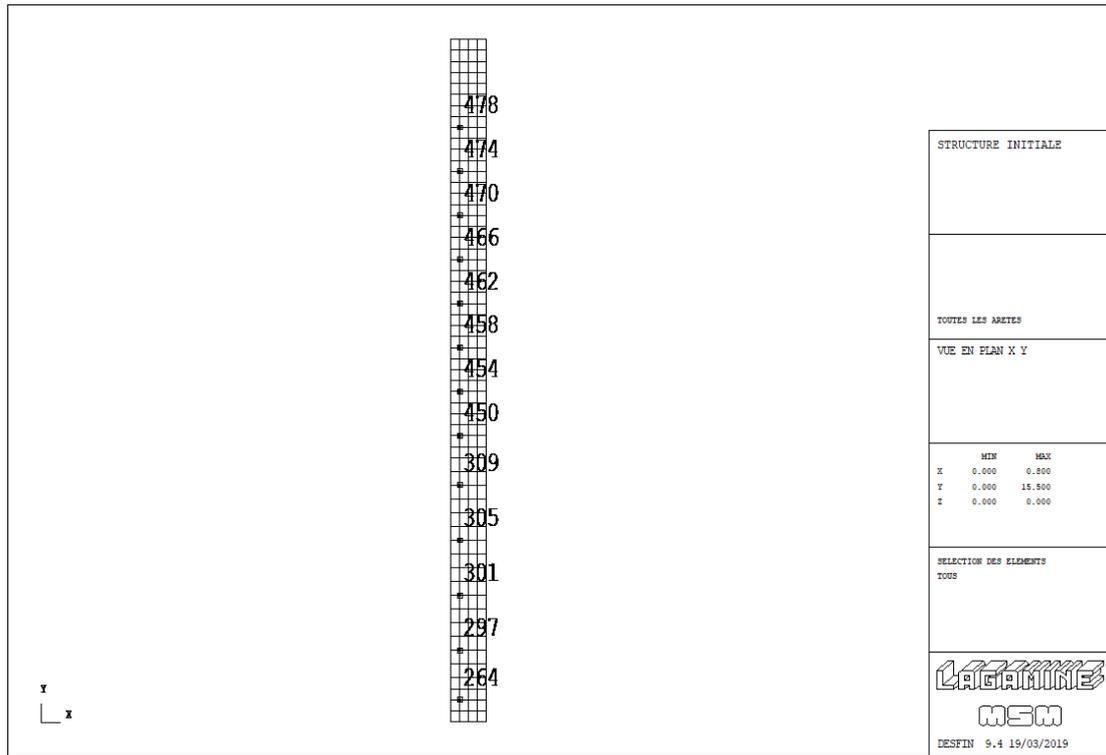


Figure 5.14 Position of the tube into the diaphragms

At day 1, when the exchanger tubes are activated, the temperature of the probes is 4°C (January) and the initial temperature of the structure is 14°C, as agreed by Di Donna (2016). For the difference in temperature, it is possible to locate the pipes in Figure 5.15.

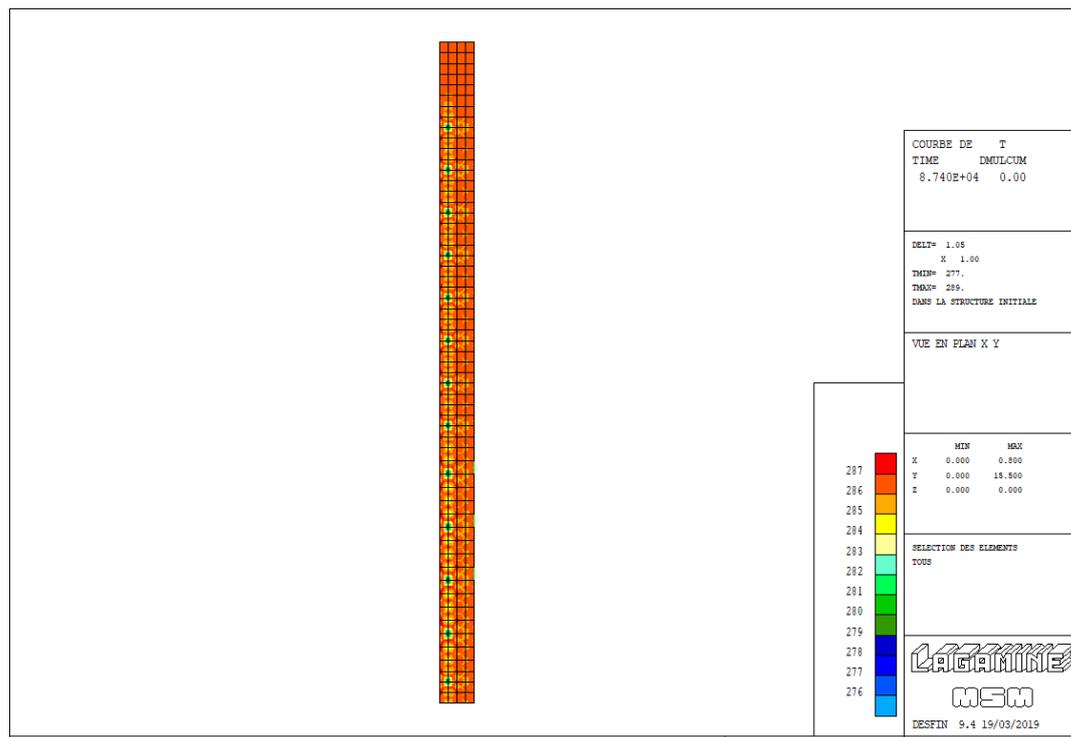


Figure 5.15 Temperature (in kelvin) inside the diaphragm wall at day 1

At day 60 (2 months), are evaluated the bending moment and the displacements, compared with the mechanical ones. As we can see from Figure 5.16 it is possible to highlighting the similarity between the two curves. Indeed, the difference between bending moments is almost perceptible inasmuch is of the order of Newton (Table 6).

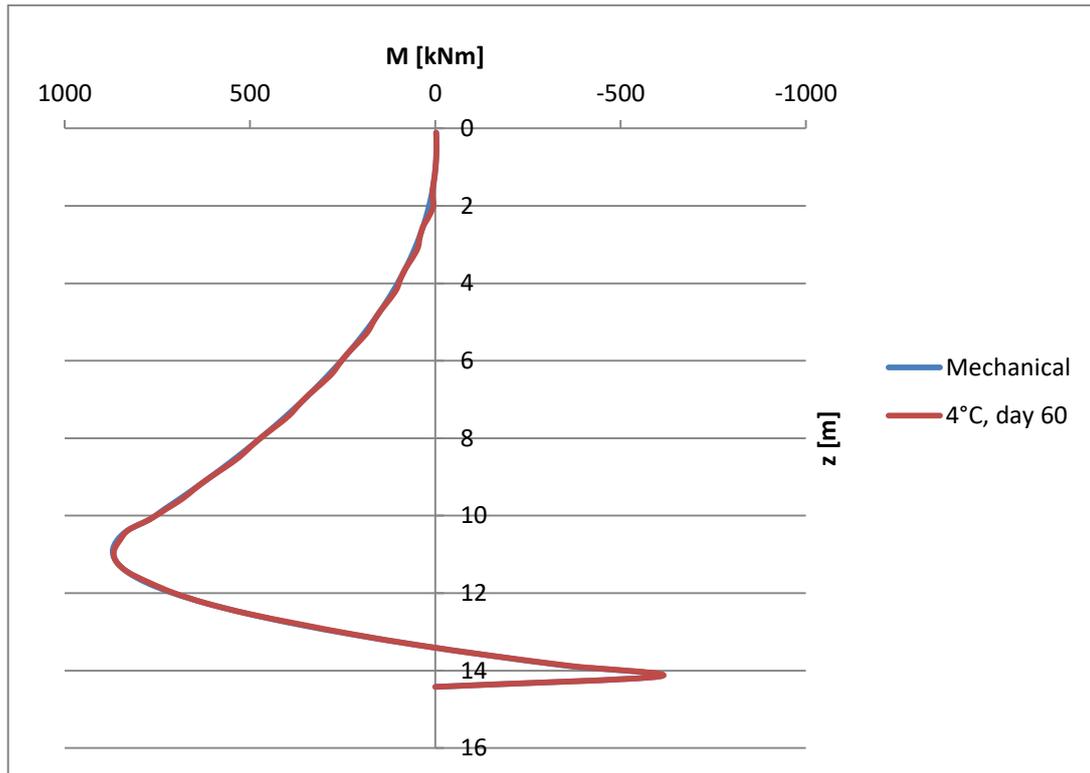


Figure 5.16 Comparison between bending moments at day 1 and day 60 from the activation

Regarding displacements, the difference is more marked as Figure 5.17 shows. Furthermore, because the system is cooled, from  $14^{\circ}\text{C}$  to  $4^{\circ}\text{C}$ , there is a contraction of the diaphragm wall, i.e. head displacement is reduced. Everything is consistent with what is expected from a “Fixed Earth support”.

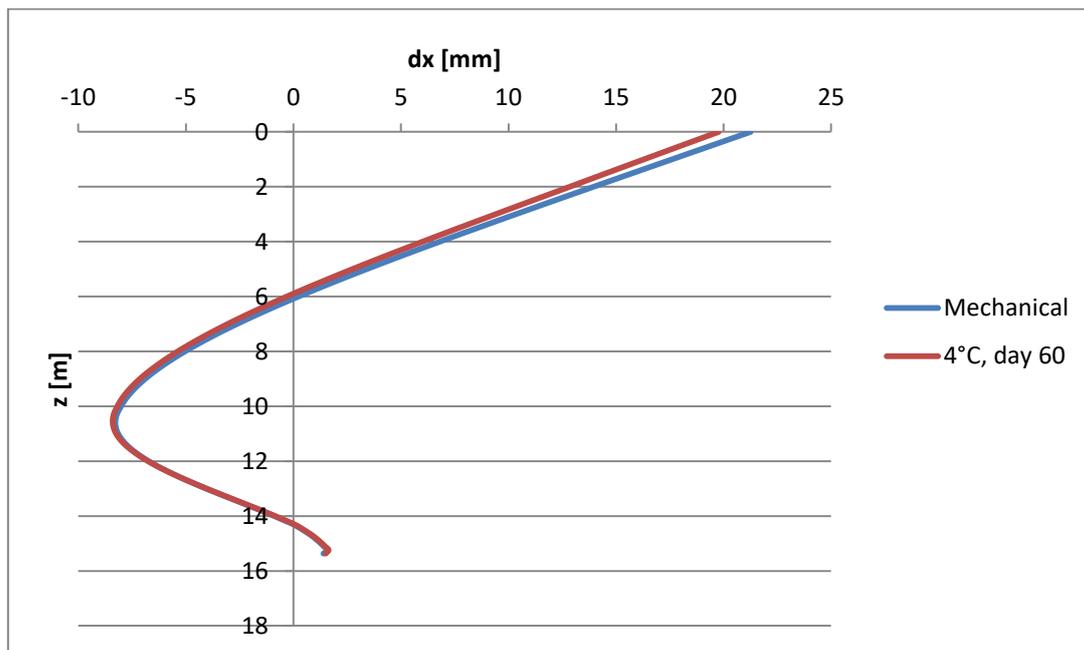


Figure 5.17 Comparison between horizontal displacements at day 1 and day 60 from activation

The comparison in terms of displacements and bending moment, can be done for the whole year, thus the results are reported in the following diagrams. As it is evident, bending moment is quite the same, but the horizontal displacement although change appreciably.

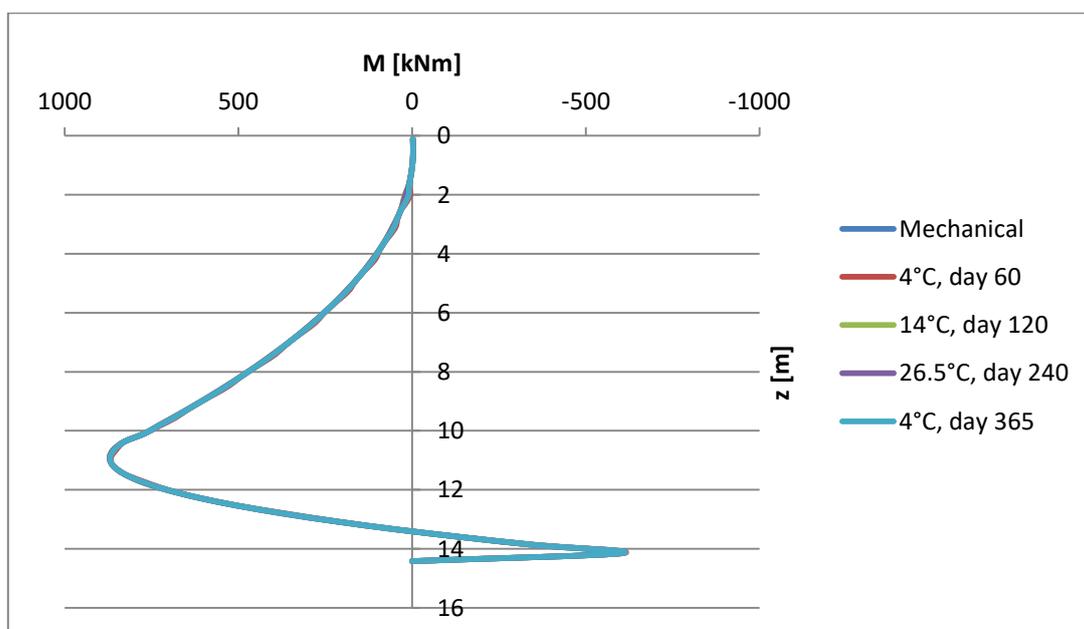


Figure 5.18 Comparison between bending moments in the whole first year of activation

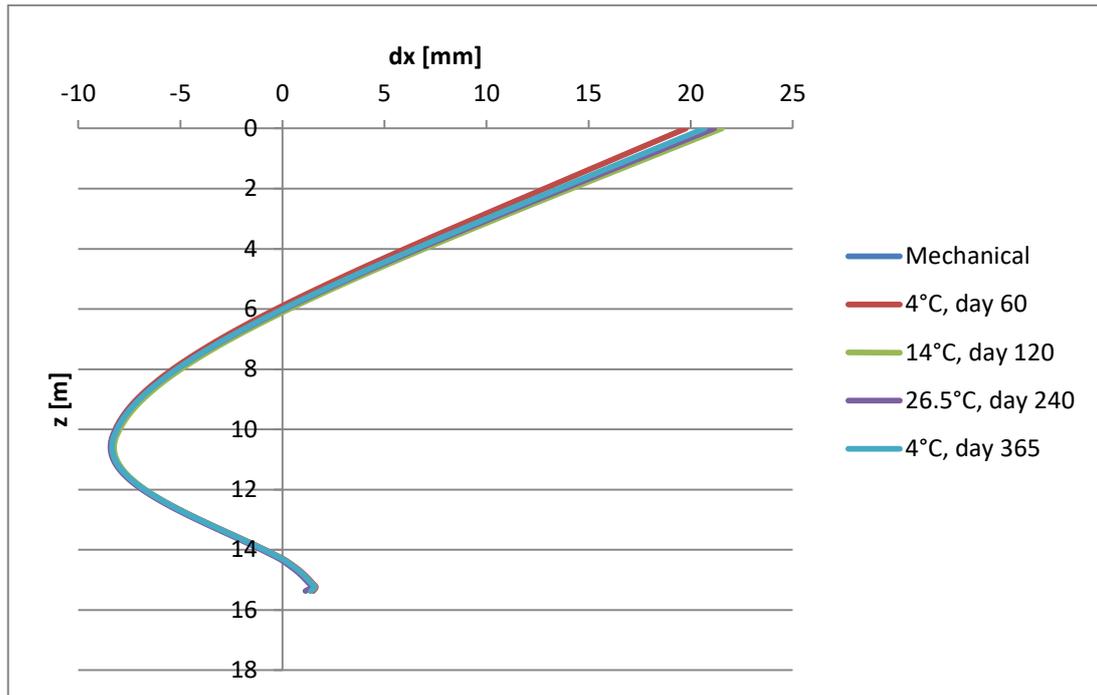


Figure 5.19 Comparison between horizontal displacements in the whole first year of activation

In summer and at the end of the first year, the temperature inside the diaphragm wall is almost uniform along it, due to the presence of the tubes with interaxis of 1 m. In both cases, the temperature is almost everywhere close to the one set by the probes. Obviously, in the area close to the top the temperature is higher inasmuch the geothermal system starts 2 m below (Figures 5.20, 5.21).

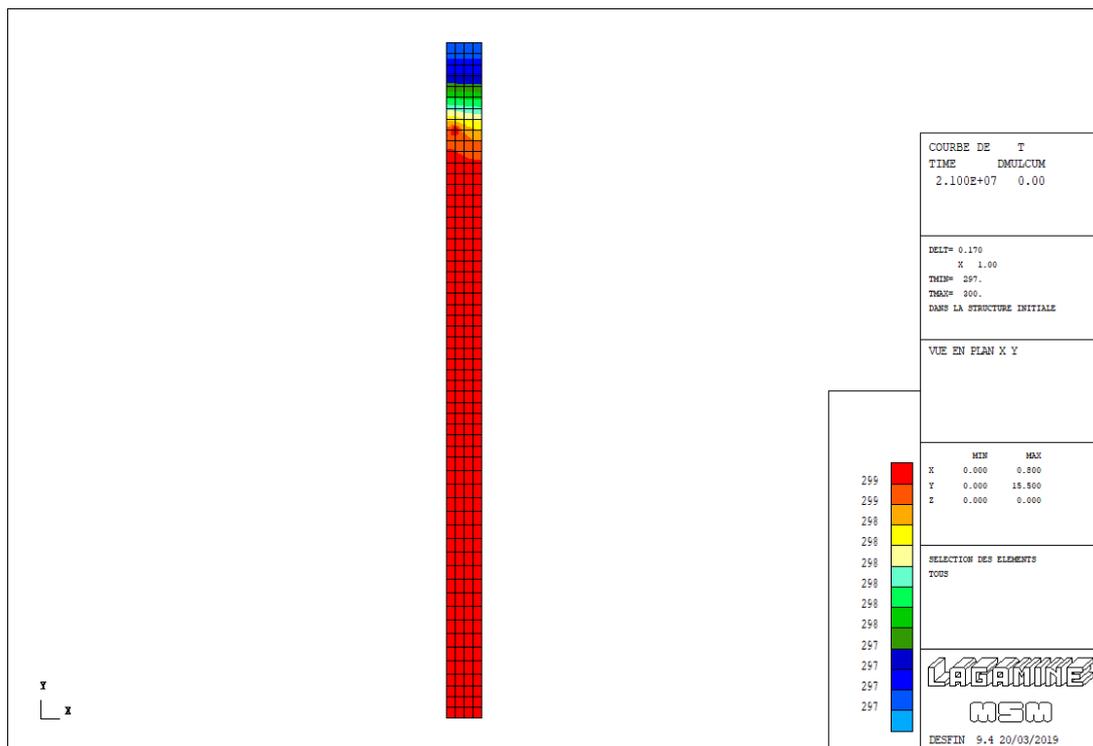


Figure 5.20 Temperature (in kelvin) inside the wall at 240 days (summer)

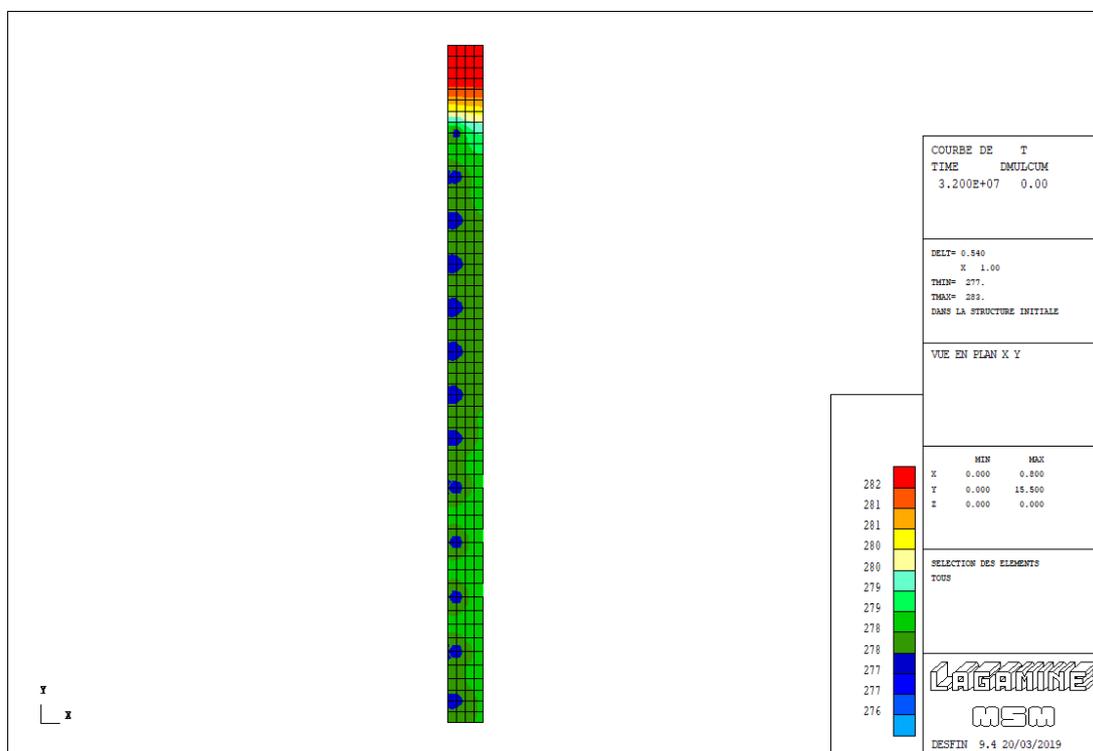


Figure 5.21 Temperature (in kelvin) inside the wall at the end of the first year of activation

The same observations can be made during the second year of the system activation. Thus, bending moment in the second year, is reported in Figure 5.22 and all the horizontal displacement occurred in the two years of activation are plotted in Figure 5.23.

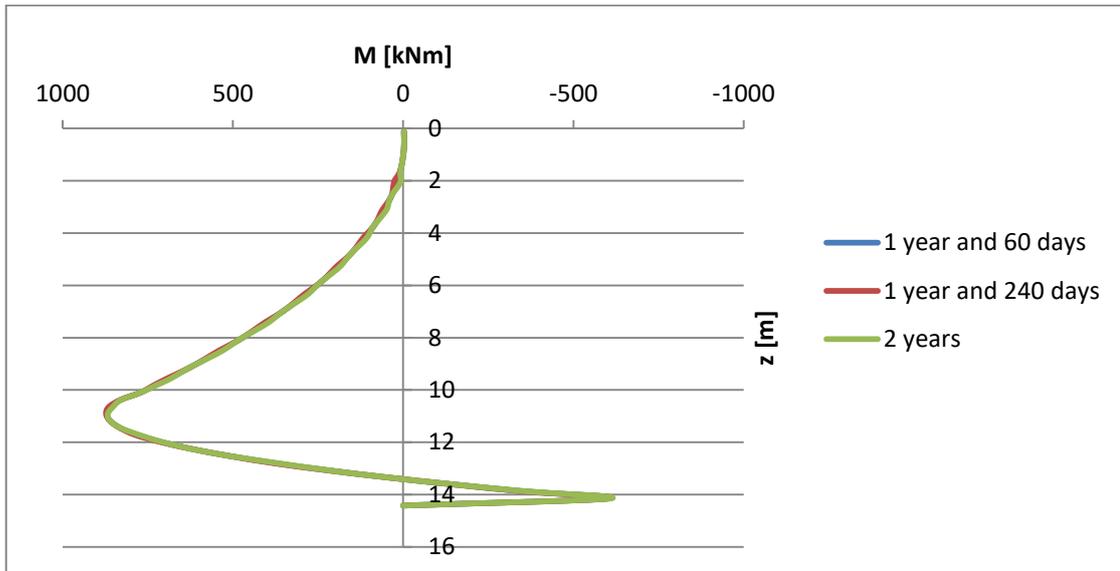


Figure 5.22 Comparison between bending moment in the second year of activation

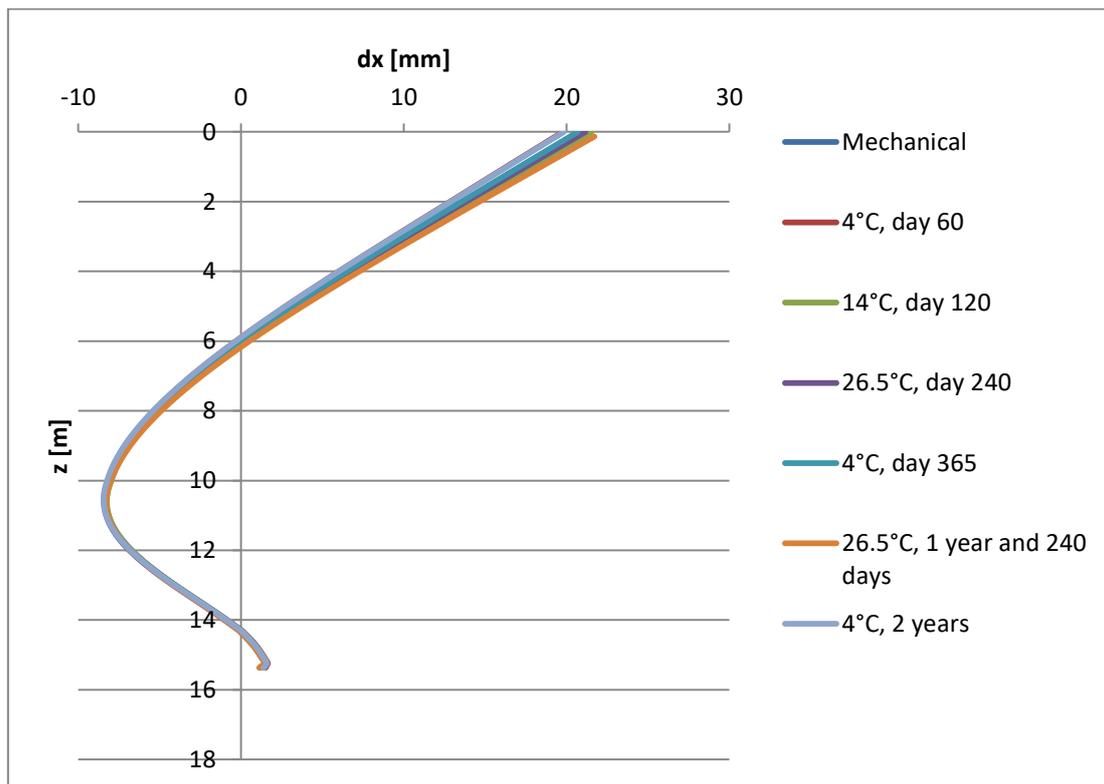


Figure 5.23 Horizontal displacements during the two years of system activation

Similarly to the first year is the temperature along the diaphragm wall during the second year of activation (Figure 5.24, 5.25). Only one interesting observation is that, during the summer of 2 year, the temperature inside the diaphragm is not as uniform as in the first year, even though the difference between the tubes and the wall is just 1 K. Same observation and same difference is noted at the end of the second year.

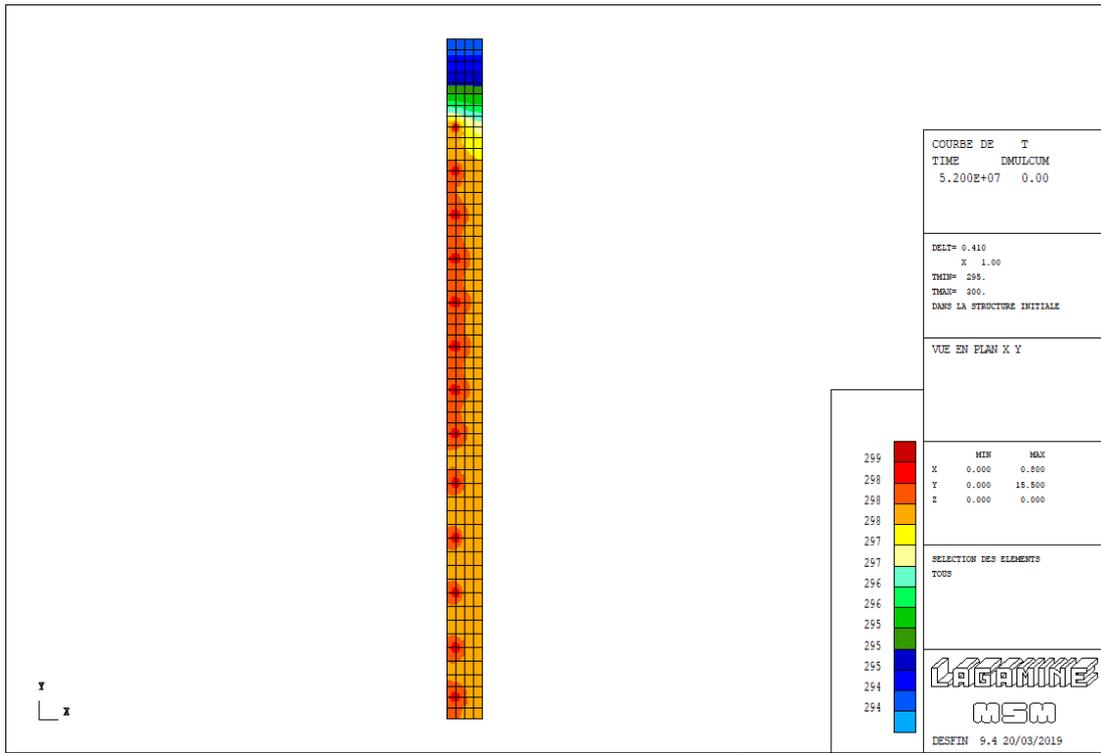


Figure 5.24 Temperature (in kelvin) inside the wall at 1 year and 240 days (summer)

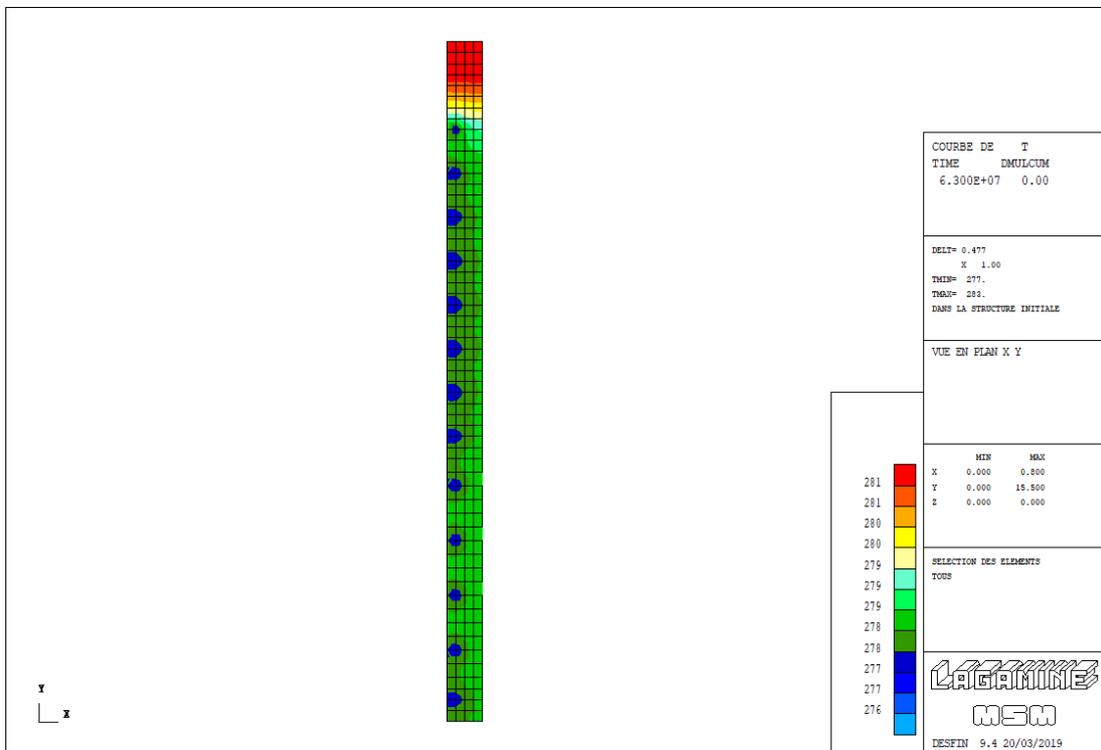


Figure 5.25 Temperature (in kelvin) inside the wall at the end of the second year of activation

### 5.5.3 Comparison of results

From the graphs it is difficult to appreciate the variations undergone by the wall, consequently Tables 6 and 7 show the numerical values that characterize the activation phases of the tubes. To this comparison is added the one referring to the analysis performed by Barla et al. (2018) (see chapter 3.4) so as to be able to draw conclusions later.

Table 6 Comparison with Barla et al. (2018) analysis of the first year of activation

	$M_{max}$ [kNm]	$M_{max}$ Barla [kNm]	$d_{head}$ [mm]	$d_{head}$ Barla [mm]
Mechanical (14°C)	870.4	380	21.25	17
Winter (4°C, day 60)	867.1	460	19.77	16
Summer (26.5°C, day 240)	870.5	352	21.5	22
Winter (4°C, 1 year)	869.3	-	20.7	-

Table 7 Comparison with Barla et al. (2018) analysis of the second year of activation

	$M_{max}$ [kNm]	$M_{max}$ Barla [kNm]	$d_{head}$ [mm]	$d_{head}$ Barla [mm]
Winter (4°C, 1 year and 60 days)	869.9	450	20.69	17
Summer (26.5°C, 1 year and 240 days)	872.7	354	22.21	22
Winter (4°C, 2 years)	867.4	470	19.82	18

The greatest discrepancy between the results obtained by the model presented in this thesis and the ones from Barla et al. (2018), can be seen in the values of bending moments. It is not particularly surprising because of the constraint conditions, which are very different even if the diaphragm wall is actually the same. Indeed, the structure here studied, presents just

two rollers at the bottom of the wall to simulate the “Fixed Earth support” condition and a rotation point on the axis of the structure at 1 m from the bottom of it. On the other hand, the analysis conducted by Barla et al. (2018) involves the same diaphragm wall where a bottom slab is presents. Moreover, the surrounding soil is simulated, i.e. the interaction between soil and wall is different from the one simulated with active and passive thrusts.

For this reasons, it is easy to perceive by intuition that the results must be different. Nevertheless, it is interesting to notice that a comparison between the two analyses can be made regarding the displacements. Indeed, when the geothermal system is not yet active, i.e. only the actions of the soil urges the wall, the difference, in terms of horizontal displacements, is only of 4 mm (Figure 5.12). In addition, the same trend during the years can be noticed: in summer the displacement increases and in winter is reduced (respectively Figure 5.26 and Figure 5.27).

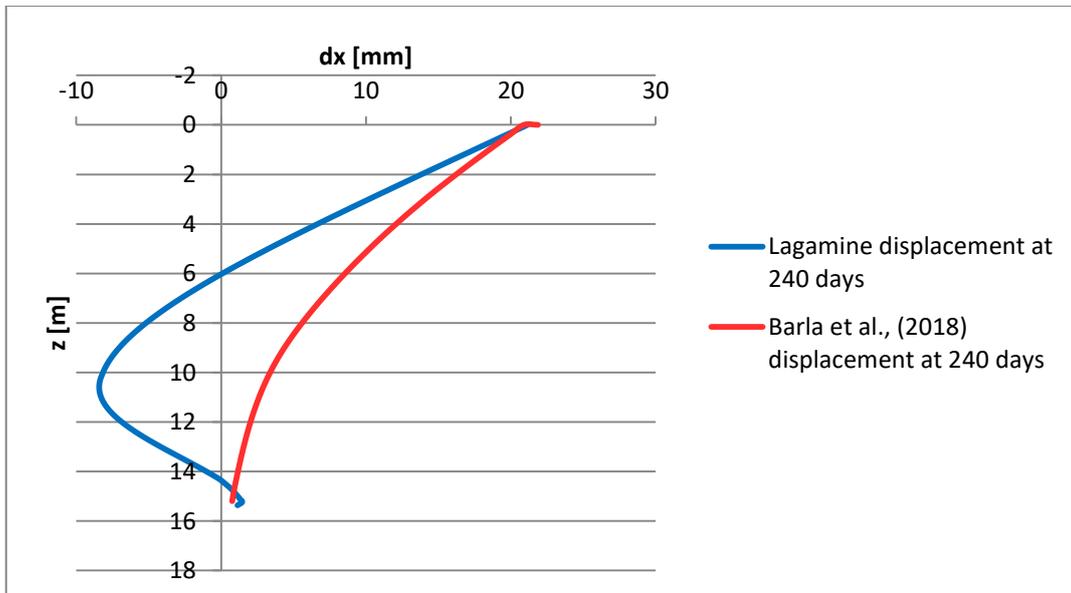


Figure 5.26 Comparison of displacements between Lagamine software and Barla et al. (2018) at 240 days of activation (end of summer)

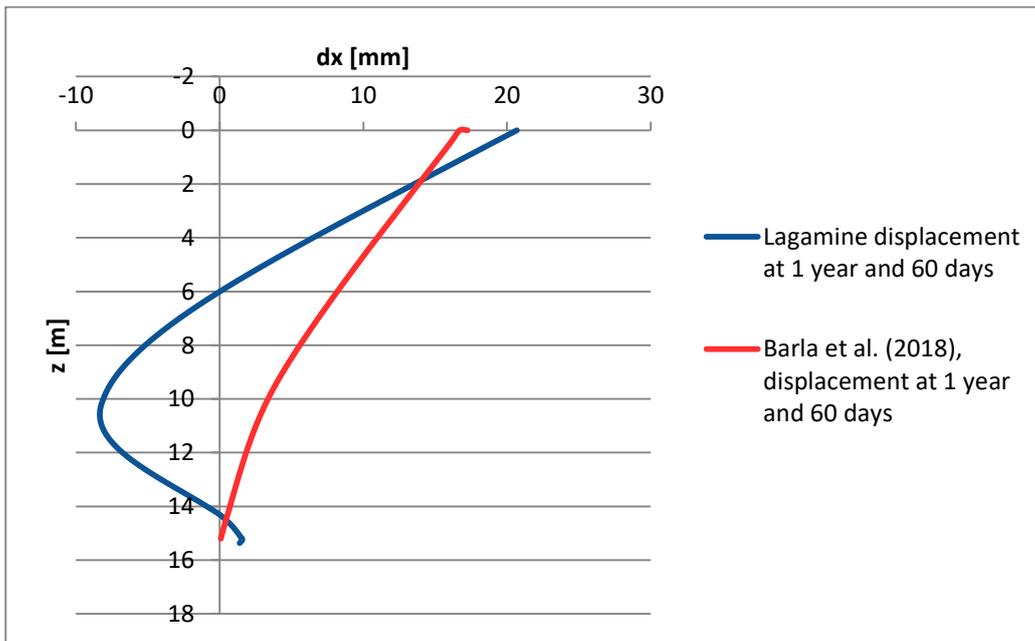


Figure 5.27 Comparison of displacements between Lagamine software and Barla et al., (2018) at 1 year and 60 days of activation (end of winter)

Especially, between the summer and the end of the second year, the variation of displacement to the head is around the 60% of the one proposed by Barla et al. (2018) (Figure 5.28 and Figure 5.29).

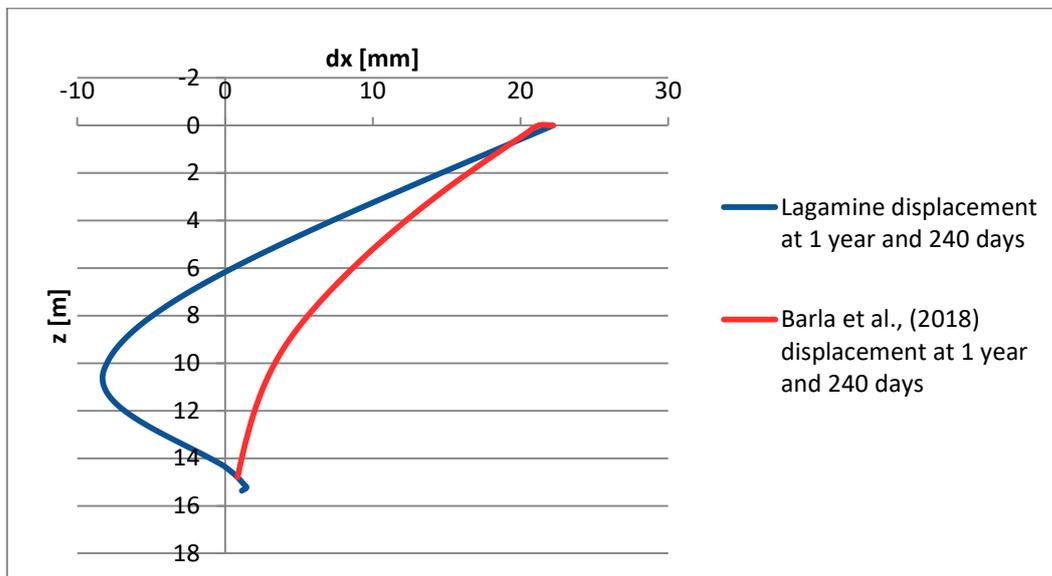


Figure 5.28 Comparison of displacements between Lagamine software and Barla et al. (2018) at 1 year and 240 days of activation (end of summer)

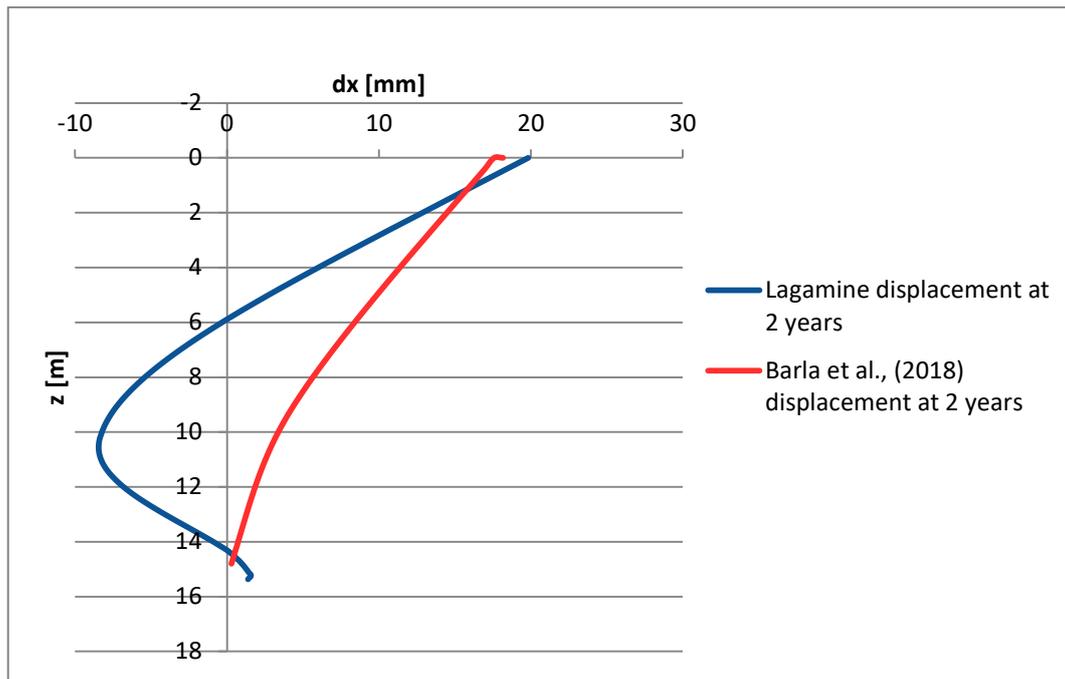


Figure 5.29 Comparison of displacements between Lagamine software and Barla et al., (2018) at 2 years of activation (end of winter)

Important observations must be done regarding the case study of this thesis.

After the mechanical phase, can be noticed a decrease in the maximum head displacement of about 1.5 mm at the end of the first winter phase (after 60 days); subsequently the maximum value at the head of the diaphragm is reached and it is equal to 21.5 mm at the end of the first summer phase (after 240 days) and later, after a year and 60 days (end of winter period) value decreases and so on cyclically. Furthermore, an interesting observation can be made concerning displacements. In the first year of the system activation, the decrease (winter) and increase (summer) of the head displacement is equal to 7%. Nevertheless, during the second year, it is highlighted an increase of 6.8% in displacement between winter (1 year and 60 days) and summer (1 year and 240 days), but at the end of the second year a decrease of 10% shows up. This suggests that increasing

cycles and the transition from summer to winter tend to make the wall more sensitive to displacements. To confirm this statement, an increase between 4.25% and 4.5% in displacements is noted between the same seasons in the two years of system activation.

Thus, in subsequent cycles, i.e. years, the percentages of increase in displacement may increase as well, or can stay constant too. Further analysis would be appropriate.

The results of the analysis brings to conclude that:

- as the temperature increases, the horizontal displacements of the diaphragm wall increase;
- with the continuation of the application cycles of the thermal inputs the values at the end of each period are greater than the previous one; also here it must be reiterated that this observation refers to two years of simulation with activated implant and does not ensure the same progression for the years to come.

## 6. Conclusions

This thesis is based on the study of the thermo-mechanical behavior of a diaphragm wall, part of the underground car park of via Ventimiglia, Turin. The aim was to analyze the effects that a geothermal system induces within a geostructure from a thermo-mechanical point of view.

The geothermal system as the one considered, allows to heat and cool the concerned area, in this case the inside of the car park, just exchanging heat with the soil. The technology exploits the shallow geothermal resource reducing dependence on fossil fuels.

Introducing the concept of geothermal energy and its different forms was fundamental to understand how the technology works. At the base of this, energy geostructure has been described. Thanks to the huge surface in contact with the ground, tunnels are perhaps the ones that can best exploit the geothermal system. Nevertheless, energy pipes and energy diaphragm wall are widely used around the world.

Diaphragm wall represents an excellent solution for exchanging heat with the ground given the particularly large surfaces. The key point of the energy geostructures is that are able to combine structural function with the

energy one. Thus, with just one structure is possible to merge two really important functions. Indeed, a great saving in construction is guaranteed because only an additional operation to install the circuit is required. The pipes must be bound on the reinforcement cage and connect to the main pipeline which will join the geothermal heat pump.

It is not enough to study the energy aspect in terms of heat transfer capacity. To use a system like this, which requires an appropriate project and an initial expenditure of money, stresses and displacements must also be taken into account.

Although a similar analysis already exists of the same diaphragm wall, it has been thought to use different software and to study only the decontextualized diaphragm wall. For this reason, no soil and no slab was modeled. The only action taken into consideration was the one of the soil, acting as a result of the excavation.

After studying the mechanical behavior due to the action of the thrusts, thermo-mechanical analysis was started. Thus, the 13 pipes were activated, causing the internal temperature to vary according to the season considered. The analysis forecasted two years of observation, with a total of 18 cycles. The results showed constancy in bending moment but an increase of displacement at the head of the diaphragm around 5%, compared to the values obtained by mechanical analysis only, going from 21.25 mm to 22.3 mm. The same percentage was noticed between the displacements of the head in the same season of the two years considered.

From this thesis work, it emerged that taking into account only the diaphragm wall without the actual in situ conditions, allows to overestimate the mechanical displacements and in any case to have the

same order of magnitude of displacements in system activation. Moreover, even if the variation of the bending moment is not appreciable, it is always in favor of safety, since the bending moment is higher than the one of the real case.

Possible developments of this work could take into account the several constraint conditions to which a real diaphragm wall is subjected. For example, more than the bottom slab, an upper slab could be considered in order to simulate the car parking roof. From a thermic point of view, the observation period can be extended to understand if the variations in displacement will stabilize or will continue to increase.

Certainly the technology deserves attention and further studies, as the benefits offered are not negligible and for sure it is an excellent to solution against the pollution problem that today more than ever afflicts our society.



# Appendix 1

## Gmail file : Geometry and boundary conditions

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7 0.0 15.5
8 0.8 15.5
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2 1 2 4 0 0 4
3 1 4 6 0 0 16
4 1 6 8 0 0 38
5 1 8 7 0 0 4
6 1 7 5 0 0 38
7 1 5 3 0 0 16
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## Data file : Properties, elements, nodes and laws

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## Appendix 1

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## Appendix 1

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# Appendix 1

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GRAVI

-9.81

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## Appendix 1

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## Appendix 1

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8 4 1 8 4 2  
521 816 558 672 559 820 522 634  
8 4 1 8 4 2  
522 820 559 673 130 131 132 635  
8 4 1 8 4 2  
257 256 4 54 55 677 523 636  
8 4 1 8 4 2  
523 677 55 56 57 681 524 637  
8 4 1 8 4 2  
524 681 57 58 59 685 525 638  
8 4 1 8 4 2  
525 685 59 60 61 689 526 639  
8 4 1 8 4 2  
526 689 61 62 63 693 527 640  
8 4 1 8 4 2  
527 693 63 64 65 697 528 641  
8 4 1 8 4 2  
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8 4 1 8 4 2  
529 701 67 68 69 705 530 643  
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530 705 69 70 71 709 531 644  
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8 4 1 8 4 2  
532 713 73 74 75 717 533 646  
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533 717 75 76 77 721 534 647  
8 4 1 8 4 2  
534 721 77 78 79 725 535 648  
8 4 1 8 4 2  
535 725 79 80 81 729 536 649  
8 4 1 8 4 2  
536 729 81 82 83 733 537 650  
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537 733 83 84 85 737 538 651  
8 4 1 8 4 2  
538 737 85 86 87 741 539 652  
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539 741 87 88 89 745 540 653  
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540 745 89 90 91 749 541 654  
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541 749 91 92 93 753 542 655  
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## Appendix 1

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542 753 93 94 95 757 543 656  
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544 761 97 98 99 765 545 658  
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545 765 99 100 101 769 546 659  
8 4 1 8 4 2  
546 769 101 102 103 773 547 660  
8 4 1 8 4 2  
547 773 103 104 105 777 548 661  
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548 777 105 106 107 781 549 662  
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549 781 107 108 109 785 550 663  
8 4 1 8 4 2  
550 785 109 110 111 789 551 664  
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551 789 111 112 113 793 552 665  
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8 4 1 8 4 2  
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8 4 1 8 4 2  
554 801 117 118 119 805 555 668  
8 4 1 8 4 2  
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8 4 1 8 4 2  
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8 4 1 8 4 2  
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8 4 1 8 4 2  
558 817 125 126 127 821 559 672  
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LICHA  
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LICHA  
4 0  
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8 248 247  
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245 244 243  
2 4  
243 242 1  
LICHA  
16 0  
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3 23 24  
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24 25 26  
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26 27 28  
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28 29 30  
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30 31 32  
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32 33 34  
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38 39 40  
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40 41 42  
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42 43 44  
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44 45 46  
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46 47 48  
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 48 49 50  
 2 5  
 50 51 52  
 2 5  
 52 53 4  
 LICHA  
 4 0  
 2 6  
 2 16 17  
 2 6  
 17 18 19  
 2 6  
 19 20 21  
 2 6  
 21 22 3

**Loading File: steps of calculation (1-60 days)**

2 3 4 8 0 0 0  
  
 1 -1.9999 1 1 1 2 1 30 0 0 1  
 3 0 0 0 0 0 0 0 0  
 1.0E-05 1.0 0.0 0.0 0.0 0.0 0.0 0.0  
 2.0 5.2E+06 0.001 10. 0.0 0.0  
  
 1.30E+06 0.0 0.0 0.001 0.001 0 0 0 0 1  
  
 0.0000000 0.0 0  
 1300000.00 0.0 0  
 2600000.00 0.0 0  
 3900000.00 0.0 0  
 5200000.00 0.0 0

**Loading File: steps of calculation (60- 120 days)**

3 2 4 18 0 0 0  
  
 1 -1.9999 1 1 1 2 1 30 0 0 1  
 3 0 0 0 0 0 0 0 0  
 1.0E-05 1.0 0.0 0.0 0.0 0.0 0.0 0.0  
 1.0 1.00E7 0.001 10.0 0.0 0.0  
  
 5.20E6 0.1 0.0 0.001 0.001 0 0 0 0 1  
  
 5200000.00 0.0 0  
 6500000.00 0.0 0  
 7800000.00 0.0 0  
 8900000.00 0.0 0  
 10000000.0 0.0 0

**Loading File: steps of calculation (120-240 days)**

3 2 4 18 0 0 0  
  
 1 -1.9999 1 1 1 2 1 30 0 0 1  
 3 0 0 0 0 0 0 0 0  
 1.0E-05 1.0 0.0 0.0 0.0 0.0 0.0 0.0  
 1.0 2.10E7 0.001 10.0 0.0 0.0  
  
 1.00E7 0.1 0.0 0.001 0.001 0 0 0 0 1  
  
 10000000.0 0.0 0  
 13000000.0 0.0 0  
 16000000.0 0.0 0  
 18000000.0 0.0 0  
 21000000.0 0.0 0

**Loading File: steps of calculation (240-365 days)**

3 2 4 18 0 0 0  
  
 1 -1.9999 1 1 1 2 1 30 0 0 1  
 3 0 0 0 0 0 0 0 0  
 1.0E-05 1.0 0.0 0.0 0.0 0.0 0.0 0.0  
 1.0 3.20E7 0.001 10.0 0.0 0.0  
  
 2.10E7 0.1 0.0 0.001 0.001 0 0 0 0 1  
  
 21000000.0 0.0 0  
 24000000.0 0.0 0  
 26000000.0 0.0 0  
 29000000.0 0.0 0  
 32000000.0 0.0 0

**LIC file: loading steps**

4  
 0  
 0.0 0.0

```
1.30E+06
0.0 0.0
2.60E+06
0.5 0.0
5.20E+06
1.0 0.0
```

**PRI file: printed nodes and elements**

```
NODES
1 1 6 -8 136 -248
2 1 6 -8 136 -248
3 1 6 -8 136 -248
5 1 6 -8 136 -248
16 1 6 -8 136 -248
17 1 6 -8 136 -248
```

```
ELEMT
1 1 -310
2 1 -310
3 1 -310
```

```
REACT
```

```
TIMES
```

**DEP file: temperature steps (4°C-14°C)**

```
3 13
5.20E+06
264 5 277.0
297 5 277.0
301 5 277.0
305 5 277.0
309 5 277.0
450 5 277.0
454 5 277.0
458 5 277.0
462 5 277.0
466 5 277.0
470 5 277.0
474 5 277.0
478 5 277.0
7.80E+06
264 5 287.0
297 5 287.0
301 5 287.0
305 5 287.0
309 5 287.0
450 5 287.0
454 5 287.0
458 5 287.0
462 5 287.0
466 5 287.0
470 5 287.0
474 5 287.0
478 5 287.0
1.00E+07
264 5 287.0
297 5 287.0
301 5 287.0
305 5 287.0
309 5 287.0
450 5 287.0
454 5 287.0
458 5 287.0
462 5 287.0
466 5 287.0
470 5 287.0
474 5 287.0
478 5 287.0
```

**DEP file: temperature steps (14°C-26.5°C)**

```
3 13
1.00E+07
264 5 287.0
297 5 287.0
301 5 287.0
305 5 287.0
309 5 287.0
450 5 287.0
454 5 287.0
458 5 287.0
462 5 287.0
466 5 287.0
470 5 287.0
474 5 287.0
478 5 287.0
1.30E+07
264 5 299.5
297 5 299.5
301 5 299.5
```

305 5 299.5  
309 5 299.5  
450 5 299.5  
454 5 299.5  
458 5 299.5  
462 5 299.5  
466 5 299.5  
470 5 299.5  
474 5 299.5  
478 5 299.5  
2.10E+07  
264 5 299.5  
297 5 299.5  
301 5 299.5  
305 5 299.5  
309 5 299.5  
450 5 299.5  
454 5 299.5  
458 5 299.5  
462 5 299.5  
466 5 299.5  
470 5 299.5  
474 5 299.5  
478 5 299.5

**DEP file: temperature steps (26.5°C-14°C)**

5 13  
2.10E+07  
264 5 299.5  
297 5 299.5  
301 5 299.5  
305 5 299.5  
309 5 299.5  
450 5 299.5  
454 5 299.5  
458 5 299.5  
462 5 299.5  
466 5 299.5  
470 5 299.5  
474 5 299.5  
478 5 299.5  
2.40E+07  
264 5 287.0  
297 5 287.0  
301 5 287.0  
305 5 287.0  
309 5 287.0  
450 5 287.0  
454 5 287.0  
458 5 287.0  
462 5 287.0  
466 5 287.0  
470 5 287.0  
474 5 287.0  
478 5 287.0  
2.60E+07  
264 5 287.0  
297 5 287.0  
301 5 287.0  
305 5 287.0  
309 5 287.0  
450 5 287.0  
454 5 287.0  
458 5 287.0  
462 5 287.0  
466 5 287.0  
470 5 287.0  
474 5 287.0  
478 5 287.0  
2.90E+07  
264 5 277.0  
297 5 277.0  
301 5 277.0  
305 5 277.0  
309 5 277.0  
450 5 277.0  
454 5 277.0  
458 5 277.0  
462 5 277.0  
466 5 277.0  
470 5 277.0  
474 5 277.0  
478 5 277.0  
3.20E+07  
264 5 277.0  
297 5 277.0  
301 5 277.0  
305 5 277.0  
309 5 277.0  
450 5 277.0  
454 5 277.0

458 5 277.0  
462 5 277.0  
466 5 277.0  
470 5 277.0  
474 5 277.0  
478 5 277.0

**DEP file: temperature steps (2th year)**

10 13  
3.20E+07  
264 5 277.0  
297 5 277.0  
301 5 277.0  
305 5 277.0  
309 5 277.0  
450 5 277.0  
454 5 277.0  
458 5 277.0  
462 5 277.0  
466 5 277.0  
470 5 277.0  
474 5 277.0  
478 5 277.0  
3.70E+07  
264 5 277.0  
297 5 277.0  
301 5 277.0  
305 5 277.0  
309 5 277.0  
450 5 277.0  
454 5 277.0  
458 5 277.0  
462 5 277.0  
466 5 277.0  
470 5 277.0  
474 5 277.0  
478 5 277.0  
3.90E+07  
264 5 287.0  
297 5 287.0  
301 5 287.0  
305 5 287.0  
309 5 287.0  
450 5 287.0  
454 5 287.0  
458 5 287.0  
462 5 287.0  
466 5 287.0  
470 5 287.0  
474 5 287.0  
478 5 287.0  
4.20E+07  
264 5 287.0  
297 5 287.0  
301 5 287.0  
305 5 287.0  
309 5 287.0  
450 5 287.0  
454 5 287.0  
458 5 287.0  
462 5 287.0  
466 5 287.0  
470 5 287.0  
474 5 287.0  
478 5 287.0  
4.40E+07  
264 5 299.5  
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301 5 299.5  
305 5 299.5  
309 5 299.5  
450 5 299.5  
454 5 299.5  
458 5 299.5  
462 5 299.5  
466 5 299.5  
470 5 299.5  
474 5 299.5  
478 5 299.5  
5.20E+07  
264 5 299.5  
297 5 299.5  
301 5 299.5  
305 5 299.5  
309 5 299.5  
450 5 299.5  
454 5 299.5  
458 5 299.5  
462 5 299.5  
466 5 299.5  
470 5 299.5

## Appendix 1

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474 5 299.5  
478 5 299.5  
5.50E+07  
264 5 287.0  
297 5 287.0  
301 5 287.0  
305 5 287.0  
309 5 287.0  
450 5 287.0  
454 5 287.0  
458 5 287.0  
462 5 287.0  
466 5 287.0  
470 5 287.0  
474 5 287.0  
478 5 287.0  
5.70E+07  
264 5 287.0  
297 5 287.0  
301 5 287.0  
305 5 287.0  
309 5 287.0  
450 5 287.0  
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458 5 287.0  
462 5 287.0  
466 5 287.0  
470 5 287.0  
474 5 287.0  
478 5 287.0  
6.00E+07  
264 5 277.0  
297 5 277.0  
301 5 277.0  
305 5 277.0  
309 5 277.0  
450 5 277.0  
454 5 277.0  
458 5 277.0  
462 5 277.0  
466 5 277.0  
470 5 277.0  
474 5 277.0  
478 5 277.0  
6.30E+07  
264 5 277.0  
297 5 277.0  
301 5 277.0  
305 5 277.0  
309 5 277.0  
450 5 277.0  
454 5 277.0  
458 5 277.0  
462 5 277.0  
466 5 277.0  
470 5 277.0  
474 5 277.0  
478 5 277.0

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